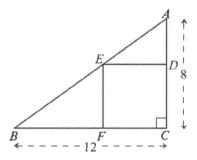
# Lengths in Rectilinear Figures

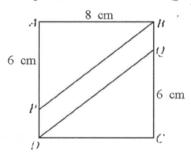
1. ABC is a triangle right-angled at C. AC = 8; BC = 12. If CDEF is a square, then ED =



- A. 3.6
- B. 4
- C. 4.8
- **D.** 6
- E. 6.4

[SP-CE-MATHS A2-51]

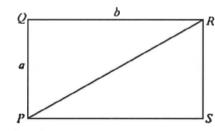
2. In the figure, ABCD is a square of side 8 cm. If AP = CQ = 6 cm, what is the distance between the parallel lines PB and DQ?



- **A.** 2.0 cm
- **B.** 1.8 cm
- C. 1.6 cm
- D. 1.5 cm
- E. 1.2 cm

[1978-CE-MATHS 2-26]

3. In the figure, PQRS is a rectangle. PQ = a, QR = b. What is the distance between Q and PR?



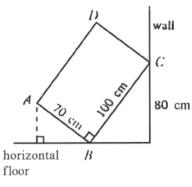
- A.  $\frac{a^2+b^2}{ab}$
- $\mathbf{B.} \quad \frac{\sqrt{a^2 + b^2}}{ab}$
- C.  $\sqrt{\frac{a^2+b^2}{ab}}$

$$\mathbf{D.} \quad \sqrt{\frac{ab}{a^2 + b^2}}$$

$$\mathbf{E.} \quad \frac{ab}{\sqrt{a^2+b^2}}$$

[1978-CE-MATHS A2-53]

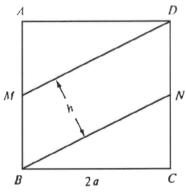
4. In the figure, ABCD represents the cross-section of a rectangular box leaning against a vertical wall. AB = 70 cm, BC = 100 cm. If C is 80 cm above the floor, how high is A above the floor?



- **A.** 38 cm
- **B.** 40 cm
- C. 42 cm
- **D.** 45 cm
- E. 56 cm

[1979-CE-MATHS 2-18]

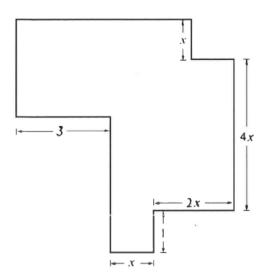
5. In the figure, ABCD is a square of side 2a. M and N are the mid-points of AB and CD respectively. h is the height of the parallelogram MBND. h =



- **A.**  $\frac{1}{2}a$ .
- **B.**  $\frac{2}{\sqrt{5}}a$
- C.  $\frac{\sqrt{5}}{2}a$
- **D.**  $\frac{2}{\sqrt{3}}a$
- $\mathbf{E.} \quad \frac{\sqrt{2}}{4}a$

[1982-CE-MATHS 2-50]

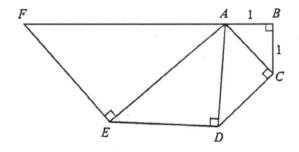
6. In the figure, all the corners are right-angled. If the perimeter of the figure is 40, then x =



- A. 0.25
- **B**. 2
- C. 2.5
- **D**. 4
- E. 4.5

[1983-CE-MATHS 2-11]

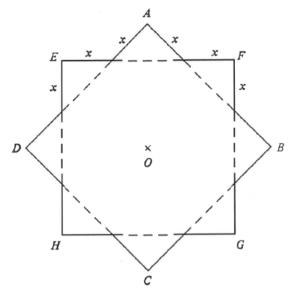
7. In the figure, ABC, ACD, ADE and AEF are right angled isosceles triangles. If AB = BC = 1, how long is AF?



- **A.**  $2\sqrt{5}$
- **B.** 4
- C.  $2\sqrt{3}$
- **D**. 3
- E.  $\sqrt{5}$

[1986-CE-MATHS 2-24]

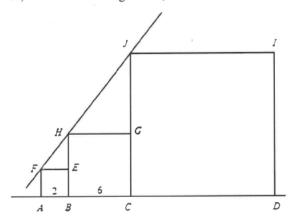
8. In the figure, ABCD and EFGH are two squares of side 1. They are placed one upon the other with their centres both at O to form a star with 16 sides, each of length x. Find x.



- **A.**  $\frac{2}{7}$
- **B.**  $\frac{1}{3}$
- c.  $\frac{2}{5}$
- **D.**  $\frac{1}{2+\sqrt{2}}$
- E.  $\frac{1}{1+\sqrt{2}}$

[1986-CE-MATHS 2-48]

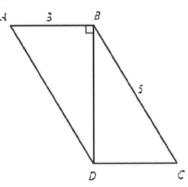
9. In the figure, ABEF, BCGH and CDIJ are three squares. If AB = 2 and BC = 6 and F, H, J lie on a straight line, then CD =



- A. 8.
- **B.** 10.
- C. 12.
- **D.** 16.
- E. 18.

[1988-CE-MATHS 2-25]

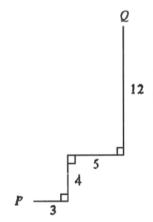
10. In the figure, ABCD is a parallelogram.  $AB \perp BD$ , AB = 3 and BC = 5. AC =



- A. 10.
- **B.** 12.
- C.  $\sqrt{13}$ .
- **D.**  $\sqrt{26}$ .
- E.  $2\sqrt{13}$

[1988-CE-MATHS 2-53]

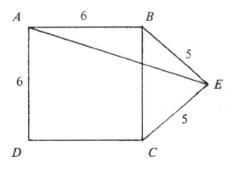
11. Referring to the figure, find the length of the line segment joining P and Q.



- A. 25
- **B.**  $10\sqrt{5}$
- **C.** 18
- **D.**  $8\sqrt{5}$
- **E.**  $\sqrt{194}$

[1989-CE-MATHS 2-22]

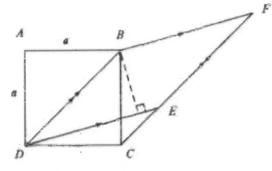
12. In the figure, ABCD is a square with side 6. If BE = CE = 5, find AE.



- **A.**  $\sqrt{61}$
- **B.** 9
- **C.** 10
- **D.**  $6\sqrt{3}$
- E.  $\sqrt{109}$

[1992-CE-MATHS 2-25]

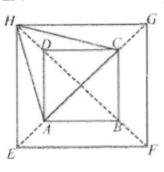
13. In the figure, *ABCD* is a square of side *a* and *BDEF* is a rhombus. *CEF* is a straight line. Find the length of the perpendicular from *B* to *DE*.



- A.  $\frac{1}{2}a$
- **B.**  $\frac{2a}{\sqrt{3}}$
- C.  $\frac{a}{\sqrt{2}}$
- **D.**  $\frac{\sqrt{3}}{2}a$
- E. 0

[1992-CE-MATHS 2-54]

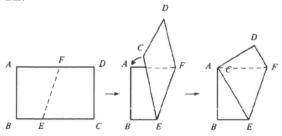
14. In the figure, *ABCD* and *EFGH* are two squares and *ACH* is an equilateral triangle. Find *AB*: *EF*.



- **A.** 1:2
- **B.** 1:3
- **C.**  $1:\sqrt{2}$
- **D.**  $1:\sqrt{3}$
- **E.**  $\sqrt{2}:\sqrt{3}$

[1993-CE-MATHS 2-52]

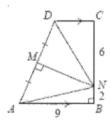
15. In the figure, a rectangular piece of paper ABCD is folded along EF so that C and Acoincide. If AB = 12 cm, BC = 16 cm, find



- A. 3.5 cm
- В. 4.5 cm
- C. 5 cm
- D. 8 cm
- 12.5 cm

[1993-CE-MATHS 2-53]

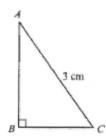
16. In the figure, ABCD is a trapezium with AB // DC,  $\angle ABC = 90^{\circ}$  and MN is the perpendicular bisector of AD. If AB = 9, BN = 2 and NC = 6, find CD.



- C.
- $\sqrt{41}$ D.
- $\sqrt{113}$

[1994-CE-MATHS 2-54]

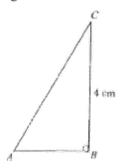
17. In the figure, AB = 2BC. Find BC correct to 3 significant figures.



- 0.775 cm
- В. 1.00 cm
- 1.34 cm C.
- 1.73 cm D.
- 1.80 cm E.

[1998-CE-MATHS 2-31]

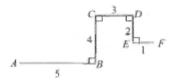
18. In the figure, AC = 3AB. Find AB correct to 3 significant figures.



- 1.26 cm
- 1.41 cm B.
- 1.79 cm C.
- 2.83 cm

[2002-CE-MATHS 2-25]

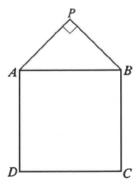
19. In the figure, the length of the line segment joining A and F is



[2005-CE-MATHS 2-30]

## Areas of Rectilinear Figures

20. In the figure, ABCD is a square of area 16 cm<sup>2</sup>. APB is an isosceles triangle rightangled at P. What is the area of  $\triangle APB$ ?



- $4 \text{ cm}^2$
- $8 \text{ cm}^2$
- $2\sqrt{2}$  cm<sup>2</sup> C.
- $4\sqrt{2}$  cm<sup>2</sup>
- $8\sqrt{2}$  cm<sup>2</sup>

[SP-CE-MATHS 2-20]

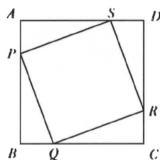
- 21. The length of a side of a rhombus is 10 cm. If its shorter diagonal is of length 12 cm, what is the area of the rhombus in cm<sup>2</sup>?
  - A. 60
  - **B.** 96
  - C. 100
  - **D.** 120
  - E. 192

[1980-CE-MATHS 2-14]

- 22. What is the area, in  $cm^2$ , of an equilateral triangle of side x cm?
  - **A.**  $\frac{\sqrt{3}}{4}x^2$
  - **B.**  $\frac{\sqrt{3}}{2}x^2$
  - C.  $\frac{1}{4}x^2$
  - **D.**  $\frac{1}{2}x^2$
  - $\mathbf{E.} \quad \sqrt{3} \, x^2$

[1980-CE-MATHS 2-20]

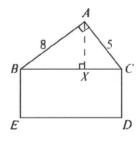
23. In the figure, ABCD is a square with AB = 5. AP = BQ = CR = DS = 1. What is the area of PQRS?



- **A.** 9
- **B.** 15
- **C.** 16
- **D.** 17
- **E.** 18

[1980-CE-MATHS 2-22]

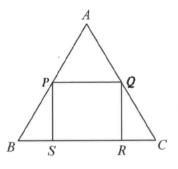
24. In the figure,  $\angle BAC = 90^{\circ}$ , AB = 8, AC = 5 and  $AX \perp BC$ . BCDE is a rectangle with CD = AX. What is the area of the rectangle BCDE?



- A. 20
- **B.** 40
- C. 80
- **D.** 89
- E.  $4\sqrt{89}$

[1981-CE-MATHS 2-40]

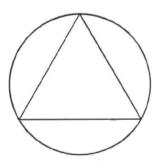
25. In the figure, ABC is an equilateral triangle of side 2a. P and Q are the mid-points of AB and AC respectively. PQRS is a rectangle. What is the area of PQRS?



- A. a
- **B.**  $\frac{1}{2}a^2$
- C.  $\frac{2}{3}a^{2}$
- **D.**  $\frac{1}{\sqrt{3}}a^2$
- E.  $\frac{\sqrt{3}}{2}a^2$

[1981-CE-MATHS 2-50]

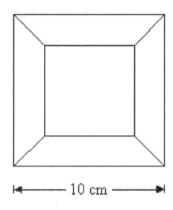
26. In the figure an equilateral triangle is inscribed in a circle of radius *a*. What is the area of the triangle?



- **A.**  $\frac{3}{2}a^2$
- **B.**  $\frac{3\sqrt{3}}{4}a^2$
- C.  $\frac{3}{4}a^2$
- **D.**  $a^2$
- $\mathbf{E.} \quad \frac{3\sqrt{3}}{2}a^{2}$

[1982-CE-MATHS 2-39]

27. Four identical trapeziums, each of area 16 cm<sup>2</sup>, are drawn inside a square of side 10 cm as shown in the figure. What is the height of each trapezium?



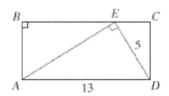
- **A.**  $\frac{1}{2}$  cm.
- B. 1 cm.
- C. 2 cm.
- D. 3 cm.
- E. 4 cm.

[1982-CE-MATHS 2-40]

- 28. If the lengths of the diagonals of a rhombus are 2 cm and 4 cm respectively, what is the area of the rhombus?
  - $\mathbf{A}$ . 2 cm<sup>2</sup>
  - $\mathbf{B.} \quad 4 \text{ cm}^2$
  - C. 8 cm<sup>2</sup>
  - **D.**  $16 \text{ cm}^2$
  - E. It cannot be determined

[1983-CE-MATHS 2-12]

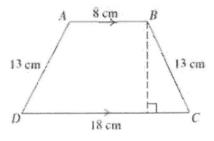
29. In the figure, ABCD is a rectangle. E is a point on BC such that  $\angle AED = 90^{\circ}$ . AD = 13 and DE = 5. The area of ABCD =



- A. 30.
- **B.** 52.
- C. 60.
- **D.** 65.
- E. 120.

[1985-CE-MATHS 2-51]

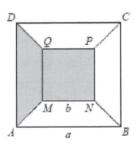
30. ABCD is a trapezium in which AB // DC, AB = 8 cm, DC = 18 cm, AD = BC = 13 cm. Find the area of the trapezium.



- **A.**  $156 \text{ cm}^2$
- **B.** 169 cm<sup>2</sup>
- C. 216 cm<sup>2</sup>
- **D.** 312 cm<sup>2</sup>
- E. 338 cm<sup>2</sup>

[1987-CE-MATHS 2-12]

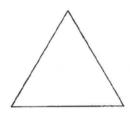
31. In the figure, *ABCD* is a square of side *a* and *MNPQ* is a square of side *b*. The four trapeziums are identical. The area of the shaded region is



- **A.**  $\frac{3b^2 + a^2}{4}$
- **B.**  $\frac{3b^2 a^2}{2}$
- C.  $\frac{5b^2 + a^2}{4}$ .
- **D.**  $\frac{5b^2 a^2}{4}$ .
- $\mathbb{E}. \quad \frac{(a-b)^2}{4} + b^2 \, .$

[1991-CE-MATHS 2-12]

32. An equilateral triangle and a square have equal perimeters.  $\frac{\text{Area of the triangle}}{\text{Area of the square}} =$ 

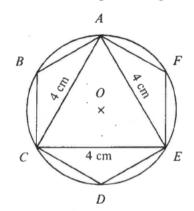




- **A.**  $\frac{9\sqrt{3}}{16}$ .
- **B.**  $\frac{\sqrt{3}}{4}$ .
- C.  $\frac{\sqrt{3}}{3}$ .
- **D.**  $\frac{4\sqrt{3}}{9}$
- E. 1.

[1991-CE-MATHS 2-14]

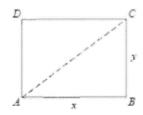
33. In the figure, the equilateral triangle *ACE* of side 4 cm is inscribed in the circle. Find the area of the inscribed regular hexagon *ABCDEF*.



- **A.**  $8\sqrt{3}$  cm<sup>2</sup>
- **B.**  $8\sqrt{2}$  cm<sup>2</sup>
- C.  $4\sqrt{3} \text{ cm}^2$
- **D.**  $4\sqrt{2}$  cm<sup>2</sup>
- **E.** 16 cm<sup>2</sup>

[1992-CE-MATHS 2-16]

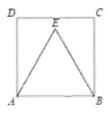
34. In the figure, the rectangle has perimeter 16 cm and area  $15 \text{ cm}^2$ . Find the length of its diagonal AC.



- A.  $\sqrt{32}$  cm
- **B.**  $\sqrt{34}$  cm
- C. 7 cm
- **D.**  $\sqrt{226}$  cm
- E.  $\sqrt{241}$  cm

[1993-CE-MATHS 2-38]

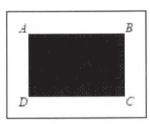
35. In the figure, ABCD is a square and ABE is an equilateral triangle.  $\frac{\text{Area of } ABE}{\text{Area of } ABCD} =$ 



- **A.**  $\frac{1}{4}$ .
- **B.**  $\frac{1}{3}$ .
- **c**.  $\frac{\sqrt{3}}{8}$
- **D.**  $\frac{\sqrt{3}}{4}$
- **E.**  $\frac{\sqrt{3}}{2}$ .

[1993-CE-MATHS 2-41]

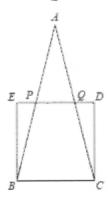
36. In the figure, ABCD is a rectangular field of length p metres and width q metres. The path around the field is of width 2 metres. Find the area of the path.



- **A.**  $(4p + 4q) \text{ m}^2$
- **B.** (2p+2q+4) m<sup>2</sup>
- C.  $(2p + 2q + 16) \text{ m}^2$
- **D.**  $(4p + 4q + 16) \text{ m}^2$ **E.**  $(pq + 4p + 4q + 16) \text{ m}^2$

[1994-CE-MATHS 2-14]

37. In the figure, area of  $\triangle ABC$ : area of square BCDE = 2:1. Find PQ:BC.

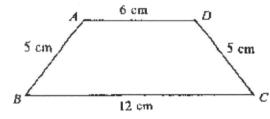


- **A.** 1:2
- **B.** 1:3

- C. 1:4
- **D.** 2:3
- E. 3:4

[1994-CE-MATHS 2-46]

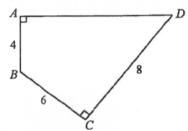
38. In the figure, ABCD is a trapezium. Find its area.



- A.  $36 \text{ cm}^2$
- **B.**  $45 \text{ cm}^2$
- $C. 48 \text{ cm}^2$
- **D.**  $72 \text{ cm}^2$
- **E.**  $90 \text{ cm}^2$

[1995-CE-MATHS 2-14]

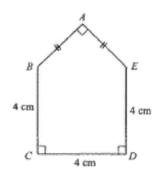
39. In the figure, the area of ABCD is



- A. 36.
- **B.** 40.
- C. 44.
- **D.**  $4\sqrt{21} + 24$
- E.  $4\sqrt{29} + 24$ .

[1996-CE-MATHS 2-17]

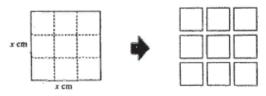
40. In the figure, find the area of the pentagon ABCDE.



- **A.**  $16 \text{ cm}^2$
- **B.**  $18 \text{ cm}^2$
- **C.**  $20 \text{ cm}^2$
- **D.**  $24 \text{ cm}^2$
- **E.**  $32 \text{ cm}^2$

[1998-CE-MATHS 2-21]

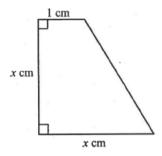
41. In the figure, a square of side x cm is cut into 9 equal squares. If the total perimeter of the 9 small squares is 72 cm more than the perimeter of the original square, then x =



- A. 6.
- **B.** 8.
- C. 9.
- **D.** 12.
- E. 18.

[2000-CE-MATHS 2-7]

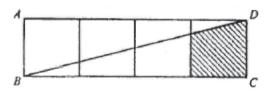
42. The figure shows a trapezium of area 6 cm $^2$ . Find x.



- A. 2
- **B.** 3
- C. 4
- $\mathbf{D}$ .  $\sqrt{6}$
- E . 11

[2000-CE-MATHS 2-8]

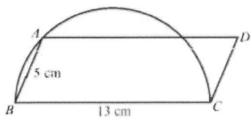
43. In the figure, *ABCD* is a rectangle formed by four squares each of area 1 cm<sup>2</sup>. *DB* is a diagonal. Find the area of the shaded region.



- **A.**  $\frac{9}{10}$  cm<sup>2</sup>
- **B.**  $\frac{7}{8}$  cm<sup>2</sup>
- C.  $\frac{5}{6}$  cm<sup>2</sup>
- **D.**  $\frac{4}{5}$  cm<sup>2</sup>
- E.  $\frac{3}{4}$  cm<sup>2</sup>

[2000-CE-MATHS 2-12]

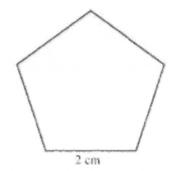
44. In the figure, *CAB* is a semicircle and *ABCD* is a parallelogram. Find the area of *ABCD*.



- **A.**  $65 \text{ cm}^2$
- **B.**  $60 \text{ cm}^2$
- C. 52 cm<sup>2</sup>
- **D.**  $32.5 \text{ cm}^2$
- $E. 30 \text{ cm}^2$

[2000-CE-MATHS 2-31]

45. The figure shows a regular pentagon. Find its area correct to the nearest  $0.01~{\rm cm}^2$ .



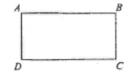
- **A.**  $3.63 \text{ cm}^2$
- **B.**  $5.88 \text{ cm}^2$
- C. 6.18 cm<sup>2</sup>
- **D.**  $6.88 \text{ cm}^2$
- **E.**  $8.51 \text{ cm}^2$

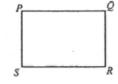
[2001-CE-MATHS 2-9]

- 46. The length of a side of a regular 8-sided polygon is 6 cm. Find its area, correct to 3 significant figures.
  - **A.**  $27.6 \text{ cm}^2$
  - **B.**  $29.8 \text{ cm}^2$
  - C.  $66.5 \text{ cm}^2$
  - **D.**  $174 \text{ cm}^2$

[2003-CE-MATHS 2-16]

47. In the figure, ABCD and PQRS are two rectangles of equal perimeter. If AB:BC=3:2 and PQ:QR=4:3, then area of ABCD:a area of PQRS=a





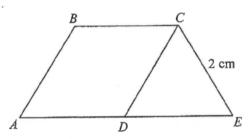
- **A.** 1:1.
- **B.** 1:2.
- C. 25:49.
- **D.** 49:50.

[2003-CE-MATHS 2-44]

- 48. If the area of a regular 10-sided polygon is 123 cm<sup>2</sup>, find the length of the side of the 10-sided polygon. Give the answer correct to the nearest 0.1 cm.
  - **A.** 3.9 cm
  - **B.** 4.0 cm
  - C. 6.8 cm
  - **D.** 8.0 cm

[2004-CE-MATHS 2-19]

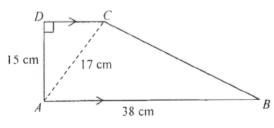
49. In the figure, ABCD is a rhombus and CDE is an equilateral triangle. If ADE is a straight line, then the area of the quadrilateral ABCE is



- **A.**  $2\sqrt{3}$  cm<sup>2</sup>.
- **B.**  $3\sqrt{3}$  cm<sup>2</sup>.
- C.  $4\sqrt{3} \text{ cm}^2$ .
- **D.**  $6\sqrt{3} \text{ cm}^2$ .

[2005-CE-MATHS 2-16]

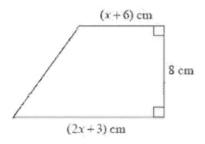
50. In the figure, the area of the trapezium ABCD



- A.  $345 \text{ cm}^2$ .
- **B.**  $349 \text{ cm}^2$ .
- C.  $690 \text{ cm}^2$ .
- **D.**  $698 \text{ cm}^2$ .

[2006-CE-MATHS 2-17]

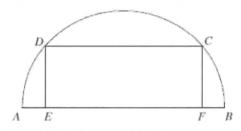
51. In the figure, the area of the trapezium is  $96 \text{ cm}^2$ . Find x.



- A. 1
- B. 5
- C. 7
- **D.** 11

[2009-CE-MATHS 2-7]

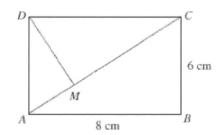
52. In the figure, ABCD is a semicircle of diameter 26 cm. It is given that CDEF is a rectangle such that E and F are points lying on AB. If AE = 1 cm, find the area of the rectangle CDEF.



- **A.**  $120 \text{ cm}^2$
- **B.**  $130 \text{ cm}^2$
- C. 288 cm<sup>2</sup>
- **D.**  $312 \text{ cm}^2$

[2010-CE-MATHS 2-20]

53. In the figure, ABCD is a rectangle. If M is a point lying on AC such that DM is perpendicular to AC, then AM:MC =

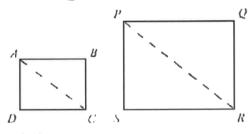


- A. 3:4.
- **B.** 4:3.
- C. 9:16.
- **D.** 16:9.

[2010-CE-MATHS 2-26]

### Areas of Similar Figures

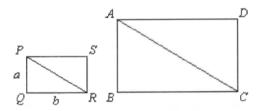
54. In the figure, ABCD and PQRS are similar rectangles, each representing a television screen. If AC is 40 cm and PR is 60 cm, what is the ratio of the areas of the rectangles ABCD and PQRS?



- **A.** 2:3
- **B.** 3:4
- C. 4:9
- **D.** 9:16
- E. It cannot be found from the information given.

[1979-CE-MATHS 2-43]

55. In the figure, the rectangles are similar. PQ = a, QR = b. If AC = 2PR, what is the area of ABCD?

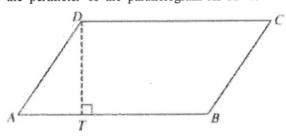


- A. 2ab
- **B.** 4*ab*
- C.  $2(a^2 + b^2)$
- **D.**  $2(a+b)\sqrt{a^2+b^2}$
- E.  $2ab\sqrt{a^2+b^2}$

[1982-CE-MATHS 2-43]

### **HKDSE Problems**

56. In the figure, ABCD is a parallelogram. T is a point lying on AB such that DT is perpendicular to AB. It is given that CD = 9 cm and AT : TB = 1 : 2. If the area of the parallelogram ABCD is  $36 \text{ cm}^2$ , then the perimeter of the parallelogram ABCD is

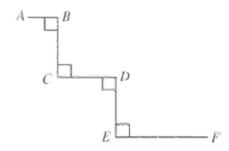


- **B.** 28 cm.
- C. 30 cm.
- **D.** 32 cm.

[SP-DSE-MATHS 2-18]

**UNIT 9.1** 

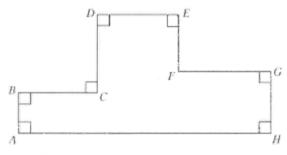
57. In the figure, AB = 1 cm, BC = CD = DE = 2 cm and EF = 3 cm. Find the distance between A and F correct to the nearest 0.1 cm.



- A. 7.2 cm
- **B.** 7.4 cm
- C. 8.0 cm
- **D.** 8.1 cm

[SP-DSE-MATHS 2-20]

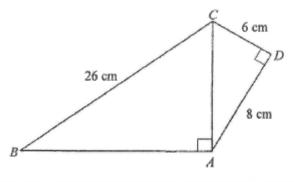
58. In the figure, AB = 4 cm, BC = CD = DE = 8 cm and FG = 9 cm. Find the perimeter of  $\triangle AEH$ .



- **A.** 60 cm
- **B.** 74 cm
- C. 150 cm
- **D.** 164 cm

[PP-DSE-MATHS 2-18]

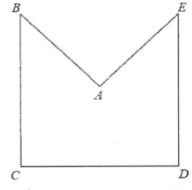
59. In the figure, the area of quadrilateral ABCD is



- A.  $144 \text{ cm}^2$ .
- **B.**  $160 \text{ cm}^2$ .
- C.  $178 \text{ cm}^2$ .
- **D.**  $288 \text{ cm}^2$ .

[2012-DSE-MATHS 2-15]

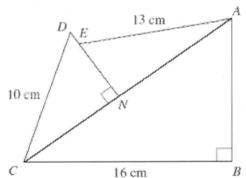
60. In the figure, AB = AE and  $\angle BAE = \angle BCD = \angle CDE = 90^{\circ}$ . If BC = CD = DE = 16 cm, then the area of the pentagon ABCDE is



- **A.**  $71 \text{ cm}^2$ .
- **B.**  $128 \text{ cm}^2$
- C.  $192 \text{ cm}^2$ .
- **D.**  $224 \text{ cm}^2$ .

[2014-DSE-MATHS 2-15]

61. In the figure, N is a point lying on AC and E is a point lying on DN. If DN = 6 cm and EN = 5 cm, then the area of  $\triangle ABC$  is



- **A.**  $24 \text{ cm}^2$ .
- **B.**  $30 \text{ cm}^2$ .
- $C. 96 \text{ cm}^2$
- **D.**  $192 \text{ cm}^2$ .

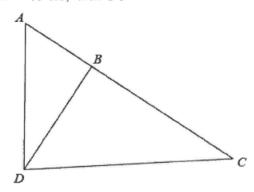
[2015-DSE-MATHS 2-15]

- 62. The diameters AC and BD of the circle ABCD intersect at the point E. If  $\angle AEB = 90^{\circ}$  and AC = 24 cm, then the area of  $\triangle AEB$  is
  - **A.**  $41 \text{ cm}^2$ .
  - **B.**  $72 \text{ cm}^2$
  - C.  $144 \text{ cm}^2$ .
  - **D.**  $288 \text{ cm}^2$ .

[2015-DSE-MATHS 2-21]

63. In the figure, ABC is a straight line. If AB = 24 cm, AD = 40 cm, BD = 32 cm and CD = 68 cm, then BC =

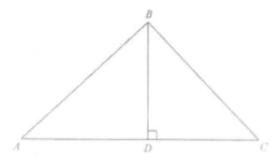
UNIT 9.1



- A. 43 cm.
- **B.** 54 cm.
- C. 55 cm.
- **D.** 60 cm.

[2016-DSE-MATHS 2-16]

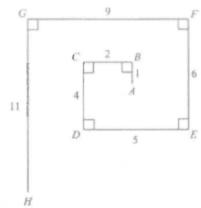
64. In the figure, D is a point lying on AC such that BD is perpendicular to AC. It is given that AC = 14 cm and BD = 12 cm. If the area of  $\Delta ABD$  is greater than the area of  $\Delta BCD$  by 24 cm<sup>2</sup>, then the perimeter of  $\Delta ABC$  is



- A. 30 cm.
- **B.** 42 cm.
- C. 54 cm.
- D. 84 cm.

[2017-DSE-MATHS 2-14]

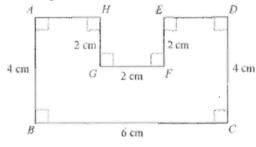
65. In the figure, the length of the line segment joining A and H is



- **A.** 6.
- **B.** 8.
- C. 9.
- **D.** 10.

[2017-DSE-MATHS 2-19]

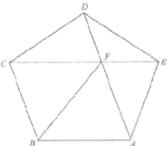
66. In the figure, ABCDEFGH is an octagon, where all the measurements are correct to the nearest cm. Let  $x \ cm^2$  be the actual area of the octagon. Find the range of values of x.



- A. 13 < x < 23
- **B.** 13 < x < 27
- C. 17 < x < 23
- **D**. 17 < x < 27

[2018-DSE-MATHS 2-14]

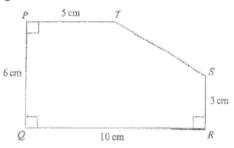
67. In the figure, ABCDE is a regular pentagon. AD and CE intersect at the point F. Which of the following are true?



- I. CD = CF
- II.  $\triangle ABF \cong \triangle CBF$
- III.  $\angle AFB + \angle EAF = 90^{\circ}$
- A. I and II only
- B. I and III only
- C. II and III only
- D. I. II and III

[2019-DSE-MATHS 2-19]

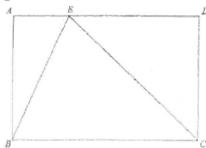
68. In the figure, PQRST is a pentagon, where all measurements are correct to the nearest cm. Let  $A cm^2$  be the actual area of the pentagon. Find the range of values of A.



- A.  $27.83 \le A < 31.83$
- **B.**  $44.75 \le A < 60.75$
- C.  $46.75 \le A < 63.25$
- **D.**  $48.25 \le A < 64.75$

[2020-DSE-MATHS 2-14]

69. In the figure, ABCD is a rectangle. Let E be a point lying on AD such that BE = 8 cm and CE = 15 cm. If BC = 17 cm, find the area of the rectangle ABCD.



- A.  $60 cm^2$
- **B.**  $68 cm^2$
- C.  $120 cm^2$
- **D.**  $136 cm^2$

[2020-DSE-MATHS 2-21]

### Definition of $\pi$

- 1.  $\pi$  is defined as
  - A. <u>circumference of a circle</u> diameter of the circle
  - B.  $\frac{\text{area of a circle}}{\text{radius of the circle}}$
  - C.  $\frac{22}{7}$
  - **D.** 3.142.
  - E. 3.1416.

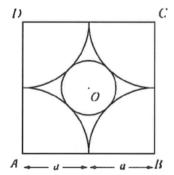
[1979-CE-MATHS 2-38]

- 2. The real number  $\pi$  is
  - **A.**  $\frac{22}{7}$ .
  - **B.** 3.1416.
  - C. the ratio of the area of a circle to the square of its diameter.
  - D. the ratio of the circumference of a circle to its radius.
  - E. the ratio of the circumference of a circle to its diameter.

[1987-CE-MATHS 2-22]

### Lengths in Circles

3. In the figure, ABCD is a square of side 2a. Four quadrants of radius a arc drawn with A, B, C and D as centres. If the circle with centre O touches all the four quadrants, what is the diameter of the circle O?



- **A.** *a*
- **B.**  $\sqrt{2a}$
- C.  $2\sqrt{2a}$
- **D.**  $2(\pi \sqrt{2})a$
- **E.**  $2(\sqrt{2}-1)a$

[1979-CE-MATHS 2-46]

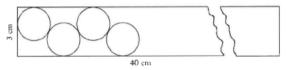
4. In the figure, an equilateral triangle is inscribed in a circle of radius 1. The circumference of the circle is greater than the perimeter of the triangle by



- **A.**  $4\pi 3\sqrt{3}$ .
- **B.**  $4\pi \frac{3\sqrt{3}}{2}$ .
- C.  $2\pi \sqrt{3}$ .
- **D.**  $2\pi \frac{3\sqrt{3}}{2}$ .
- E.  $2\pi 3\sqrt{3}$ .

[1990-CE-MATHS 2-40]

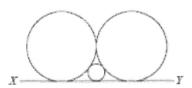
5. From a rectangular metal sheet of width 3 cm and length 40 cm, at most how many circles each of radius 1 cm can be cut?



- A. 20
- **B.** 21
- C. 22
- **D.** 23
- E. 24

[1991-CE-MATHS 2-44]

6. In the figure, the three circles touch one another. XY is their common tangent. The two larger circles are equal. If the radius of the smaller circle is 4 cm, find the radii of the larger circles.



- A. 8 cm
- **B.** 10 cm
- C. 12 cm
- **D.** 14 cm
- E. 16 cm

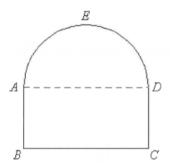
[1993-CE-MATHS 2-54]

## Areas of Circles

- 7. The area of a circle is  $A ext{ cm}^2$ . Its circumference is  $s ext{ cm}$ . Express  $s ext{ in terms of } A$ .
  - $\mathbf{A.} \quad s = 2\sqrt{\pi A}$
  - **B.**  $s = 2\pi\sqrt{A}$
  - C.  $s = \sqrt{2\pi A}$
  - $\mathbf{D.} \quad s = \sqrt{\frac{A}{\pi}}$
  - $\mathbf{E.} \quad s = \sqrt{\frac{2A}{\pi}}$

[1978-CE-MATHS 2-39]

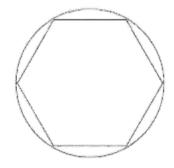
8. The perimeter of the given figure ABCDE is  $2(\pi + 4)$  cm. The upper portion AED is a semi-circle and the lower portion ABCD is a rectangle. AB:BC=1:2. What is the area of the given figure?



- $\mathbf{A}$ . 8 cm<sup>2</sup>
- **B.**  $2\pi \text{ cm}^2$
- C.  $4\pi$  cm<sup>2</sup>
- **D.**  $4(\pi + 2)$  cm<sup>2</sup>
- E.  $2(\pi + 4)$  cm<sup>2</sup>

[1982-CE-MATHS 2-41]

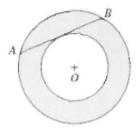
9. In the figure, a regular hexagon of side 2 cm is inscribed in a circle. The area of the circle is greater than the area of the hexagon by



- **A.**  $(3\pi 6)$  cm<sup>2</sup>
- **B.**  $(3\pi 3\sqrt{3})$  cm<sup>2</sup>
- C.  $(4\pi 6)$  cm<sup>2</sup>
- **D.**  $(4\pi 3\sqrt{3})$  cm<sup>2</sup>
- E.  $(4\pi 6\sqrt{3})$  cm<sup>2</sup>

[1985-CE-MATHS 2-16]

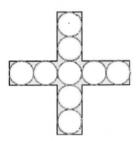
10. In the figure, O is the centre of two concentric circles. AB is tangent to the smaller circle. If AB = 2, find the area of the shaded part.



- A.  $\frac{\pi}{2}$
- B.  $\pi$
- C.  $2\pi$
- **D.**  $4\pi$
- E. It cannot be found.

[1989-CE-MATHS 2-33]

11. In the figure, there are nine circles, each of radius 1. Find the shaded area.



- **A.**  $9 9\pi$
- **B.**  $36 9\pi$
- **C.**  $40 9\pi$
- **D.**  $10 10\pi$
- E.  $40 10\pi$

[1990-CE-MATHS 2-13]

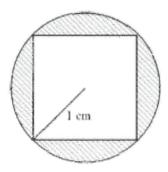
12. Three equal circles of radii 1 touch each other as shown in the figure, shaded area =



- **A.**  $1 \frac{\pi}{2}$ .
- **B.**  $\sqrt{3} \frac{\pi}{2}$ .
- C.  $2\sqrt{3} \frac{\pi}{2}$
- **D.**  $\sqrt{3} \frac{\pi}{6}$ .
- **E.**  $2\sqrt{3} \frac{\pi}{6}$ .

[1990-CE-MATHS 2-41]

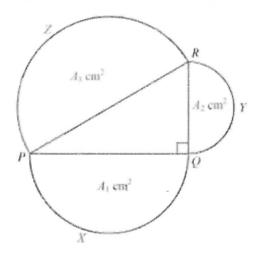
13. In the figure, a square is inscribed in a circle with radius 1 cm. Find the area of the shaded region.



- A.  $(\pi 2)$  cm<sup>2</sup>
- **B.**  $(\pi \sqrt{2})$  cm<sup>2</sup>
- C.  $(\pi 1)$  cm<sup>2</sup>
- **D.**  $(2\pi 2)$  cm<sup>2</sup>
- E.  $(2\pi 1)$  cm<sup>2</sup>

[1999-CE-MATHS 2-21]

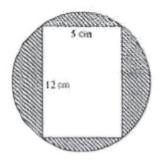
14. In the figure, PXQ, QYR and RZP are semicircles with areas  $A_1$  cm<sup>2</sup>,  $A_2$  cm<sup>2</sup> and  $A_3$  cm<sup>2</sup> respectively. If  $A_1$  = 12 and  $A_2$  = 5, find  $A_3$ .



- A. 13
- **B.** 17
- C. 169
- **D.**  $13\pi$
- E.  $\frac{169}{8}\pi$

[2000-CE-MATHS 2-25]

15. The figure shows a rectangular inscribed in a circle. Find the area of the shaded region correct to the nearest 0.1 cm<sup>2</sup>.

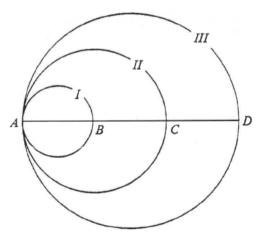


- **A.**  $60.0 \text{ cm}^2$
- **B.**  $72.7 \text{ cm}^2$
- C. 132.7 cm<sup>2</sup>
- **D.**  $470.9 \text{ cm}^2$

[2002-CE-MATHS 2-17]

### Mensuration of Circles in Ratio

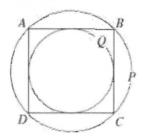
16. In the figure, ABCD is a straight line with AB = BC = CD. Three circles I, II and III are drawn respectively on AB, AC and AD as diameters. Areas of circle I: Area of circle II: Area of circle III =



- A. 1:2:3.
- **B.** 1:2:4.
- **C.** 1:4:9.
- **D.** 1:4:16.
- **E.** 1:8:27.

[1986-CE-MATHS 2-10]

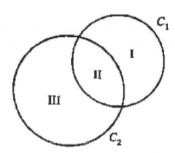
17. The figure shows the circumscribed circle P and the inscribed circle Q of the square ABCD. Find area of P: area of Q.



- **A.**  $\sqrt{2}:1$
- **B.** 2:1
- **C.**  $2\sqrt{2}:1$
- **D.**  $\pi:1$
- **E.** 4:1

[1988-CE-MATHS 2-46]

18. In the figure,  $C_1$  and  $C_2$  are two circles. If area of region II: area of region III = 2:1:3, then radius of  $C_1$ : radius  $C_2$  =



- A. 9:16.
- **B.** 2:3.
- C. 3:4.
- **D.**  $\sqrt{2}:\sqrt{3}$ .
- $\mathbf{E} = \sqrt{3} \cdot 2$

[1995-CE-MATHS 2-46]

19. In the figure, the radii of the two circles are 3 cm and 1 cm respectively. Find the ratio of the area of the shaded part to that of the smaller circle.

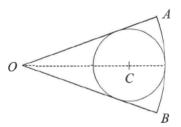


- **A.** 2:1
- **B.** 3:1
- **C.** 4:1
- **D.** 8:1
- **E.** 9:1

[1998-CE-MATHS 2-19]

### Mensuration of Sectors

20. In the figure, a circle, centre C, of radius 1 cm is inscribed in a sector AOB of radius 3 cm. The length of arc AB =



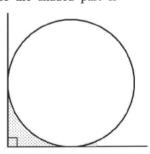
- **A.**  $\frac{1}{2}\pi$  cm.
- **B.**  $\frac{2}{3}\pi$  cm.
- C.  $\frac{3}{4}\pi$  cm.
- **D.**  $\pi$  cm.
- $\mathbf{E.} \quad \frac{3}{2}\pi \ \mathrm{cm} \ .$

[1977-CE-MATHS 2-24]

- 21. The angle of a sector is 2 radians (i.e.  $\frac{360^{\circ}}{\pi}$ ) and its perimeter is 12 cm. The area of the sector is
  - A.  $6 \text{ cm}^2$ .
  - **B.**  $9 \text{ cm}^2$ .
  - **C.**  $16 \text{ cm}^2$
  - **D.**  $18 \text{ cm}^2$ .
  - **E.**  $36 \text{ cm}^2$ .

[1977-CE-MATHS 2-26\*]

22. In the figure, the radius of the circle is r. The area of the shaded part is



- **A.**  $r^2 \frac{\pi}{4}$ .
- **B.**  $r(r-\frac{\pi}{4})$ .
- C.  $r^2(1-\frac{\pi}{4})$ .
- **D.**  $r^2(1-\pi)$ .
- **E.**  $r^2(\pi-1)$ .

[SP-CE-MATHS 2-16]

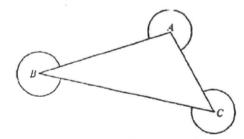
- 23. What is the size of the angle of a circular sector whose area is 5 cm<sup>2</sup> and whose radius is 10 cm?
  - A.  $\frac{9}{\pi}$  degrees
  - B.  $\frac{18}{\pi}$  degrees
  - C.  $\frac{90}{\pi}$  degrees
  - **D.**  $\frac{360}{\pi}$  degrees
  - E.  $\frac{900}{\pi}$  degrees

[SP-CE-MATHS 2-30\*]

- 24. A wire of length b is bent to form the perimeter of a sector of radius r. The angle of the sector in degrees is
  - A.  $\frac{b}{r} \times \frac{180^{\circ}}{\pi}$ .
  - **B.**  $\frac{r}{h-r} \times \frac{180^{\circ}}{\pi}$ .
  - C.  $\frac{r}{h-2r} \times \frac{180^{\circ}}{\pi}$
  - **D.**  $\frac{b-r}{r} \times \frac{180^{\circ}}{\pi}$ .
  - $\mathbb{E}$ .  $\frac{b-2r}{r} \times \frac{180^{\circ}}{\pi}$ .

[1978-CE-MATHS 2-30\*]

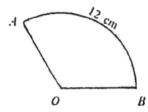
25. In the figure,  $\triangle ABC$  is any triangle. Three circular arcs, with vertices as centres and radii 1 cm. What is the total length of the 3 arcs?



- $6\pi$  cm
- B.  $5\pi$  cm
- C.  $4.5\pi$  cm
- D.  $4\pi$  cm
- It cannot be found from the information given.

[1978-CE-MATHS 2-40]

26. The figure below shows a sector. The length of arc AB is 12 cm. If the area of the sector is 36 cm<sup>2</sup>, then  $\angle AOB =$ 



- A.  $\frac{270}{\pi}$  degrees.
- **B.**  $\frac{360}{\pi}$  degrees.
- C.  $\frac{450}{\pi}$  degrees.
- **D.**  $\frac{720}{\pi}$  degrees.
- $\frac{1080}{\pi}$  degrees.

[1979-CE-MATHS 2-17\*]

- 27. The perimeter of a sector is 16 and its angle degrees. What is the area of the sector?
  - A. 16
  - B. 32
  - C. 64
  - D.  $16\pi$
  - E.  $32\pi$

[1980-CE-MATHS 2-41\*]

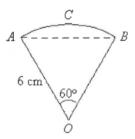
- 28. The radius of a sector is 3 cm and the perimeter is 10 cm. What is the area of the sector?
  - $\mathbf{A}$ . 6 cm<sup>2</sup>
  - **B.**  $12 \text{ cm}^2$
  - C.  $15 \text{ cm}^2$
  - **D.**  $18 \text{ cm}^2$
  - **E.**  $45 \text{ cm}^2$

[1981-CE-MATHS 2-46]

- 29. In a circle, the angle of a sector is 30° and the radius is 2 cm. The area of the sector is
  - **A.**  $120 \text{ cm}^2$ .
  - **B.**  $60 \text{ cm}^2$ .
  - C.  $\frac{30}{\pi}$  cm<sup>2</sup>.
  - **D.**  $\frac{2\pi}{3}$  cm<sup>2</sup>.
  - $\mathbb{E}$ .  $\frac{\pi}{3}$  cm<sup>2</sup>.

[1982-CE-MATHS 2-22]

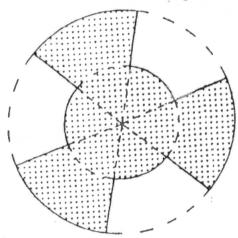
30. In the figure, OACB is a sector of a circle of radius 6 cm. Arc ACB is longer than the chord AB by



- **A.**  $(\pi 3)$  cm
- **B.**  $2(\pi 3)$  cm
- C.  $3(\pi 1)$  cm
- **D.**  $6(\pi 1)$  cm
- **E.**  $3(2\pi \sqrt{3})$  cm

[1982-CE-MATHS 2-23]

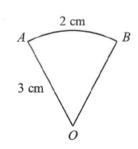
31. In the figure, the two concentric circles are of radius 2 cm and 4 cm respectively. Each circle is divided into 6 equal parts by 6 radii. What is the area of the shaded region?



- **A.**  $12\pi \text{ cm}^2$
- **B.**  $10\pi \text{ cm}^2$
- C.  $9\pi$  cm<sup>2</sup>
- **D.**  $6\pi$  cm<sup>2</sup>
- E.  $2\pi$  cm<sup>2</sup>

[1982-CE-MATHS 2-42]

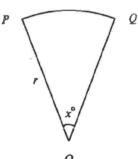
32. In the figure, OAB is a sector of a circle. Radius OA is 3 cm long and arc AB = 2 cm. The area of the sector is



- A.  $3 \text{ cm}^2$ .
- **B.**  $6 \text{ cm}^2$ .
- $\mathbf{C}$ . 9 cm<sup>2</sup>.
- **D.**  $3\pi$  cm<sup>2</sup>.
- E.  $6\pi$  cm<sup>2</sup>.

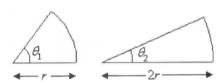
[1983-CE-MATHS 2-20]

- 33. In the figure, the radius of the sector is r and  $\angle POQ = x^{\circ}$ . If the area of the sector is A, then x =
  - A.  $\frac{2A}{r^2}$
  - **B.**  $\frac{360A}{r^2}$
  - C.  $\frac{360A}{\pi r^2}$
  - **D.**  $\frac{180A}{r^2}$ .
  - E.  $\frac{180A}{\pi r^2}$ .



[1984-CE-MATHS 2-47]

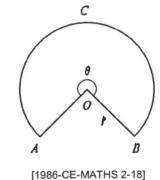
34. The figure shows two sectors with radii r and 2r. If these two sectors are equal in area, then  $\theta_1:\theta_2=$ 



- A. 2:1.
- **B.** 3:1.
- C. 4:1.
- **D.** 5:1.
- **E.** 6:1.

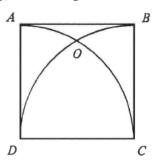
[1986-CE-MATHS 2-9]

- 35. In the figure, if the area of the sector is x, then  $\widehat{ACB} =$ 
  - A.  $\frac{2x}{r}$ .
  - **B.**  $\frac{x}{r}$ .
  - C.  $\frac{2x}{x^2}$ .
  - **D.**  $\frac{\pi x}{90r}$ .
  - E.  $\frac{90x}{\pi r}$



Past Paper Review (Multiple Choice)

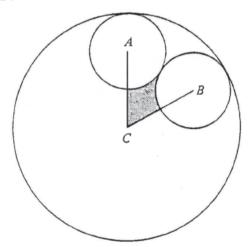
36. In the figure, ABCD is a square. Arcs AC and BD are drawn with centres D and C respectively, intersecting at O.  $\widehat{AO}$ :  $\widehat{OC}$  =



- **A.**  $1:\sqrt{2}$ .
- **B.**  $1:\sqrt{3}$ .
- C. 1:2.
- **D.** 1:3.
- E. 2:3.

[1986-CE-MATHS 2-47]

37. Three circles, centres A, B and C touch each other as shown in the figure. The radii of the two circles with centre A and B are both 1 cm and radius of the circle with centre C is 3 cm. Find the area of the shaded part in cm<sup>2</sup>.



- **A.**  $\sqrt{3} \frac{\pi}{3}$
- **B.**  $\sqrt{3} \frac{\pi}{6}$
- C.  $2\sqrt{3} \frac{\pi}{3}$
- **D.**  $2\sqrt{3} \frac{\pi}{6}$
- E. It cannot be determined.

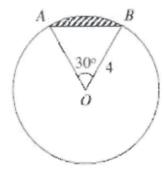
[1986-CE-MATHS 2-52]

38. The circumference of a circle is  $6\pi$  cm. The length of an arc of the circle which subtends an angle of  $\frac{60}{\pi}$  degrees at the centre is

- 1 cm.
- $\frac{3}{2}$  cm.
- 2 cm.
- $\pi$  cm.
- $2\pi$  cm.

[1987-CE-MATHS 2-17\*]

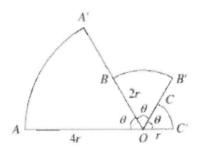
39. In the figure, O is the centre of the circle of radius 4. The area of the shaded region is



- **A.**  $\frac{4\pi}{3} 4$ .
- **B.**  $\frac{4\pi}{3} 8$ .
- C.  $\frac{4\pi}{3} 4\sqrt{3}$ .
- **D.**  $\frac{2\pi}{3} 4$ .
- E.  $\frac{8\pi}{3} 8$ .

[1987-CE-MATHS 2-52]

40. In the figure, AOC' is a straight line. OAA', OBB' and OCC' are 3 sectors. If OA = 4r, OB = 2r and OC' = r, find the total area of the sectors in terms of r.

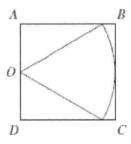


- **A.**  $7\pi r^2$  **B.**  $\frac{7}{2}\pi r^2$

- E.  $\frac{7}{12}\pi r^2$

[1988-CE-MATHS 2-18]

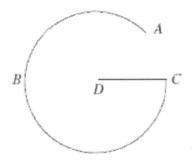
41. ABCD is a square of side 2 cm. O is the mid-point of AD. A sector with centre O is inscribed in the square as shown in the figure. What is the area of the sector?



- A.  $\frac{\pi}{2}$  cm<sup>2</sup>
- **B.**  $2\sqrt{3}\pi \text{ cm}^2$
- C.  $\sqrt{3}\pi$  cm<sup>2</sup>
- **D.**  $\frac{2}{3}\pi \text{ cm}^2$
- E.  $\frac{4}{3}\pi \text{ cm}^2$

[1988-CE-MATHS 2-49]

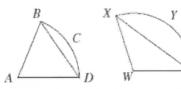
42. In the figure, ABCD is a G-shaped curve, where ABC is an arc of a circle and DC is a radius. If the length of the curve ABCD is the same as that of the complete circle, find the angle subtended by the arc ABC at the centre.



- **A.** 270°
- **B.**  $(180 + \frac{180}{\pi})^{\circ}$
- C. 240°
- **D.**  $(360 \frac{180}{\pi})^{\circ}$
- E. 315°

[1988-CE-MATHS 2-50\*]

43.



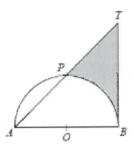
In the figure, ABCD and WXYZ are sectors of equal radii. If  $\widehat{BCD}:\widehat{XYZ}=s:t$ , then which of the following is/are true?

$$(1) \quad \frac{BD}{XZ} = \frac{s}{t}$$

- (2)  $\frac{\text{area of sector } ABCD}{\text{area of sector } WXYZ} = \frac{s}{t}$
- $(3) \quad \frac{\angle BAD}{\angle XWZ} = \frac{s}{t}$
- **A.** (1) only
- **B.** (2) only
- C. (3) only
- **D.** (1) and (3) only
- E. (2) and (3) only

[1989-CE-MATHS 2-32]

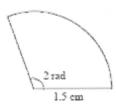
44. In the figure, TB touches the semi-circle at B. TA cuts the semi-circle at P such that TP = PA. If the radius of the semi-circle is 2, find the area of the shaded region.



- **A.**  $12 \pi$
- **B.**  $8 \pi$
- C.  $6 \pi$
- **D.**  $4 \pi$
- E.  $2(4-\pi)$

[1991-CE-MATHS 2-13]

45. Find the perimeter of the sector in the figure.  $(\pi \text{ rad} = 180^{\circ})$ 



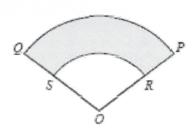
- A. 2.25 cm
- **B.** 3 cm
- C.  $\left(\frac{\pi}{60} + 3\right)$  cm
- **D.** 4.5 cm
- E. 6 cm

[1993-CE-MATHS 2-15]

46. In the figure, the radii of the sectors *OPQ* and *ORS* are 5 cm and 3 cm respectively,

Area of shaded region

Area of sector *OPQ* 



- A.  $\frac{4}{25}$ .

  B.  $\frac{2}{5}$ .

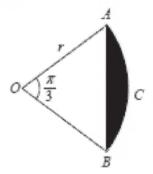
  C.  $\frac{9}{25}$ .

  D.  $\frac{16}{25}$ .

  E.  $\frac{21}{25}$ .

[1993-CE-MATHS 2-42]

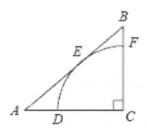
47. In the figure, OACB is a sector of radius r. If  $\angle AOB = \frac{\pi}{3}$  (i.e. 60°), find the area of the shaded part.



- $\mathbf{A.} \quad \left(\frac{\pi}{6} \frac{\sqrt{3}}{4}\right) r^2$
- **B.**  $\left(\frac{\pi}{6} \frac{1}{4}\right)r^2$
- C.  $\left(\frac{\pi}{3} \frac{\sqrt{3}}{2}\right)r^2$
- **D.**  $\left(\frac{\pi}{3} \frac{1}{2}\right)r^2$
- E.  $\frac{\pi}{3}r \frac{\sqrt{3}}{4}r^2$

[1994-CE-MATHS 2-15]

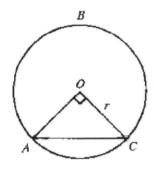
48. In the figure, CDEF is a sector of a circle which touched AB at E. If AB = 25 and BC = 15, find the radius of the sector.



- 9 A.
- 10 В.
- C. 11.25
- D. 12
- Ε. 12.5

[1994-CE-MATHS 2-44]

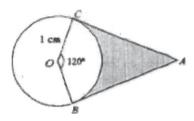
49. In the figure, O is the centre of the circle. Find the area of the major segment ABC.



- **B.**  $\frac{3\pi}{4}r^2$
- C.  $\left(\frac{\pi}{4} \frac{1}{2}\right)r^2$
- **D.**  $\left(\frac{3\pi}{4} \frac{1}{2}\right)r^2$
- $\mathbf{E.} \quad \left(\frac{3\pi}{4} + \frac{1}{2}\right)r^2$

[1995-CE-MATHS 2-45]

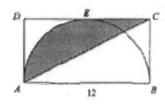
50. In the figure, O is the centre of the circle. AB and AC are tangents to the circle at B and C respectively. Area of the shaded region =



- **A.**  $(2 \frac{\pi}{6})$  cm<sup>2</sup>.
- **B.**  $(2-\frac{\pi}{3})$  cm<sup>2</sup>.
- C.  $(\sqrt{3} \frac{\pi}{6}) \text{ cm}^2$ .
- **D.**  $(\sqrt{3} \frac{\pi}{3})$  cm<sup>2</sup>.
- E.  $(\frac{\sqrt{3}}{2} \frac{\pi}{6})$  cm<sup>2</sup>.

[1996-CE-MATHS 2-16]

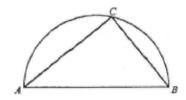
51. In the figure, *BEA* is a semicircle. *ABCD* is a rectangle and *DC* touches the semicircle at *E*. Find the area of the shaded region.



- A.  $9\pi$
- **B.**  $18\pi$
- C.  $36\pi$
- **D.**  $36 9\pi$
- E.  $36 + 9\pi$

[1997-CE-MATHS 2-16]

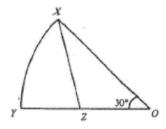
52. In the figure, BCA is a semicircle. If AC = 6 and CB = 4, find the area of the semicircle.



- **A.**  $\frac{5}{2}\pi$
- **B.**  $\frac{13}{2}\pi$
- $\mathbb{C}$ .  $10\pi$
- **D.**  $13\pi$
- E.  $26\pi$

[1997-CE-MATHS 2-18]

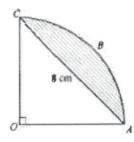
53. In the figure, OXY is a sector with centre O. If Z is the mid-point of YO, find area of  $\Delta OXZ$ : area of sector OXY.



- **A.** 1:2
- **B.**  $2:\sqrt{3}\pi$
- **C.**  $2:3\pi$
- **D.**  $3:2\pi$
- **E.**  $3\sqrt{3}:2\pi$

[1997-CE-MATHS 2-48]

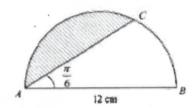
54. In the figure, *OABC* is a sector. Find the area of the shaded region.



- **A.**  $(\pi 2)$  cm<sup>2</sup>
- **B.**  $(2\pi 4)$  cm<sup>2</sup>
- C.  $(4\pi 8)$  cm<sup>2</sup>
- **D.**  $(8\pi 8)$  cm<sup>2</sup>
- E.  $(8\pi 16)$  cm<sup>2</sup>

[1998-CE-MATHS 2-23]

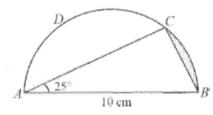
55. In the figure, ABC is a semicircle. Find the area of the shaded part.



- A.  $6\pi$  cm<sup>2</sup>
- **B.**  $15\pi \text{ cm}^2$
- C.  $(6\pi 9\sqrt{3})$  cm<sup>2</sup>
- **D.**  $(6\pi + 9\sqrt{3})$  cm<sup>2</sup>
- E.  $(12\pi 9\sqrt{3})$  cm<sup>2</sup>

[1998-CE-MATHS 2-46]

56. In the figure, ABCD is a semicircle. Find the area of the shaded region correct to the nearest  $0.01 \text{ cm}^2$ .

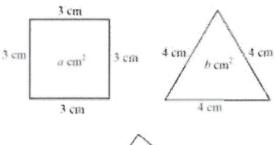


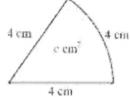
- **A.**  $5.33 \text{ cm}^2$
- **B.**  $2.87 \text{ cm}^2$
- $C. 2.67 \text{ cm}^2$
- **D.**  $1.33 \text{ cm}^2$
- **E.**  $0.17 \text{ cm}^2$

[1999-CE-MATHS 2-25]

57. The figure shows a square, a triangle and a sector with areas  $a \text{ cm}^2$ ,  $b \text{ cm}^2$  and  $c \text{ cm}^2$  respectively.

**UNIT 9.2** 



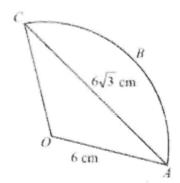


Which of the following is true?

- A. a > b > c
- **B.** a > c > b
- **C.** b > a > c
- **D.** b > c > a
- **E.** c > a > b

[2000-CE-MATHS 2-32]

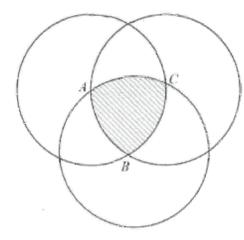
58. In the figure, *OABC* is a sector. Find the length of the arc *ABC*.



- A.  $\frac{2\pi}{3}$  cm
- **B.**  $4\pi$  cm
- C.  $5\pi$  cm
- D.  $6\pi$  cm
- E.  $12\pi$  cm

[2001-CE-MATHS 2-25]

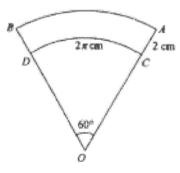
59. In the figure, A, B and C are the centres of three equal circles, each of radius 1 cm. Find the area of the shaded region.



- $\mathbf{A.} \quad \left(\frac{\pi}{2} \frac{\sqrt{3}}{2}\right) \text{ cm}^2$
- **B.**  $\left(\frac{\pi}{2} \frac{3\sqrt{3}}{4}\right) \text{ cm}^2$
- C.  $\left(\frac{\pi}{2} + \frac{\sqrt{3}}{4}\right)$  cm<sup>2</sup>
- **D.**  $\frac{\pi}{2}$  cm<sup>2</sup>
- $E. \quad \left(\frac{\pi}{2} \frac{\sqrt{3}}{4}\right) \text{ cm}^2$

[2001-CE-MATHS 2-26]

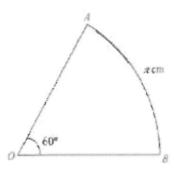
60. In the figure, OCD and OAB are two sectors. The length of  $\widehat{AB}$  is



- **A.**  $\frac{8}{3}\pi$  cm
- **B.**  $\frac{10}{3}\pi$  cm
- C.  $(2\pi + 2)$  cm
- **D.**  $4\pi$  cm

[2002-CE-MATHS 2-20]

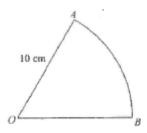
61. In the figure, OAB is a sector and  $\widehat{AB} = \pi$  cm. Find the area of the sector.



- **A.**  $\frac{3}{2}\pi$  cm<sup>2</sup>
- **B.**  $3\pi \text{ cm}^2$
- C.  $\frac{9}{2}\pi \text{ cm}^2$
- **D.**  $6\pi \text{ cm}^2$

[2003-CE-MATHS 2-19]

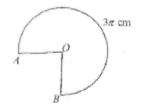
62. In the figure, OAB is a sector. The perimeter and the area of the sector are x cm and y cm<sup>2</sup> respectively. If x = y, then  $\widehat{AB} =$ 



- **A.** 5 cm
- **B.** 10 cm
- C.  $\frac{5\pi}{3}$  cm
- **D.**  $\frac{10\pi}{3}$  cm

[2004-CE-MATHS 2-45]

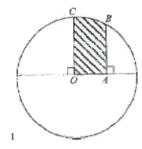
63. In the figure, OAB is a sector of radius 2 cm. If the length of  $\widehat{AB}$  is  $3\pi$  cm, then the area of the sector OAB is



- **A.**  $\frac{3\pi}{2}$  cm<sup>2</sup>.
- **B.**  $3\pi \text{ cm}^2$ .
- C.  $4\pi$  cm<sup>2</sup>.
- **D.**  $6\pi$  cm<sup>2</sup>.

[2005-CE-MATHS 2-19]

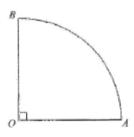
64. In the figure, O is the centre of the circle. B and C are points lying on the circle. If OC = 2 cm and OA = 1 cm, then the area of the shaded region OABC is



- **A.**  $\frac{\pi}{2}$  cm<sup>2</sup>.
- **B.**  $\frac{2\pi}{3}$  cm<sup>2</sup>.
- $\mathbf{C.} \quad \left(\frac{\sqrt{3}}{2} + \frac{\pi}{3}\right) \, \mathbf{cm}^2 \, .$
- $\mathbf{D.} \quad \left(\sqrt{3} + \frac{2\pi}{3}\right) \, \mathrm{cm}^2 \, .$

[2006-CE-MATHS 2-19]

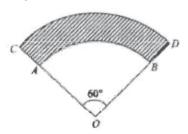
65. In the figure, OAB is a sector with centre O. If the perimeter of the sector OAB is 12 cm, find OA correct to the nearest 0.01 cm.



- A. 3.36 cm
- **B.** 3.91 cm
- C. 4.31 cm
- **D.** 7.64 cm

[2007-CE-MATHS 2-16]

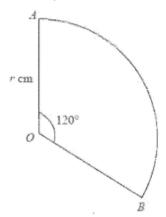
66. In the figure, OAB and OCD are sectors with centre O. It is given that the area of the shaded region ABCD is  $54\pi$  cm<sup>2</sup>. If AC = 6 cm, then OA =



- A. 15 cm.
- B. 21 cm.
- C. 24 cm.
- D. 30 cm.

[2008-CE-MATHS 2-20]

67. In the figure, OAB is a sector of radius r cm. If  $\angle AOB = 120^{\circ}$  and the area of the sector is  $12\pi$  cm<sup>2</sup>, then r =



- A. 3.
- В.
- C. 6.
- D. 18.

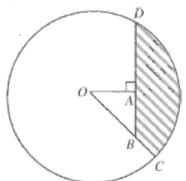
[2009-CE-MATHS 2-20]

- 68. If the radius and the area of a sector are 12 cm and  $48\pi$  cm<sup>2</sup> respectively, find the perimeter of the sector correct to the nearest 0.1 cm.
  - 25.1 cm. A.
  - В. 36.6 cm.
  - C. 49.1 cm.
  - D. 99.4 cm.

[2011-CE-MATHS 2-16]

## **HKDSE Problems**

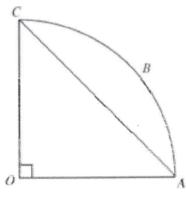
69. In the figure, O is the centre of the circle. Cand D are points lying on the circle. OBCand BAD are straight lines. If OC = 20 cm and OA = AB = 10 cm, find the area of the shaded region BCD correct to the nearest cm<sup>2</sup>.



- $214 \text{ cm}^2$
- $230 \text{ cm}^2$ В.
- $246 \text{ cm}^2$ C.
- $270 \text{ cm}^2$

[SP-DSE-MATHS 2-16]

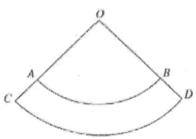
70. In the figure, O is the centre of the sector *OABC*. If the area of  $\triangle OAC$  is 12 cm<sup>2</sup>, find the area of the segment ABC.



- **A.**  $3(\pi 2)$  cm<sup>2</sup>
- **B.**  $3(\pi 1)$  cm<sup>2</sup>
- C.  $6(\pi 2)$  cm<sup>2</sup>
- **D.**  $6(\pi 1)$  cm<sup>2</sup>

[PP-DSE-MATHS 2-15]

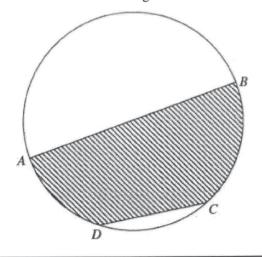
71. In the figure, OAB and OCD are sectors with centre O. If  $\overrightarrow{AB} = 12\pi$  cm,  $\overrightarrow{CD} = 16\pi$  cm and OA = 30 cm, then AC =



- 5 cm.
- 10 cm.
- C. 20 cm.
- D. 40 cm.

[2012-DSE-MATHS 2-16]

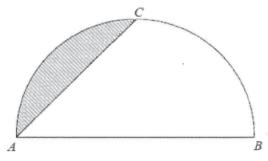
72. In the figure, AB is a diameter of the circle ABCD. If AB = 12 cm and CD = 6 cm, then the area of the shaded region is



- A.  $(12\pi 9)$  cm<sup>2</sup>.
- **B.**  $(12\pi + 9)$  cm<sup>2</sup>.
- C.  $(12\pi 9\sqrt{3})$  cm<sup>2</sup>.
- **D.**  $(12\pi + 9\sqrt{3})$  cm<sup>2</sup>.

[2012-DSE-MATHS 2-21]

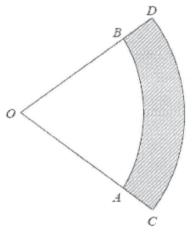
73. In the figure, the diameter of the semicircle ABC is 3 cm. If AC = 2 cm, find the area of the shaded region correct to the nearest  $0.01 \text{ cm}^2$ .



- **A.**  $0.23 \text{ cm}^2$
- **B.**  $0.52 \text{ cm}^2$
- $C. 0.64 \text{ cm}^2$
- **D.**  $1.07 \text{ cm}^2$

[2013-DSE-MATHS 2-16]

74.

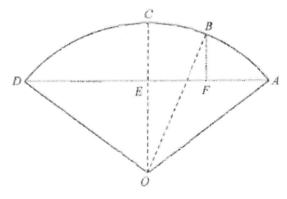


In the figure, OAB and OCD are sectors with centre O, where OA = 33 cm and OC = 39 cm. The area of the shaded region ABDC is  $72\pi$  cm<sup>2</sup>. Which of the following is/are true?

- (1) The angle of the sector OAB is 60°.
- (2) The area of the sector OAB is  $11\pi$  cm<sup>2</sup>.
- (3) The perimeter of the sector OCD is  $13\pi$  cm.
- **A.** (1) only
- **B.** (2) only
- C. (1) and (3) only
- **D.** (2) and (3) only

[2016-DSE-MATHS 2-19]

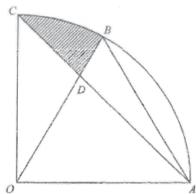
75. In the figure, O is the centre of the sector OABCD. AD and OC are perpendicular to each other and intersects at the point E. F is a point lying on AD such that BF is perpendicular to AD. If AF = 9 cm, DF = 39 cm and OE = 18 cm, then the area of the sector OBC is



- A.  $48\pi \ cm^2$
- B.  $75\pi \ cm^2$
- C.  $96\pi \text{ cm}^2$
- **D.**  $150\pi \ cm^2$

[2018-DSE-MATHS 2-17]

76. In the figure, O is the centre of sector OABC. It is given that  $\triangle OAB$  is an equilateral triangle. AC and OB intersect at the point D. If OA = 12 cm and  $\triangle AOC = 90^{\circ}$ , find the area of the shaded region BCD correct to the nearest  $cm^2$ .



- A. 11 cm2
- B. 16 cm<sup>2</sup>
- C. 26 cm<sup>2</sup>
- D. 38 cm<sup>2</sup>

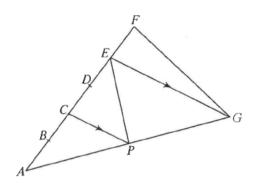
[2019-DSE-MATHS 2-38]

- 77. The angle of a sector is decreased by 60% but its radius is increased by k%. If the arc length of the sector remains unchanged, find the value of k.
  - A. 40
  - B. 60
  - C. 67
  - D. 150

[2020-DSE-MATHS 2-15]

# Areas in Proportion

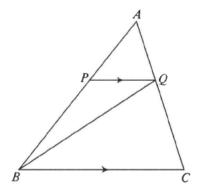
1. In  $\triangle AFG$ , points B, C, D and E divide AF into 5 equal parts.  $CP /\!/ EG$ . Area of  $\triangle AGF$ 



- **A.**  $\frac{1}{2}$ .
- **B.**  $\frac{1}{3}$ .
- **C.**  $\frac{2}{5}$ .
- **D.**  $\frac{3}{5}$ .
- **E.**  $\frac{4}{5}$ .

[SP-CE-MATHS A2-50]

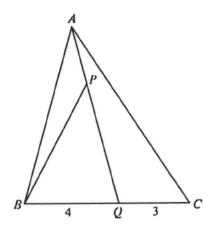
2. In  $\triangle ABC$ , PQ//BC. The area of  $\triangle APQ$  is 4. The area of  $\triangle PQB$  is 6. What is the area of  $\triangle QBC$ ?



- **A.** 8
- **B.** 9
- C. 10
- **D.** 12
- **E.** 15

[SP-CE-MATHS A2-52]

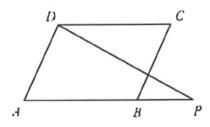
3. In the figure, BQ: QC = 4:3, and AP: PQ= 1:3. Then  $\frac{\text{Area of } \Delta ABP}{\text{Area of } \Delta ABC}$  =



- **A.**  $\frac{1}{3}$ .
- **B.**  $\frac{1}{4}$ .
- C.  $\frac{1}{7}$ .
- **D.**  $\frac{1}{8}$ .
- E.  $\frac{1}{9}$ .

[1978-CE-MATHS A2-54]

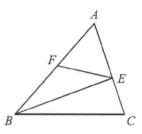
4. In the figure, ABCD is a parallelogram. AB is produced to P such that  $BP = \frac{1}{2}AB$ . Then  $\frac{\text{Area of } \Delta APD}{\text{Area of } ABCD} =$ 



- **A.**  $\frac{3}{4}$ .
- **B.**  $\frac{2}{3}$ .
- **C.**  $\frac{1}{2}$ .
- **D.**  $\frac{1}{3}$ .
- **E.**  $\frac{1}{4}$

[1979-CE-MATHS 2-44]

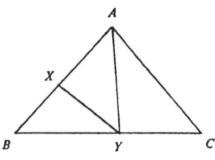
5. In the figure, F is the mid-point of AB. E is a point on AC such that AE : EC = 2 : 1.  $\frac{\text{Area of } \Delta BFE}{\text{Area of } \Delta BCE} =$ 



- **A.**  $\frac{1}{2}$
- **B.**  $\frac{2}{3}$
- **C.** 1
- **D.**  $\frac{3}{2}$
- **E.** 2

[1981-CE-MATHS 2-53]

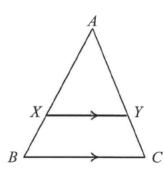
6. In the figure, X and Y are points on AB and BC respectively such that AX:XB=3:2 and BY:YC=4:3. If the area of  $\triangle ABC=70$ , then the area of  $\triangle AXY=$ 



- **A.** 16.
- **B.** 24.
- C. 30.
- **D.** 40.
- E. 42.

[1983-CE-MATHS 2-52]

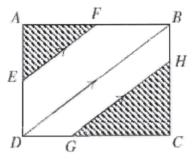
7. In the figure, XY // BC. AX : XB = 2 : 1. If the area of the trapezium BCYX = 20, then the area of  $\triangle ABC =$ 



- A. 80.
- **B.** 60.
- C. 45.
- **D.** 40.
- E. 36.

[1984-CE-MATHS 2-50]

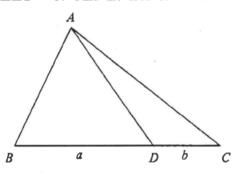
8. In the figure, *ABCD* is a rectangle *E*, *F*, *G* and *H* are points on the four sides such that *EF* // *DB* // *GH*. *AF* = *FB* and *HC* = 2 *BH*. What fraction of the area of *ABCD* is shaded?



- **A.**  $\frac{13}{36}$
- **B.**  $\frac{5}{12}$
- C.  $\frac{25}{36}$
- **D.**  $\frac{25}{72}$
- E.  $\frac{47}{72}$

[1985-CE-MATHS 2-52]

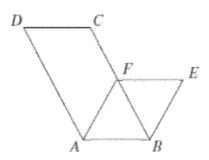
9. In the figure, BD = a, DC = b and the area of  $\triangle ABD = s$ . Find the area of  $\triangle ABC$ .



- $\mathbf{A.} \quad \frac{s(a+b)}{a}$
- $\mathbf{B.} \quad \frac{s(a+b)}{b}$
- $\mathbf{C.} \quad \frac{s(a+b)^2}{a^2}$
- **D.**  $\frac{s(a+b)^2}{b^2}$
- E.  $\frac{s(a^2+b^2)}{a^2}$

[1987-CE-MATHS 2-21]

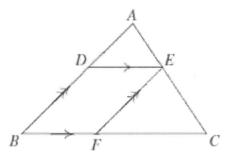
10. In the figure, ABCD and ABEF are parallelograms.  $\frac{Area \text{ of } ABCD}{Area \text{ of } ABEF} =$ 



- A.  $\frac{AD}{AF}$
- **B.**  $\frac{BC}{BF}$
- C.  $\frac{BC}{EF}$ .
- $\mathbf{D.} \quad \frac{AD^2}{AF^2}.$
- E.  $\frac{BC^2}{EF^2}$ .

[1987-CE-MATHS 2-24]

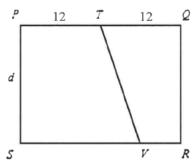
11. In the figure,  $DE /\!\!/ BC$  and  $AB /\!\!/ EF$ . If AE: EC = 1:2, then area of  $\Delta ADE$ : area of parallelogram BFED =



- **A.** 1:2.
- **B.** 1:3.
- **C.** 1:4.
- **D.** 1:5.
- **E.** 1:6.

[1987-CE-MATHS 2-54]

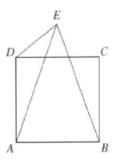
12. In the figure, PQRS is a rectangle with PQ = 24 and PS = d. T is the mid-point of PQ. V is a point on SR and  $\frac{\text{area } PTVS}{\text{area } TQRV} = 2$ .  $SV = \frac{1}{2} \frac$ 



- A. 14
- **B.** 16.
- C. 18.
- **D.** 20.
- E. 22.

[1988-CE-MATHS 2-11]

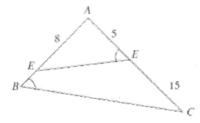
13. In the figure, ABCD is a square and AE = BE.  $\frac{\text{Area of } AED}{\text{Area of } ABCD} =$ 



- **A.**  $\frac{1}{2}$
- **B.**  $\frac{3}{8}$
- C.  $\frac{1}{3}$
- **D.**  $\frac{1}{4}$
- E.  $\frac{1}{8}$

[1989-CE-MATHS 2-11]

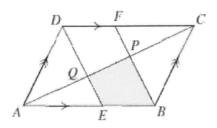
14. In the figure, D and E are points on AB and AC respectively such that  $\angle ABC = \angle AED$ , AD = 8, AE = 5 and EC = 15. If the area of  $\triangle ADE$  is 16, then the area of the quadrilateral BCED is



- A. 200.
- **B.** 100.
- C. 96
- D. 84.
- E. 40.

[1989-CE-MATHS 2-37]

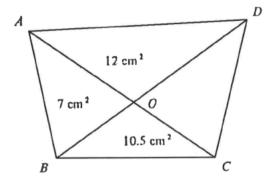
15. In the figure, ABCD is a parallelogram. E and F are the mid-points of AB and DC respectively. BF and ED cut AC at P and Q respectively. If the area of ABCD is 48, find the area of the shaded part.



- **A.** 6
- **B.** 8
- C. 9.6
- **D.** 12
- E. 16

[1989-CE-MATHS 2-53]

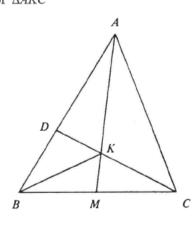
16. In the figure, AC cuts BD at O. The areas of  $\triangle AOB$ ,  $\triangle AOD$  and  $\triangle BOC$  are 7 cm<sup>2</sup>, 12 cm<sup>2</sup> and 10.5 cm<sup>2</sup> respectively. Find the area of  $\triangle OCD$ .



- **A.**  $5.5 \text{ cm}^2$
- **B.** 8 cm<sup>2</sup>
- **C.**  $8.5 \text{ cm}^2$
- **D.**  $15.5 \text{ cm}^2$
- **E.**  $18 \text{ cm}^2$

[1989-CE-MATHS 2-54]

17. In the figure, M is the mid-point of BC and AD = 2DB. AM and CD intersect at K. Find  $\frac{\text{area of } \Delta ADK}{\text{area of } \Delta AKC}$ .

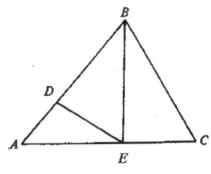


**A.**  $\frac{1}{2}$ 

- **B.**  $\frac{2}{3}$
- C.  $\frac{3}{4}$
- **D.**  $\frac{4}{5}$
- **E.** 1

[1991-CE-MATHS 2-53]

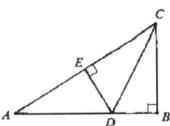
18. In the figure, AD:DB=1:2, AE:EC=3:2. Area of  $\triangle BDE:$  Area of  $\triangle ABC=$ 



- **A.** 1:3.
- **B.** 2:5.
- **C.** 3:4.
- **D.** 4:25.
- **E.** 36:65.

[1994-CE-MATHS 2-45]

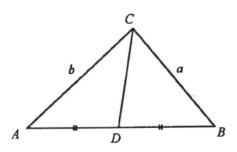
19. In the figure, DE = DB, AC = 13 and BC = 5. Area of  $\triangle ADE$ : Area of  $\triangle ACB =$ 



- **A.** 64:169.
- **B.** 5:13.
- C. 4:9.
- **D.** 8:13.
- E. 2:3.

[1995-CE-MATHS 2-47]

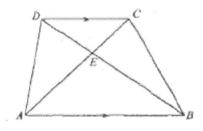
20. In the figure, area of  $\Delta ACD$  : area of  $\Delta BCD$ 



- 1:1.
- a:b. В.
- C. b:a.
- **D.**  $a^2:b^2$ .
- **E.**  $b^2 : a^2$ .

[1996-CE-MATHS 2-15]

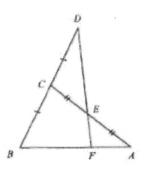
Area of triangle CDE 21. In the figure, if Area of triangle BCE Area of triangle CDE find Area of trapezium ABCD



- D.
- E.

[1996-CE-MATHS 2-46]

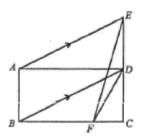
22. In the figure, DE: EF =



- 1:1.
- В. 2:1.
- C. 3:1.
- D. 3:2.
- 4:1. E.

[1996-CE-MATHS 2-52]

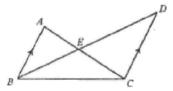
23. In the figure, ABCD is a rectangle. CDE is a straight line and AE // BD. If the area of ABCD is 24 and F is a point on BC such that BF:FC=3:1, find the area of  $\Delta DEF$ .



- 2 A.
- 3 В.
- C. 4
- D. 6
- E. 8

[1997-CE-MATHS 2-53]

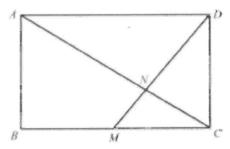
24. In the figure, AB // DC. If the areas of  $\triangle ABE$ and  $\Delta CDE$  are 4 and 9 respectively, find the area of  $\Delta BCE$ .



- A.
- 5 В.
- C. 6
- D. 6.5
- 9 E.

[1997-CE-MATHS 2-54]

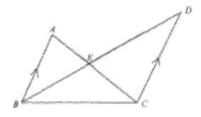
25. In the figure, ABCD is a rectangle. M is the midpoint of BC and AC intersects MD at N. Area of  $\triangle NCD$ : area of ABMN =



- 1:2. A.
- В. 1:3.
- 2:3.
- 2:5. D.
- 4:7.

[1999-CE-MATHS 2-54]

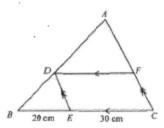
26. In the figure, AEC and BED are straight lines. If the area of  $\triangle ABE = 4 \text{ cm}^2$  and the area of  $\triangle BCE = 5 \text{ cm}^2$ , find the area of  $\triangle CDE$ .



- **A.**  $4.5 \text{ cm}^2$
- $B. 5 cm^2$
- C. 6 cm<sup>2</sup>
- **D.**  $6.25 \text{ cm}^2$
- $\mathbf{E}$ . 9 cm<sup>2</sup>

[2000-CE-MATHS 2-54]

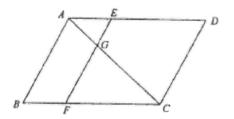
27. In the figure, ADB, BEC and CFA are straight lines. If the area of  $\triangle ABC$  is 225 cm<sup>2</sup>, find the area of the parallelogram DECF.



- **A.**  $81 \text{ cm}^2$
- **B.**  $108 \text{ cm}^2$
- $C. 126 \text{ cm}^2$
- **D.**  $135 \text{ cm}^2$
- E. 162 cm<sup>2</sup>

[2001-CE-MATHS 2-50]

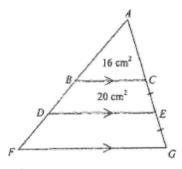
28. In the figure, ABCD is a parallelogram. E and F are points on AD and BC respectively such that AB // EF. EF meets AC at G. If AG:GC=1:2, then area of ABFG: area of EGCD=



- **A.** 1:2.
- **B.** 1:4.
- C. 3:4.
- **D.** 5:8.

[2002-CE-MATHS 2-44]

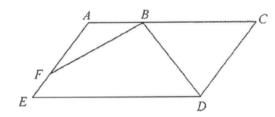
29. In the figure, ABDF and ACEG are straight lines. If the area of  $\Delta ABC$  is  $16~\rm cm^2$  and the area of quadrilateral BDEC is  $20~\rm cm^2$ , then the area of quadrilateral DFGE is



- **A.**  $24 \text{ cm}^2$ .
- **B.**  $28 \text{ cm}^2$ .
- C.  $36 \text{ cm}^2$ .
- **D.**  $44 \text{ cm}^2$ .

[2003-CE-MATHS 2-17]

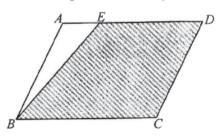
30. In the figure, AEDC is a parallelogram. If AB:BC=1:2 and AF:FE=2:1, then the area of  $\triangle ABF:$  area of  $\triangle BCD=$ 



- A. 1:2.
- **B.** 1:3.
- C. 1:4.
- **D.** 2:9.

[2003-CE-MATHS 2-18]

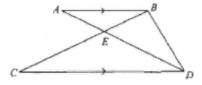
31. In the figure, ABCD is a parallelogram and E is a point on AD such that AE : ED = 1 : 3. If the area of  $\triangle ABE$  is  $3 \text{ cm}^2$ , then the area of the shaded region is



- A.  $9 \text{ cm}^2$ .
- **B.**  $15 \text{ cm}^2$ .
- C.  $21 \text{ cm}^2$ .
- **D.**  $24 \text{ cm}^2$ .

[2004-CE-MATHS 2-17]

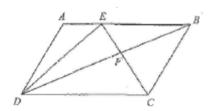
32. In the figure, AD and BC meet at E. If CE:EB=3:1, then area of  $\Delta ABD:$  area of  $\Delta CDE=$ 



- A. 1:1.
- **B.** 1:3.
- C. 2:3.
- **D.** 4:9.

[2004-CE-MATHS 2-18]

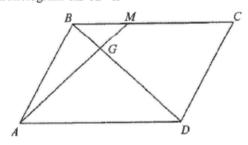
33. In the figure, ABCD is a parallelogram. E is a point lying on AB. If EC and BD intersect at F, then the ratio of the area of  $\Delta DEF$  to the area of  $\Delta CBF$  is



- A. 1:1:
- **B.** 1:2.
- C. 2:1.
- **D.** 2:3.

[2007-CE-MATHS 2-19]

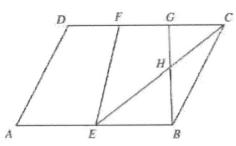
34. In the figure, ABCD is a parallelogram. M is a point lying on BC such that BM : MC = 1 : 2. If BD and AM intersect at G and the area of  $\Delta BGM$  is  $1 \text{ cm}^2$ , then the area of the parallelogram ABCD is



- $\mathbf{A.} \quad 9 \text{ cm}^2$
- **B.**  $11 \text{ cm}^2$ .
- C.  $12 \text{ cm}^2$ .
- **D.**  $24 \text{ cm}^2$ .

[2008-CE-MATHS 2-21]

35. In the figure, ABCD is a parallelogram. E is the mid-point of AB. F and G are points lying on CD such that DF = FG = GC. BG and CE intersect at H. If the area of  $\Delta BCH$  is  $6 \text{ cm}^2$ , then the area of the quadrilateral EFGH is

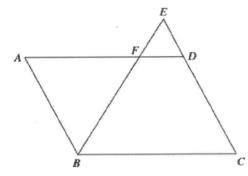


- **A.**  $10 \text{ cm}^2$ .
- **B.**  $12 \text{ cm}^2$ .
- C.  $15 \text{ cm}^2$ .
- **D.**  $16 \text{ cm}^2$ .

[2011-CE-MATHS 2-19]

### **HKDSE Problems**

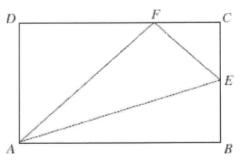
36. In the figure, ABCD is a parallelogram. F is a point lying on AD. BF produced and CD produced meet at E. If CD:DE=2:1, then AF:BC=



- A. 1:2.
- **B.** 2:3.
- C. 3:4.
- **D.** 8:9.

[SP-DSE-MATHS 2-23]

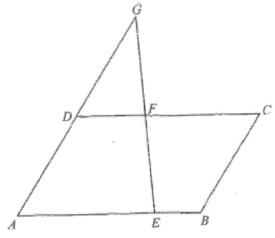
37. In the figure, ABCD is a rectangle. E is the mid-point of BC. F is a point lying on CD such that DF = 2CF. If the area of  $\Delta CEF$  is  $1 \text{ cm}^2$ , then the area of  $\Delta AEF$  is



- $\mathbf{A}$ . 2 cm<sup>2</sup>.
- **B.**  $3 \text{ cm}^2$ .
- $\mathbf{C}$ . 4 cm<sup>2</sup>.
- **D.**  $6 \text{ cm}^2$ .

[PP-DSE-MATHS 2-17]

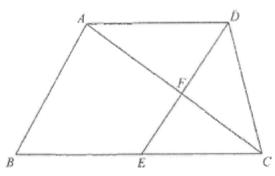
38. In the figure, ABCD is a parallelogram. E and F are points lying on AB and CD respectively. AD produced and EF produced meet at G. It is given that DF:FC=3:4 and AD:DG=1:1. If the area of  $\Delta DFG$  is  $3 \text{ cm}^2$ , then the area of the parallelogram ABCD is



- **A.**  $12 \text{ cm}^2$ .
- **B.**  $14 \text{ cm}^2$ .
- C.  $18 \text{ cm}^2$ .
- **D.**  $21 \text{ cm}^2$ .

[2012-DSE-MATHS 2-17]

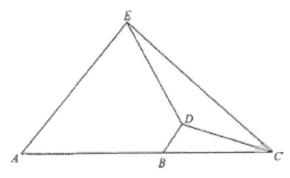
39. In the figure, ABCD is a trapezium with AD // BC and AD : BC = 2 : 3. Let E be the mid-point of BC. AC and DE intersect at F. If the area of  $\Delta CEF$  is 36 cm<sup>2</sup>, then the area of the trapezium ABCD is



- **A.**  $216 \text{ cm}^2$ .
- **B.**  $264 \text{ cm}^2$ .
- C.  $280 \text{ cm}^2$ .
- **D.**  $320 \text{ cm}^2$ .

[2013-DSE-MATHS 2-18]

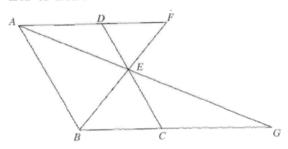
40. In the figure, B is a point lying on AC such that AB:BC=3:2. It is given that  $AE \parallel BD$ . If the area of  $\Delta BCD$  and the area of  $\Delta CDE$  are 4 cm<sup>2</sup> and 8 cm<sup>2</sup> respectively, then the area of the trapezium ABDE is



- **A.**  $18 \text{ cm}^2$ .
- **B.**  $21 \text{ cm}^2$ .
- C. 27 cm<sup>2</sup>.
- **D.**  $33 \text{ cm}^2$ .

[2014-DSE-MATHS 2-17]

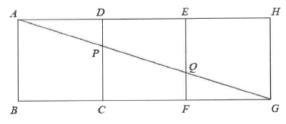
41. In the figure, ABCD is a parallelogram. E is a point lying on CD such that DE:EC=2: 3. AD produced and BE produced meet at F while AE produced and BC produced meet at G. If the area of  $\Delta DEF$  is  $8 \text{ cm}^2$ , then the area of  $\Delta CEG$  is



- **A.**  $12 \text{ cm}^2$ .
- **B.**  $18 \text{ cm}^2$ .
- C.  $20 \text{ cm}^2$ .
- **D.**  $27 \text{ cm}^2$ .

[2015-DSE-MATHS 2-17]

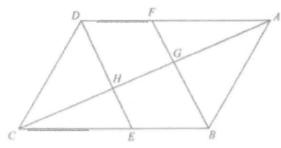
42. In the figure, ABCD, CDEF and EFGH are squares. AG cuts CD and EF at P and Q respectively. Find the ratio of the area of the quadrilateral DEQP to the area of the quadrilateral ABCP.



- **A.** 1:2
- **B.** 2:3
- C. 3:5
- **D.** 4:9

[2016-DSE-MATHS 2-20]

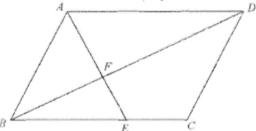
43. In the figure, ABCD and BEDF are parallelograms. E is a point lying on BC such that BE:EC=2:3. AC cuts BF and DE at G and H respectively. If the area of  $\triangle ABG$  is 135 cm<sup>2</sup>, then the area of the quadrilateral DFGH is



- **A.**  $60 \text{ cm}^2$
- **B.**  $81 \text{ cm}^2$
- $C_* = 90 \text{ cm}^2$
- **D.** 144 cm<sup>2</sup>.

[2017-DSE-MATHS 2-16]

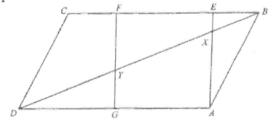
44. In the figure, ABCD is a parallelogram. E is a point lying on BC such that BE:EC=5:3. AE and BD intersect at point F. If the area of  $\triangle ABF$  is  $120cm^2$ , then the area of the quadrilateral CDFE is



- A. 237 cm<sup>2</sup>
- B. 307 cm<sup>2</sup>
- C. 312 cm<sup>2</sup>
- D. 429 cm<sup>2</sup>

[2018-DSE-MATHS 2-16]

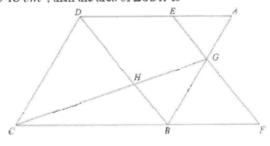
45. In the figure, ABCD is parallelogram and AEFG is a square. It is given that BE: EF: FC = 2:7:3. BD cuts AE and FG at points X and Y respectively. If the area of  $\triangle ABX$  is  $24 \ cm^2$ , then the area of the quadrilateral CDYF is



- A. 54 cm<sup>2</sup>
- B. 77 cm<sup>2</sup>
- C. 81 cm<sup>2</sup>
- D.  $87 cm^2$

[2019-DSE-MATHS 2-16]

46. In the figure, ABCD is a parallelogram. Let E be a point lying on AD such that AE:ED=2:5. CB is produced to the point F such that BF=DE. Denote the point of intersection of AB and EF by G. It is given that BD and CG intersect at the point H. If the area of  $\triangle AEG$  is  $48 \ cm^2$ , then the area of  $\triangle CDH$  is



- A.  $98 cm^2$
- B. 343 cm<sup>2</sup>
- C. 420 cm<sup>2</sup>
- **D.**  $588 cm^2$

[2020-DSE-MATHS 2-18]

# Mensuration of Solids

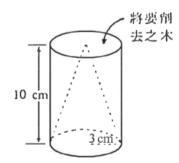
- 1. A cube of edge 4 cm floats upright in water with  $\frac{3}{4}$  of its volume immersed. The total surface area under water is
  - **A.**  $72 \text{ cm}^2$ .
  - **B.**  $64 \text{ cm}^2$ .
  - $C. 60 \text{ cm}^2.$
  - **D.**  $52 \text{ cm}^2$ .
  - **E.**  $48 \text{ cm}^2$ .

[1977-CE-MATHS 2-12]

- 2. If the height, the width and the length of a rectangular block are in the ratios of 1:2:3 respectively and its total surface area is 88 cm², then the height of the block is
  - A. 8 cm.
  - B. 6 cm.
  - C. 4 cm.
  - D. 2 cm.
  - E. 1 cm.

[SP-CE-MATHS A2-42]

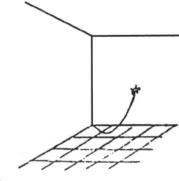
3. A solid wooden cylinder of base radius 3 cm and height 10 cm is to be cut into a right circular cone of the same base radius and height. The volume of wood to be cut away is



- **A.**  $10\pi \text{ cm}^3$ .
- **B.**  $20\pi \text{ cm}^3$ .
- C.  $30\pi \text{ cm}^3$ .
- **D.**  $60\pi \text{ cm}^3$ .
- **E.**  $90\pi \text{ cm}^3$ .

[1978-CE-MATHS 2-23]

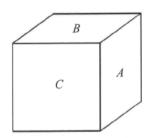
4. A dragonfly is tied to a string 1 metre long attached to a corner of a room. (See figure.) The walls and the floor are at right angles to one another. In how much space, in m<sup>3</sup>, can the dragonfly move?



- A.  $\frac{3}{32}\pi$
- **B.**  $\frac{1}{6}\pi$
- C.  $\frac{1}{3}\pi$
- **D.**  $\frac{2}{3}\pi$
- E.  $\frac{4}{3}\pi$

[1979-CE-MATHS 2-26]

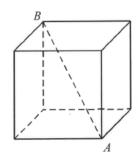
5. In the figure, the areas of the surfaces A, B, C of the cuboid are 10 cm<sup>2</sup>, 14 cm<sup>2</sup> and 35 cm<sup>2</sup> respectively. What is the volume of the cuboid?



- $\mathbf{A.} \quad 49 \text{ cm}^3$
- **B.**  $70 \text{ cm}^3$
- **C.**  $140 \text{ cm}^3$
- **D.**  $350 \text{ cm}^3$
- **E.** 4900 cm<sup>3</sup>

[1980-CE-MATHS 2-39]

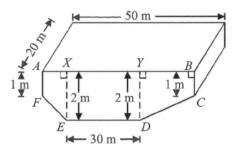
6. The total area of the six faces of the solid cube in the figure is 96 cm<sup>2</sup>. What is the length of the diagonal AB?



- A.  $6\sqrt{2}$  cm
- **B.**  $4\sqrt{3}$  cm
- C.  $4\sqrt{2}$  cm
- **D.**  $2\sqrt{6}$  cm
- E. 4 cm

[1981-CE-MATHS 2-16]

7.

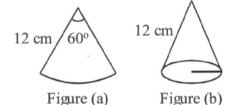


The figure above represents a  $50 \text{ m} \times 20 \text{ m}$  swimming pool. The pool is in the shape of a prism with a rectangular surface and four vertical walls. The dimensions of the sidewall *ABCDEF* are as shown in the figure. What is the capacity of the pool in  $\text{m}^3$ ?

- A. 1200
- **B.** 1500
- **C.** 1800
- **D.** 2000
- E. It cannot be determined

[1981-CE-MATHS 2-42]

8.



The cone in Figure (b) is formed by bending the sector in Figure (a). The angle of the sector is 60° and the radius is 12 cm. The radius of the base of the cone is

- A. 2 cm.
- B. 4 cm.
- C. 6 cm.
- **D.**  $2\pi$  cm.
- $E. \quad \frac{360}{\pi} \text{ cm}$

[1981-CE-MATHS 2-47]

- 9. A right circular cone of altitude 3r and base radius r has the same volume as a cube of side x. x =
  - A.  $\pi r^3$ .
  - B.  $\pi r$ .
  - C.  $\frac{1}{3}\pi r$ .
  - $\mathbf{D.} \quad \sqrt[3]{3\pi}r$
  - E.  $\sqrt[3]{\pi r}$ .

[1982-CE-MATHS 2-14]

- A hollow cylindrical metal pipe, 1 m long, has an external radius and an internal radius of 5 cm and 4 cm respectively. The volume of metal is
  - **A.**  $90\pi \text{ cm}^3$ .
  - **B.**  $100\pi \text{ cm}^3$ .
  - C.  $180\pi \text{ cm}^3$ .
  - **D.**  $900\pi \text{ cm}^3$ .
  - E.  $1800\pi \text{ cm}^3$ .

[1983-CE-MATHS 2-13]

- 11. A rectangular box, without a lid, is 40 cm long, 30 cm wide and 10 cm height. The area of the external surface of the box is
  - A.  $2 600 \text{ cm}^2$ .
  - **B.**  $3 400 \text{ cm}^2$ .
  - C.  $3\,500\,\mathrm{cm}^2$ .
  - **D.**  $3 800 \text{ cm}^2$ .
  - E. 12 000 cm<sup>2</sup>.

[1984-CE-MATHS 2-13]

- 12. The base radii of two right circular cylinders are in the ratio 2:3. If the two cylinders have the same height, what is the ratio of their curved surface area?
  - **A.** 2:3
  - **B.** 4:9
  - C. 8:27
  - **D.**  $\sqrt{8}:\sqrt{27}$
  - E. None of the above.

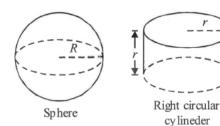
[1984-CE-MATHS 2-43]

- 13. A cone of base radius 2r cm and height h cm has a volume of  $60 \text{ cm}^3$ . The volume of a cylinder of base radius r cm and height 4h cm is
  - **A.**  $60 \text{ cm}^3$
  - **B.**  $120 \text{ cm}^3$ .
  - **C.**  $180 \text{ cm}^3$ .
  - **D.**  $240 \text{ cm}^3$
  - **E.**  $360 \text{ cm}^3$

[1985-CE-MATHS 2-43]

**UNIT 9.4** 

14.



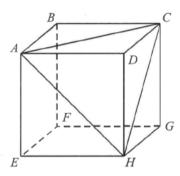
 $\frac{\text{In the figure,}}{\text{Volume of the sphere}} = \frac{\text{if}}{2},$ 

then  $\frac{R}{r} =$ 

- **A.**  $\frac{3}{2}$ .
- **B.**  $\frac{3}{\sqrt{2}}$
- C. 3.
- **D.**  $\frac{\sqrt[3]{9}}{\sqrt[3]{2}}$
- **E.**  $\frac{9}{2}$

[1986-CE-MATHS 2-12]

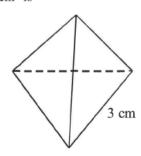
15. ABCDEFGH is a cube of side 3 cm. A tetrahedron DACH is cut away along the plane ACH. The volume of the remaining solid is



- A.  $6 \text{ cm}^3$ .
- **B.**  $9 \text{ cm}^3$ .
- C.  $13.5 \text{ cm}^3$ .
- **D.**  $18 \text{ cm}^3$
- E.  $22.5 \text{ cm}^3$

[1986-CE-MATHS 2-38]

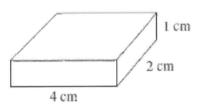
16. The total surface area of a regular tetrahedron of side 3 cm is



- **A.**  $\frac{9\sqrt{3}}{4}$  cm<sup>2</sup>.
- **B.**  $9 \text{ cm}^2$ .
- C.  $\frac{27\sqrt{3}}{4}$  cm<sup>2</sup>.
- **D.**  $9\sqrt{3}$  cm<sup>2</sup>.
- **E.**  $12\sqrt{3}$  cm<sup>2</sup>.

[1986-CE-MATHS 2-40]

17. A solid rectangular iron block,  $4 \text{ cm} \times 2 \text{ cm} \times 1 \text{ cm}$ , is melted and recast into a cube. The decrease in the total surface area is



- A.  $1 \text{ cm}^2$ .
- **B.**  $2 \text{ cm}^2$ .
- $\mathbf{C}$ . 3 cm<sup>2</sup>.
- **D.**4 cm<sup>2</sup>.
- $E. 5 cm^2$ .

[1987-CE-MATHS 2-13]

18. Figure A shows a circular measuring cylinder 4 cm in diameter containing water. Three iron balls, each of diameter 2 cm, are dropped into the cylinder as shown in Figure B. What is the rise in the water level?

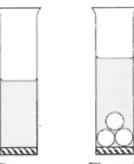


Figure a

Figure b

- **A.**  $\frac{1}{4}$  cm
- **B.**  $\frac{1}{3}$  cm
- C.  $\frac{1}{2}$  cm
- **D.** 1 cm

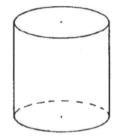
E. 2 cm

[1987-CE-MATHS 2-14]

- 19. A solid iron sphere of radius r is melted and recast into a circular cone and a circular cylinder. If both of them have the same height h and the same base radius r, find h in terms of r.
  - A.  $\frac{r}{2}$
  - **B.**  $\frac{9r}{16}$
  - C.  $\frac{2r}{3}$
  - **D.**  $\frac{3r}{4}$
  - E. 1

[1988-CE-MATHS 2-10]

20. In the figure, the circular cylinder and the circular cone have the same height. The radius of the base of the cylinder is twice that of the cone. If the volume of the cone is 20 cm³, what is the volume of the cylinder?





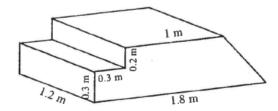
- **A.**  $40 \text{ cm}^3$
- **B.**  $80 \text{ cm}^3$
- C. 120 cm<sup>3</sup>
- **D.**  $240 \text{ cm}^3$
- E. 300 cm<sup>3</sup>

[1990-CE-MATHS 2-11]

- 21. The length, width and height of a cuboid are in the ratios 3:2:1. If the total surface area of the cuboid is 88 cm<sup>2</sup>, find its volume.
  - A.  $6 \text{ cm}^3$
  - **B.**  $48 \text{ cm}^3$
  - C.  $48\sqrt{2} \text{ cm}^3$
  - **D.**  $96\sqrt{2} \text{ cm}^3$
  - E. 384 cm<sup>3</sup>

[1990-CE-MATHS 2-12]

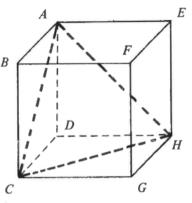
22. The figure shows a solid platform with steps on one side and a slope on the other. Find its volume.



- **A.**  $0.75 \text{ m}^3$
- **B.**  $0.84 \text{ m}^3$
- $\mathbf{C}$ . 0.858  $\mathbf{m}^3$
- **D.**  $1.008 \text{ m}^3$
- E.  $1.608 \text{ m}^3$

[1992-CE-MATHS 2-13]

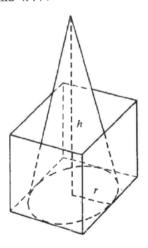
23. Find the ratio of the volume of the tetrahedron *ACHD* to the volume of the cube *ABCDEFGH* in the figure.



- **A.** 1:8
- **B.** 1:6
- C. 1:4
- **D.** 1:3
- **E.** 1:2

[1992-CE-MATHS 2-15]

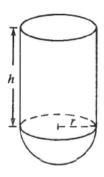
24. In the figure, the base of the conical vessel is inscribed in the bottom of the cubical box. If the box and the conical vessel have the same capacity, find h:r.



- **A.** 24:  $\pi$
- **B.** 3:1
- C.  $6:\pi$
- **D.**  $3:\pi$
- **E.**  $8:3\pi$

[1993-CE-MATHS 2-16]

25.



**UNIT 9.4** 

The figure shows a solid consisting of a cylinder of height h and a hemisphere of radius r. The area of the curved surface of the cylinder is twice that of the hemisphere.

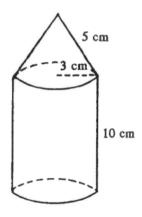
Find the ratio

volume of cylinder: volume of hemisphere.

- A. 1:3
- **B.** 2:3
- C. 3:4
- **D.** 3:2
- **E.** 3:1

[1993-CE-MATHS 2-17]

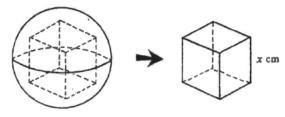
26. In the figure, the solid consists of a cylinder and a right circular cone with a common base which is a circle of radius 3 cm. The height of the cylinder is 10 cm and the slant height of the cone is 5 cm. Find the total surface area of the solid.



- **A.**  $75\pi \text{ cm}^3$
- **B.**  $84\pi \text{ cm}^3$
- C.  $93\pi \text{ cm}^3$
- **D.**  $105\pi \text{ cm}^3$
- **E.**  $114\pi \text{ cm}^3$

[1995-CE-MATHS 2-15]

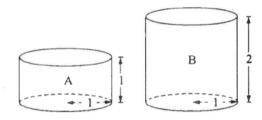
27. In the figure, a solid wooden sphere of radius 3 cm is to be cut into a cube of side x cm. Find the largest possible value of x.



- **A.**  $3\sqrt{2}$
- **B.**  $2\sqrt{3}$
- C. :
- **D.**  $\frac{3}{2}\sqrt{2}$
- $\mathbf{E}$ .  $\sqrt{3}$

[1995-CE-MATHS 2-48]

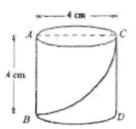
28. In the figure, A and B are two right solid cylinders with the same base radius 1. If the heights of A and B are 1 and 2 respectively, find  $\frac{\text{the total surface area of } A}{\text{the total surface area of } B}$ .



- **A.**
- B. -
- C.  $\frac{1}{2}$
- **D.**  $\frac{3}{5}$
- E.  $\frac{2}{3}$

[1996-CE-MATHS 2-18]

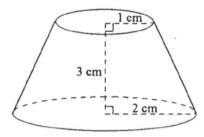
29. The figure shows a right circular cylinder with *AC* being a diameter of its upper face. *AB* and *CD* are two vertical lines on the curved surface. A curve is drawn on the surface of the cylinder from *B* to *C*. Find its shortest possible length.



- A.  $2\pi$  cm
- **B.**  $2\sqrt{\pi^2 + 4}$  cm
- C.  $4\sqrt{2}$  cm
- **D.**  $4\sqrt{\pi^2 + 1}$  cm
- E.  $4\sqrt{\pi^2 + 4}$  cm

[1996-CE-MATHS 2-27]

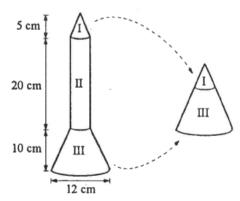
30. The figure shows a frustum of a right circular cone. The radii of the upper face and the base are 1 cm and 2 cm respectively. If the height is 3 cm, find the volume.



- A.  $3\pi$  cm<sup>3</sup>
- **B.**  $\frac{9}{2}\pi \text{ cm}^3$
- C.  $\frac{11}{2}\pi$  cm<sup>3</sup>
- **D.**  $7\pi \text{ cm}^3$
- **E.**  $\frac{15}{2}\pi \text{ cm}^3$

[1996-CE-MATHS 2-45]

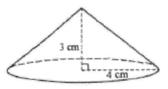
31. In the figure, the rocket model consists of three parts. Parts I and III can be joined together to form a right circular cone. Part II is a right cylinder. Find the volume of the rocket model.



- **A.**  $260\pi \text{ cm}^3$
- **B.**  $360\pi \text{ cm}^3$
- C.  $620\pi \text{ cm}^3$
- **D.**  $720\pi \text{ cm}^3$
- **E.**  $900\pi \text{ cm}^3$

[1997-CE-MATHS 2-49]

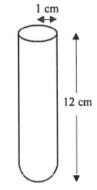
32. The figure shows a right circular cone of base radius 4 cm and height 3 cm. Find the area of its curved surface.



- **A.**  $12\pi \text{ cm}^2$
- **B.**  $16\pi \text{ cm}^2$
- C.  $20\pi \text{ cm}^2$
- **D.**  $24\pi \text{ cm}^2$
- **E.**  $48\pi \text{ cm}^2$

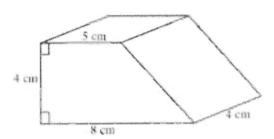
[1998-CE-MATHS 2-20]

- 33. The figure shows a test tube consisting of a cylindrical upper part of radius 1 cm and a hemispherical lower part of the same radius. If the height of the test tube is 12 cm, find its capacity.
  - **A.**  $\frac{35}{3}\pi \text{ cm}^3$
  - **B.**  $\frac{37}{3}\pi \text{ cm}^3$
  - C.  $\frac{38}{3}\pi \text{ cm}^3$
  - **D.**  $\frac{40}{3}\pi \text{ cm}^3$
  - **E.**  $\frac{68}{3}\pi \text{ cm}^3$



[1998-CE-MATHS 2-22]

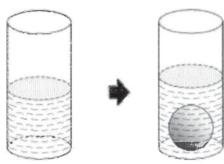
34. The figure shows a right prism. Find its total surface area.



- **A.** 104 cm<sup>2</sup>
- **B.**  $108 \text{ cm}^2$
- C. 114 cm<sup>2</sup>
- **D.**  $120 \text{ cm}^2$
- **E.**  $140 \text{ cm}^2$

[1999-CE-MATHS 2-22]

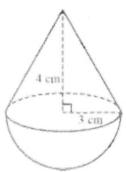
35. In the figure, a cylindrical vessel of internal diameter 6 cm contains some water. A steel ball of radius 2 cm is completely submerged in the water. Find the rise in the water level.



- $\frac{32}{27} \text{ cm}$   $\frac{8}{27} \text{ cm}$
- cm
- cm

[1999-CE-MATHS 2-23]

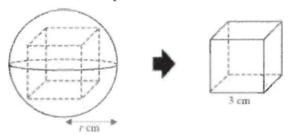
36. In the figure, the solid consists of a right circular cone and a hemisphere with a common base. Find the volume of the solid.



- $30\pi$  cm<sup>3</sup> A.
- $33\pi$  cm<sup>3</sup> В.
- C.  $48\pi$  cm<sup>3</sup>
- $54\pi$  cm<sup>3</sup> D.
- E.  $72\pi$  cm<sup>3</sup>

[1999-CE-MATHS 2-24]

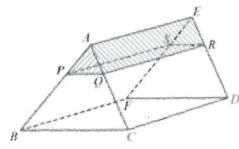
37. In the figure, a solid wooden sphere of radius r cm is to be cut into a cube of side 3 cm. Find the smallest possible value of r.



- D.
- $3\sqrt{2}$

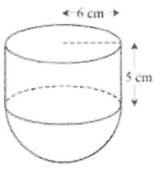
[2000-CE-MATHS 2-33]

38. In the figure, ABCDEF is a right triangular prism. It is cut into two parts along the plane PQRS, which is parallel to the face BCDF, and AP : PB = 2 : 5. Find volume of the prism APQRES volume of the prism ABCDEF



[2000-CE-MATHS 2-43]

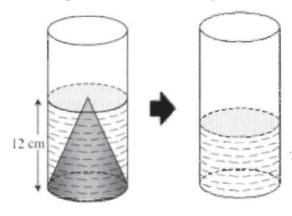
39. In the figure, the solid consists of a cylinder and a hemisphere with a common base of radius 6 cm. Find the total surface area of the solid.



- $132\pi$  cm<sup>2</sup> A.
- $168\pi \text{ cm}^2$ В.
- C.  $204\pi \text{ cm}^2$
- D.  $240\pi$  cm<sup>2</sup>
- $324\pi \text{ cm}^2$ E.

[2001-CE-MATHS 2-8]

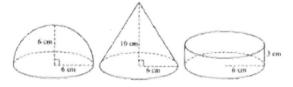
40. In the figure, a solid right circular cone of height 12 cm is put into a cylinder which has the same internal radius as the base radius of the cone. Water is then poured into the cylinder until the water level just reaches the tip of the cone. If the cone is removed, what is the height of the water in the cylinder?



- **A.** 3 cm
- **B.** 4 cm
- C. 6 cm
- D. 8 cm
- **E.** 9 cm

[2001-CE-MATHS 2-24]

41. The figure shows a hemisphere, a right circular cone and a right cylinder with equal base radii. Their volumes are  $a \text{ cm}^3$ ,  $b \text{ cm}^3$  and  $c \text{ cm}^3$  respectively.

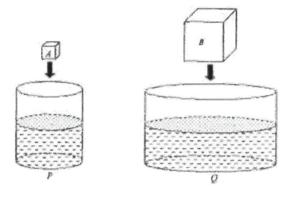


Which of the following is true?

- A. a < b < c
- **B.** a < c < b
- C. c < a < b
- **D.** c < b < a

[2002-CE-MATHS 2-19]

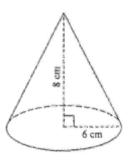
42. In the figure, P and Q are two right cylindrical vessels each containing some water. The two vessels are placed on the same horizontal surface. The internal base radii of P and Q are in the ratio 1:3. A and B are two cubes with sides in the ratio 1:2. A and B are put into P and Q respectively. Suppose both cubes are totally immersed in water without any overflow. If the rise in water level in P is 1 cm, then the rise in water level in Q is



- **A.**  $\frac{2}{3}$  cm.
- **B.**  $\frac{9}{8}$  cm.
- C.  $\frac{8}{9}$  cm.
- **D.**  $\frac{8}{27}$  cm.

[2002-CE-MATHS 2-45]

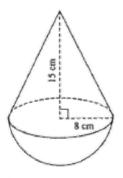
43. The figure shows a right circular cone of base radius 6 cm and height 8 cm. Find its volume.



- A.  $32\pi$  cm<sup>3</sup>
- **B.**  $60\pi \text{ cm}^3$
- **C.**  $96\pi \text{ cm}^3$
- **D.**  $288\pi \text{ cm}^3$

[2003-CE-MATHS 2-20]

44. In the figure, the solid consists of a right circular cone and a hemisphere with a common base. Find the total surface area of the solid.



- **A.**  $136\pi \text{ cm}^2$
- **B.**  $248\pi \text{ cm}^2$
- C.  $264\pi \text{ cm}^2$
- **D.**  $392\pi \text{ cm}^2$

[2003-CE-MATHS 2-21]

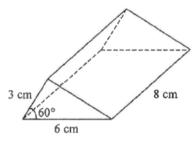
45. The figure shows a solid right circular cone of height 5 cm and slant height 13 cm. Find the total surface area of the cone.



- **A.**  $144\pi \text{ cm}^2$
- **B.**  $156\pi \text{ cm}^2$
- C.  $240\pi \text{ cm}^2$
- **D.**  $300\pi \text{ cm}^2$

[2005-CE-MATHS 2-17]

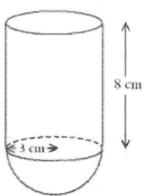
46. The figure shows a right triangular prism. Find the volume of the prism.



- **A.**  $36 \text{ cm}^3$
- **B.**  $72 \text{ cm}^3$
- C.  $36\sqrt{3} \text{ cm}^3$
- **D.**  $72\sqrt{3}$  cm<sup>3</sup>

[2005-CE-MATHS 2-18]

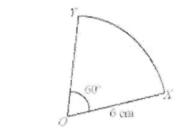
47. In the figure, the solid consists of a hemisphere of radius 3 cm joined to the bottom of a right circular cylinder of height 8 cm and base radius 3 cm. Find the volume of the solid.

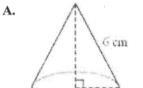


- **A.**  $75\pi \text{ cm}^3$
- **B.**  $90\pi \text{ cm}^3$
- C.  $93\pi \text{ cm}^3$
- **D.**  $108\pi \text{ cm}^3$

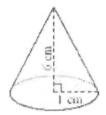
[2006-CE-MATHS 2-18]

48. In the figure, sector *OXY* is a thin metal sheet. By joining *OX* and *OY* together, which of the following right circular cones can be folded?



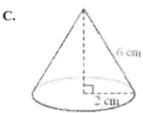


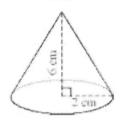
Lem



В.

D.





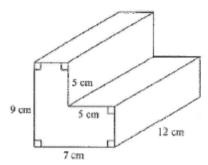
[2006-CE-MATHS 2-20]

- 49. If the length of a side of a regular tetrahedron is 3 cm, then the height of the tetrahedron is
  - A. 3 cm.
  - **B.**  $\sqrt{3}$  cm.
  - C.  $\sqrt{6}$  cm.
  - **D.**  $\frac{3\sqrt{3}}{2}$  cm

[2006-CE-MATHS 2-45]

50. In the figure, the volume of the right prism is

**UNIT 9.4** 



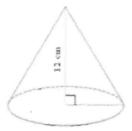
- A. 456 cm<sup>3</sup>.
- **B.**  $540 \text{ cm}^3$ .
- C.  $552 \text{ cm}^3$ .
- **D.**  $636 \text{ cm}^3$ .

[2007-CE-MATHS 2-17]

- 51. If a solid metal hemisphere of radius r is melted and recast into 3 identical solid right circular cones of height h and base radius r, then r:h=
  - A. 2:3.
  - **B.** 3:2.
  - C. 3:4.
  - **D.** 4:3.

[2007-CE-MATHS 2-18]

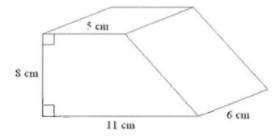
52. The figure shows a solid right circular cone of height 12 cm. The circumference of the base is  $18\pi$  cm. Find the total surface area of the circular cone.



- **A.**  $81\pi \text{ cm}^2$
- **B.**  $135\pi \text{ cm}^2$
- C.  $216\pi \text{ cm}^2$
- **D.**  $324\pi \text{ cm}^2$

[2008-CE-MATHS 2-18]

53. In the figure, the volume of the right prism is



- **A.**  $128 \text{ cm}^3$ .
- **B.**  $332 \text{ cm}^3$ .
- C.  $384 \text{ cm}^3$ .
- **D.**  $768 \text{ cm}^3$ .

[2008-CE-MATHS 2-19]

- 54. The base of a solid right pyramid is a square. If the perimeter of the base is 48 cm and the length of each slant edge of the pyramid is 10 cm, then the total surface area of the pyramid is
  - **A.**  $192 \text{ cm}^2$ .
  - **B.**  $336 \text{ cm}^2$ .
  - $C. 384 \text{ cm}^2.$
  - **D.**  $96\sqrt{7}$  cm<sup>2</sup>.

[2009-CE-MATHS 2-17]

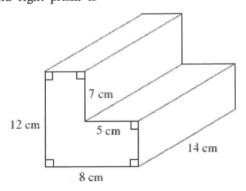
- 55. The base radius and the height of a right circular cylinder are 3 cm and 12 cm respectively while the base radius of a right circular cone is 6 cm. If the volume of the circular cylinder and the volume of the circular cone are the same, then the height of the circular cone is
  - A. 3 cm.
  - **B.** 9 cm.
  - C. 18 cm.
  - D. 27 cm.

[2009-CE-MATHS 2-18]

- 56. The volume of a right circular cylinder of radius R is twice the volume of another right circular cylinder of radius r. If the heights of these two circular cylinders are the same, then R: r =
  - A. 2:1.
  - **B.** 4:1.
  - C.  $\sqrt{2}:1$ ,
  - **D.**  $\sqrt{3}:1$ .

[2010-CE-MATHS 2-18]

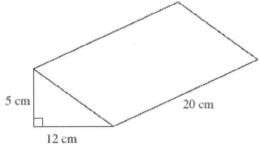
57. In the figure, the total surface area of the solid right prism is



- **A.**  $560 \text{ cm}^2$ .
- **B.**  $621 \text{ cm}^2$ .
- $C. 682 \text{ cm}^2.$
- **D.**  $854 \text{ cm}^2$ .

[2010-CE-MATHS 2-19]

58. In the figure, the total surface area of the solid right triangular prism is



- A.  $120 \text{ cm}^2$ .
- **B.**  $600 \text{ cm}^2$ .
- $C. 660 \text{ cm}^2$ .
- **D.**  $720 \text{ cm}^2$ .

[2011-CE-MATHS 2-17]

- 59. If the volume of a solid hemisphere of radius r is equal to the volume of a solid right circular cylinder of height h and base radius r, then r:h=
  - A. 2:3.
  - **B.** 3:2.
  - C. 3:4.
  - **D.** 4:3.

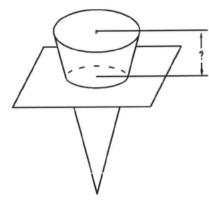
[2011-CE-MATHS 2-18]

#### Mensuration of Similar Solids

- 60.  $V_1$  = the volume of a sphere of radius 2a.  $V_2$  = the volume of a sphere of radius 3a. Then  $V_1:V_2$  =
  - A. 2:3.
  - **B.** 4:9.
  - C. 8:27.
  - **D.**  $4\pi:9\pi$ .
  - **E.**  $\sqrt[3]{2}:\sqrt[3]{3}$ .

[SP-CE-MATHS 2-34]

61. A circular hole of diameter 8 cm is drilled in a thin plate for holding a right circular cone. (See figure.) The base of the cone is parallel to the plate. If the base diameter of the cone is 10 cm and the height of the cone is 20 cm, what is the distance between the base of the cone and the plate?



- **A.** 2 cm
- **B.** 4 cm
- C. 6 cm
- **D.** 8 cm
- E. 10 cm

[1979-CE-MATHS 2-45]

- 62. A, B, C are three spheres.
  - If  $\frac{\text{Surface area of } A}{\text{Surface area of } B} = 4$  and

$$\frac{\text{Volume of } B}{\text{Volume of } C} = 2,$$

then 
$$\frac{\text{Volume of } A}{\text{Volume of } C} =$$

- **A.** 16.
- B. 8.
- C. 2.
- **D.**  $\frac{1}{8}$
- **E.**  $\frac{1}{16}$

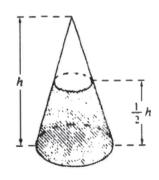
[1980-CE-MATHS 2-30]

63. The height of the cone in the figure is h.

It contains water to a depth of  $\frac{1}{2}h$ .

Volume of water
Capacity of the cone

- **A.**  $\frac{1}{8}$
- **B.**  $\frac{1}{4}$
- C.  $\frac{1}{2}$ .
- **D.**  $\frac{3}{4}$ .
- **E.**  $\frac{7}{8}$



[1981-CE-MATHS 2-41]

64. The external and internal radii of a hollow metal sphere are 4 cm and 3 cm respectively.

Volume of metal

Volume of the enclosed empty space

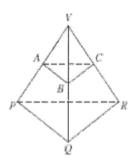
- **A.**  $\frac{1}{27}$ .
- **B.**  $\frac{1}{3}$ .
- **C.**  $\frac{4}{3}$
- **D.**  $\frac{37}{27}$ .
- **E.**  $\frac{64}{27}$ .

[1984-CE-MATHS 2-41]

- 65. A solid metal sphere of volume 252 cm³ is melted and recast into 3 smaller solid spheres whose radii are in the ratio 1:2:3. The volume of the smaller sphere is
  - A.  $5 \text{ cm}^3$ .
  - **B.**  $7 \text{ cm}^3$ .
  - C.  $14 \text{ cm}^3$ .
  - **D.**  $18 \text{ cm}^3$ .
  - $E. 28 \text{ cm}^3$ .

[1984-CE-MATHS 2-42]

66. In the figure, the volumes of the pyramids VABC and VPQR are 27 cm<sup>3</sup> and 64 cm<sup>3</sup> respectively. Planes ABC and PQR are parallel. Area of  $\Delta ABC$ : Area of  $\Delta PQR$ 

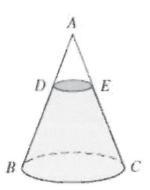


- **A.**  $\sqrt{27}:\sqrt{64}$ .
- **B.**  $\sqrt{37} : \sqrt{64}$ .
- C. 3:4.
- **D.** 9:16.
- **E.** 27:64.

[1985-CE-MATHS 2-44]

67. A right conical vessel placed on horizontal ground contains some water as shown in the figure. If AD:DB=2:3, then volume of empty space

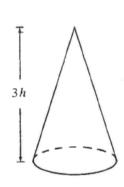
volume of water

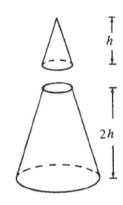


- **A.**  $\frac{4}{9}$
- **B.**  $\frac{8}{19}$ .
- C.  $\frac{8}{27}$ .
- **D.**  $\frac{8}{117}$ .
- E.  $\frac{8}{125}$ .

[1989-CE-MATHS 2-12]

68.



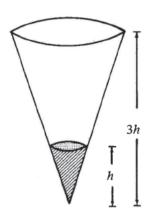


In the figure, a cone of height 3h is cut by a plane parallel to its base into a smaller cone of height h and a frustum. Find the ratio of the volume of the smaller cone to the volume of the frustum.

- **A.** 1:27
- **B.** 1:26
- C. 1:9
- **D.** 1:8
- **E.** 1:7

[1992-CE-MATHS 2-17]

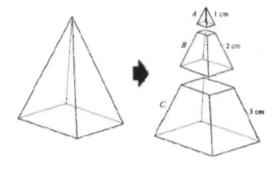
69. In the figure, the paper cup in the form of a circular cone contains 10 ml of water. How many ml of water must be added to fill up the paper cup?



- **A.** 20
- **B.** 80
- **C.** 90
- **D.** 260
- E. 270

[1994-CE-MATHS 2-13]

70. In the figure, a right pyramid with a square base is divided into three parts A, B and C by two planes parallel to the base such that the lengths of their slant edges are 1 cm, 2 cm and 3 cm respectively.

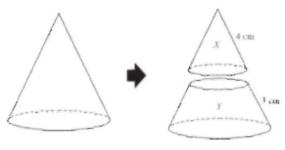


Find volume of A: volume of B: volume of C.

- **A.** 1:2:3
- **B.** 1:4:9
- **C.** 1:8:27
- **D.** 1:26:189
- E. 1:27:216

[1998-CE-MATHS 2-42]

71. In the figure, a right circular cone is divided into two parts X and Y by a plane parallel to the base such that the lengths of their slant edges are 4 cm and 3 cm respectively. Find the ratio of the curved surface areas of X and Y.



- **A.** 16:9
- **B.** 16:33
- C. 16:49
- **D.** 64:27
- E. 64:279

[1999-CE-MATHS 2-37]

- 72. It is given that A, B and C are solid spheres. If the volume of B: the volume of C = 1:8 and the surface area of A: the surface area of B = 9:4, then the radius of A: the radius of C = 1:4
  - A. 3:4.
  - **B.** 3:16.
  - C. 9:8.
  - **D.** 9:32.

[2009-CE-MATHS 2-19]

### **HKDSE Problems**

73. The figure shows a right circular cylinder, a hemisphere and a right circular cone with equal base radii. Their curved surface areas are  $a \text{ cm}^2$ ,  $b \text{ cm}^2$  and  $c \text{ cm}^2$  respectively.





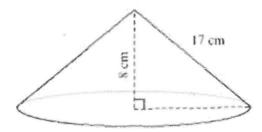


Which of the following is true?

- $\mathbf{A.} \quad a < b < c$
- **B.** a < c < b
- C. c < a < b
- **D.** c < b < a

[SP-DSE-MATHS 2-17]

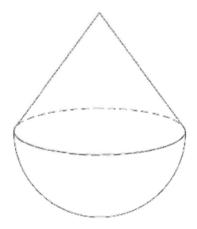
74. The figure shows a right circular cone of height 8 cm and slant height 17 cm. Find the volume of the circular cone.



- A.  $255\pi \text{ cm}^3$
- **B.**  $345\pi \text{ cm}^3$
- C.  $480\pi \text{ cm}^3$
- **D.**  $600\pi \text{ cm}^3$

[PP-DSE-MATHS 2-16]

75. In the figure, the solid consists of a right circular cone and a hemisphere with a common base. The base radius and the height of the circular cone are 3 cm and 4 cm respectively. Find the total surface area of the solid.



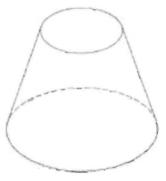
- A.  $30\pi$  cm<sup>2</sup>
- **B.**  $33\pi \text{ cm}^2$
- C.  $48\pi \text{ cm}^2$
- **D.**  $51\pi \text{ cm}^2$

[2013-DSE-MATHS 2-17]

- 76. If the height of a regular tetrahedron is 2 cm, then the volume of the tetrahedron is
  - A.  $2 \text{ cm}^3$ .
  - **B.**  $\sqrt{3} \text{ cm}^3$ .
  - C.  $\sqrt{6}$  cm<sup>3</sup>.
  - **D.**  $3\sqrt{3}$  cm<sup>3</sup>.

[2013-DSE-MATHS 2-40]

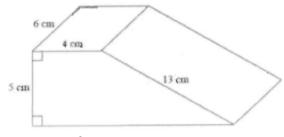
77. The height and the base radius of a right circular cone are 12 cm and 9 cm respectively. The figure shows a frustum which is made by cutting off the upper part of the circular cone. The height of the frustum is 8 cm. Find the volume of the frustum.



- **A.**  $210\pi \text{ cm}^3$
- **B.**  $312\pi \text{ cm}^3$
- C.  $324\pi \text{ cm}^3$
- **D.**  $936\pi \text{ cm}^3$

[2015-DSE-MATHS 2-16]

78. The figure shows a right prism. Find the volume of the prism.



- **A.**  $216 \text{ cm}^3$ .
- **B.**  $240 \text{ cm}^3$ .
- **C.**  $300 \text{ cm}^3$ .
- **D.**  $328 \text{ cm}^3$ .

[2016-DSE-MATHS 2-18]

- 79. The base radius of a right circular cone is 2 times the base radius of a right circular cylinder while the height of the circular cylinder is 3 times the height of the circular cone. If the volume of the circular cone is  $36\pi$  cm<sup>3</sup>, then the volume of the circular cylinder is
  - **A.**  $27\pi \text{ cm}^3$ .
  - **B.**  $48\pi \text{ cm}^3$ .
  - C.  $81\pi \text{ cm}^3$ .
  - **D.**  $144\pi \text{ cm}^3$ .

[2017-DSE-MATHS 2-15]

80. In the figure, the volume of the solid right triangular prism is



- **A.**  $544 cm^3$
- **B.**  $600 \text{ cm}^3$
- C.  $660 \text{ cm}^3$
- **D.**  $720 cm^3$

[2018-DSE-MATH\$ 2-15]

- 81. The base of a solid right pyramid is a square of side 18 cm. If the height of the pyramid is 12 cm, then the total surface area of the pyramid is
  - **A.**  $432 cm^2$
  - **B.**  $540 cm^2$
  - C.  $756 cm^2$
  - **D.**  $864 cm^2$

[2019-DSE-MATHS 2-15]

- 82. If the volume of a right circular cylinder of base radius 5a cm and height 7b cm is 525 cm<sup>3</sup>, then the volume of a right circular cone of base radius 7a cm and height 5b cm is
  - **A.**  $175 cm^3$
  - **B.** 245 cm<sup>3</sup>
  - C.  $490 \text{ cm}^3$
  - **D.**  $735 cm^3$

[2020-DSE-MATHS 2-16]

# Percentage Change in Mensuration

- 1. If the height and the base diameter of a cone are doubled, the new volume of the cone will
  - A. 2 times the original volume.
  - **B.**  $2\pi$  times the original volume.
  - C. 4 times the original volume.
  - **D.**  $4\pi$  times the original volume.
  - E. 8 times the original volume.

[SP-CE-MATHS 2-35]

- 2. If the length of a rectangle is increased by 10% and the width decreased by 10%, which of the following is true?
  - Its area remains the same.
  - Its area is decreased by 1%.
  - C. Its area is increased by 1%.
  - **D.** Its area is decreased by 10%.
  - Its area is increased by 10%.

[1980-CE-MATHS 2-13]

- 3. If the surface area of a spherical soap bubble increases by 44%, its volume increases by
  - **A.** 20%.
  - В. 33.1%.
  - C. 60%.
  - D. 66%.
  - E. 72.8%.

[1981-CE-MATHS 2-15]

- 4. Some air escapes from a spherical balloon of volume  $a^3$ . The balloon keeps its spherical shape and is now of volume  $b^3$ . What is the percentage decrease in the radius?
  - A.  $\frac{a-b}{a} \times 100\%$
  - **B.**  $\frac{a-b}{b} \times 100\%$
  - C.  $\sqrt[3]{\frac{a^3-b^3}{a^3}} \times 100\%$
  - **D.**  $\sqrt[3]{\frac{a^3-b^3}{b^3}} \times 100\%$
  - **E.**  $\frac{a^3-b^3}{a^3} \times 100\%$

[1982-CE-MATHS 2-15]

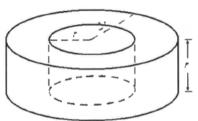
- 5. A solid sphere is cut into two hemispheres. The percentage increase in the total surface area is
  - 25%. A.
  - $33\frac{1}{3}\%$ .
  - 50%.
  - D. 75%.
  - E. 100%.

[1983-CE-MATHS 2-45]

- 6. The length and the width of a cuboid are each increased by 10% and the height remains The percentage increased in unchanged. volume is
  - A. 10%.
  - **B.** 20%.
  - C. 21%.
  - **D.** 24%.
  - 33%.

[1985-CE-MATHS 2-42]

7. A cylindrical hole of radius r is drilled through a solid cylinder, base radius 2r and height r, as shown in the figure. percentage increase in the total surface area is



- **A.** 0%.
- $16\frac{2}{3}\%$
- C. 20%.
- D. 25%.
- E.  $33\frac{1}{3}\%$ .

[1988-CE-MATHS 2-45]

- 8. A blanket loses 10% of its length and 8% of its width after washing. The percentage loss in area is
  - A. 18.8%.
  - В. 18%.
  - C. 17.2%.
  - 9%.
  - 8%.

[1991-CE-MATHS 2-11]

- 9. The length of a rectangle is decreased by 20%. If the area remains unchanged, find the percentage increase of its width.
  - **A.**  $1\frac{1}{4}\%$
  - **B.**  $12\frac{1}{2}\%$
  - C.  $16\frac{2}{3}\%$
  - D. 20%
  - E. 25%

[1996-CE-MATHS 2-43]

- 10. The length of a rectangle is decreased by 20% but its breadth is increased by k%. If the area of the rectangle remains unchanged, find the value of k.
  - A. 20
  - **B.** 25
  - C. 75
  - **D.** 80

[2011-CE-MATHS 2-11]

# **HKDSE Problems**

- 11. If the length and the width of a rectangle are increased by 20% and x% respectively so that its area is increased by 50%, then x =
  - A. 20.
  - B. 25.
  - C. 30.
  - D. 35.

[SP-DSE-MATHS 2-12]

- 12. If the circumference of a circle is increased by 40%, then the area of the circle is increased by
  - **A.** 18%.
  - **B.** 20%.
  - C. 40%.
  - D. 96%.

[PP-DSE-MATHS 2-11]

- 13. If the angle and the radius of a sector are decreased by x% and 50% respectively so that its area is decreased by 90%, then x =
  - **A.** 20.
  - **B.** 40.
  - C. 60.
  - **D.** 80.

[2014-DSE-MATHS 2-10]