## Hong Kong Certificate of Education Examination Mathematics Paper 1

## General Marking Instructions

- It is very important that all markers should adhere as closely as possible to the marking scheme. In
  many cases, however, candidates will have obtained a correct answer by an alternative method not
  specified in the marking scheme. In general, a correct answer merits all the marks allocated to that
  part, unless a particular method has been specified in the question. Makers should be patient in
  marking alternative solutions not specified in the marking scheme.
- In the marking scheme, marks are classified into the following three categories:

'M' marks
'A' marks

awarded for correct methods being used; awarded for the accuracy of the answers;

Marks without 'M' or 'A'

awarded for correctly completing a proof or arriving at an answer given in a question.

In a question consisting of several parts each depending on the previous parts, 'M' marks should be awarded to steps or methods correctly deduced from previous answers, even if these answers are erroneous. However, 'A' marks for the corresponding answers should NOT be awarded (unless otherwise specified).

- 3. For the convenience of markers, the marking scheme was written as detailed as possible. However, it is still likely that candidates would not present their solution in the same explicit manner, e.g. some steps would either be omitted or stated implicitly. In such cases, markers should exercise their discretion in marking candidates' work. In general, marks for a certain step should be awarded if candidates' solution indicated that the relevant concept/technique had been used.
- 4. Use of notation different from those in the marking scheme should not be penalized.
- In marking candidates' work, the benefit of doubt should be given in the candidates' favour.
- Marks may be deducted for wrong units (u) or poor presentation (pp).
  - a. The symbol (u-) should be used to denote 1 mark deducted for u. At most deduct 1 mark for u for the whole paper.
  - b. The symbol pp-D should be used to denote 1 mark deducted for pp. At most deduct 2 marks for pp for the whole paper. For similar pp, deduct 1 mark for the first time that it occurs. Do not penalize candidates twice in the paper for the same pp.
  - c. At most deduct 1 mark in each question. Deduct the mark for u first if both marks for u and pp may be deducted in the same question.
  - d. In any case, do not deduct any marks for pp or u in those steps where candidates could not score any marks.
- Marks entered in the Page Total Box should be the NET total scored on that page.
- 8. In the marking scheme, 'r.t.' stands for 'accepting answers which can be rounded off to', 'f.t.' stands for 'follow through' and 'or equivalent' means 'accepting equivalent forms of the equation which may have not been simplified but without uncollected like terms'. Steps which can be skipped are shaded whereas alternative answers are enclosed with rectangles or (brackets). All fractional answers must be simplified.

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|   | Solution  | Marks                | Remarks   |
|---|---|----------------------|---|
| 1. When $C = 30$ , $30 = \frac{5}{9}(F - 32)$                       |   | IM                   | substituting $C = 30$   |
| , ,   | (or 270 = 5E ÷ 160.)  | ΪA                   | removing brackets   |
| $\frac{30 \times 9}{5} = F - 32$ $F = 86$                           |   | 1A                   |   |
| $C = \frac{5}{9}(F - 32)$ $F = \frac{9}{5}C + 32$                   | (or g(= 5F €160)  | IA                   | removing brackets   |
| When $C = 30$ ,<br>$F = \frac{9}{5} \times 30 + 32$                 |   | IM                   | substituting $C = 30$   |
| F = 86  |   | IA                   |   |
| 2. $\frac{x^{-1}y}{x^2} = \frac{y}{x^{2}x^{2}}$ $= \frac{y}{x^{5}}$ | (ar. 122)<br>(ar. 127)  | (3)  1M  1M  1A  (3) | applying $a^{-4i} = \frac{1}{a^m}$ applying $a^m a^n = a^{m+n}$           |
| 3. Area of the sector   | $= \frac{75}{360} (6^2 \pi) \text{ cm}^2$ $\approx 23.6 \text{ cm}^2  \text{(or } 7\frac{1}{2}\pi \text{ cm}^2\text{)}$ | 1M+1A                | 1M for ratio or area of circle r.t. 23.6 or $\frac{15}{2}\pi$ , 7.5 $\pi$ |
|   | $=\frac{1}{2}\times6^2\times\frac{75}{180}\pi$ cm <sup>2</sup>  | IM+IA                | IM for $\frac{1}{2}r^2\theta$ or correct value of $\theta$                |
| <u> </u>  | $\approx 23.6 \text{ cm}^2  (\text{or } 7\frac{1}{2}\pi \text{ cm}^2)$  | <u> </u>             | r.t. 23.6 or $\frac{15}{2}\pi$ , $7.5\pi$                                 |
|   |   | (3)                  | 6 cm 75°  |
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|------|---|---------------------------|---|
| _    | Solution  | Marks                     | Remarks   |
| 4.   | $a^{2} + 7^{2} = 10^{2}$ (or $a = \sqrt{10^{2} - 7^{2}}$ )<br>$a = \sqrt{51}$ (or 7.14)<br>$\cos x^{o} = \frac{7}{10}$ (or $\sin x^{o} = \frac{\sqrt{51}}{10}$ , $\tan x^{o} = \frac{\sqrt{51}}{7}$ )<br>x = 45.6 | 1A<br>1A<br>1M<br>1A      | r.t. 7.14  r.t. 45.6, $u-1$ for $v \approx 45.6^\circ$ ,  |
|      | $\cos x^{\circ} = \frac{7}{10}$<br>$x \approx 45.6$<br>$a \approx 10 \sin 45.6^{\circ}$ (or $a \approx 7 \tan 45.6^{\circ}$ )<br>$a \approx 7.14$   | IA<br>IA<br>IM<br>IA      | $x \approx 45^{\circ}34^{\circ}, x^{\circ} \approx 45.6^{\circ}, x^{\circ} \approx 45.6$ 10 cm $a \text{ cm}$ |
| i,   | $\frac{11-2x}{5} < 1$ $11-2x < 5 \qquad \text{(or } \frac{11}{5} - \frac{2}{5}x < 1 \text{)}$ $-2x < -6$ $2x > 6 \qquad \text{(or } 6 < 2x, \frac{2}{5}x > \frac{6}{5} \text{)}$ $x > 3$                          | (4)                       | For any 2 of these 3 steps, !A for each. 2 of these 3 steps can be omitted.                                   |
|      | -5 -4 -3 -2 -1 0 t 2 · 3 4 5  | )<br>— <u>IM</u> —<br>(4) | or  |
| i.   | f(-3) (or $2(-3)^3 + 6(-3)^2 - 2(-3) - 7$ )<br>= -1<br>: The remainder is -1.   | 2A<br>1A                  |   |
|      | $ \begin{array}{r} 2+0-2 \\ 1+3 \overline{\smash{\big)}2+6-2-7} \\ 2+6 \\ \hline -2-7 \\ -2-6 \\ \hline -1 \\                                   $   | 5A                        |   |
|      | IVIIIIIIII1   | (3)                       |   |
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| Solu   | tion                   | Marks                 | Remarks  |
|--|------------------------|-----------------------|--|
| , x=25   |                        | 1 <b>A</b>            | $u-1$ for $x = 25^{\circ}$ , $x^{\circ} = 25^{\circ}$  |
| $\therefore \angle ADB = x^{0}$ $\therefore y = 180 - 56 - 25 - x$ $= 74$                          |                        | 1M<br>1M<br>1A<br>(4) | applying $\angle s$ in same segment $u-1$ for $y = 74^\circ$ , $y^\circ = 74^\circ$ $y^\circ = 74^\circ$ |
| Actual area = $220 \times 5000^{2}$ cm <sup>2</sup><br>$5000^{2}$<br>= $550000$ m <sup>2</sup> (or | area in m² = 550 000 ) | 2M<br>FM<br>1A<br>(4) | for ×5000 <sup>2</sup> , ignore unit<br>for +100 <sup>2</sup> , pp-1 for not<br>handling units properly  |
| 9. (a) Slope of $L = \frac{4-0}{-4-6}$<br>= $-\frac{2}{5}$ (or                                     | -0.4)                  | 1A                    |  |
| (b) Equation of L:<br>$y = -\frac{2}{5}(x-6)$ (or $y = -\frac{2}{5}x + \frac{12}{5}$ (or           |                        | 1M                    | or equivalent  |
| (c) When $x = 0$ ,<br>$y = \frac{12}{5}$ . (o) $C = (0, \frac{12}{5})$ .                           |                        | 1M<br>1A              |  |
| C = (0, <del>3</del> ).  |                        | (5)                   |  |
|  |                        |                       |  |
|  |                        |                       |  |
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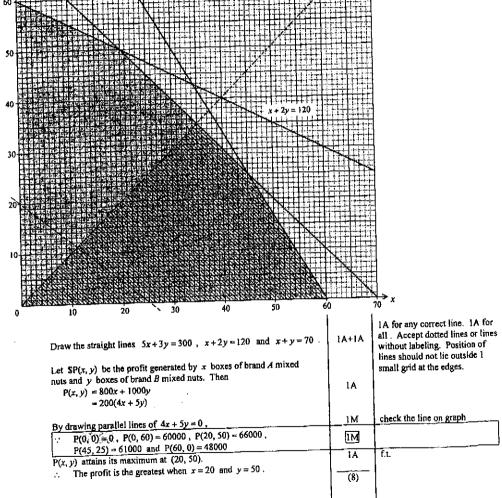
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|-------------|---|---|---------------------------|---|
|             | Soluti  | Marks   | Remarks                   |   |
| -<br>). (a) | $10x^{2} + 9x - 22 = 0$ $(x+2)(10x-11) = 0$ $x = -2 \text{ or } \frac{11}{10}$    | (or $x = \frac{-9 \pm \sqrt{9^2 + 4 \times 10 \times 22}}{2 \times 10}$ )<br>(or $x = -2$ or 1.1) | IA<br>LA                  |   |
|             | $r = -2$ or $\frac{10}{10}$   | <b>(</b> = = = = = .  | (2)                       |   |
| (b)         |   |   | IM+1A                     | 1M for 10000(1+1%) <sup>2</sup>   |
|             | [10000(1+r%)+9000](1+r%)  | - 22000   | [MHIA                     | 1M for 10000(1+r%)+9000   |
|             | $10(1+r\%)^2+9(1+r\%)-22=0$   | (or $r^2 + 290r - 3000 = 0$ ,<br>$10(r\%)^2 + 29(r\%) - 3 = 0$ )                                  | lM                        | pp-1 for confusing r with r%  for choosing '+ve' value from '+ve' and 1 '-ve' roots, provid |
|             | From (a), $1+r\%=1.1$   |   |                           | that the original equation must correct   |
|             | r = 10  |   | <u> A</u><br>(4)          |   |
| l. (a)      | ) Missing value in 1st table = 66<br>Missing value in 2nd table = 20              |   | 1A<br>— <u>1A</u><br>—(2) |   |
| (b          | An estimate of the mean  210×3+230×13+260×30+  75  255 seconds                    | 270×20 # 290×9 (seconds)  | 1M<br>1A                  | r.t. 255  |
| (c          | ) Median ≈ 254 seconds  | ( or 255 seconds )  | <u>iA</u> (1)             | r.t. 254 or 255   |
| (d          | Number of songs have length<br>but not greater than 260 seco<br>= 13 + 30<br>= 43 | s greater then 220 seconds<br>ands<br>(or 46 - 3)   | 1A                        |   |
|             | Percentage required = $\frac{43}{75} \times 10^{-10}$                             | 0%  |                           |   |
|             | ≈ 57.3%   | (or $57\frac{1}{3}\%$ )   | <u>IA</u>                 | r.t. 57.3   |
|             |   |   |                           |   |
|             |   |   |                           |   |
|             |   |   |                           |   |
|             |   |   |                           |   |
|             |   |   |                           |   |
|             |   |   | l                         | I   |

|          | Solution  |                     | Marks | Remarks       |
|----------|---|---------------------|-------|---------------|
| (a) Num  | nbers having two zero digits are 100,   | 200,, 900.          |       |               |
|          | pability required = 9   |                     | ĪΑ    | for numerator |
|          | • •   | 4.013               | lA    |               |
|          | 100   | (or 0.01)           | 10    |               |
| Pro      | bability required = $\frac{1}{10} \times \frac{1}{10}$  |                     | ĺΑ    |               |
|          | $=\frac{1}{100}$  | ( or 0.01 )         | [A    |               |
|          |   |                     | (2)   |               |
| (b) Nu   | mbers having no zero digits are   |                     | i     |               |
| • •      | 111, 112,, 119  | 911, 912,, 919      | 1     |               |
|          | 121, 122,, 129  | 921, 922,, 929<br>: |       |               |
|          | :<br>191, 192,, 199   | 991, 992,, 999      |       |               |
| Pro      | bability required = $\frac{9 \times 9 \times 9}{900}$   |                     | 1A    | for numerator |
|          | <u>81</u><br>100  | (or 0.81)           | 1A    |               |
| Pro      | obability required $=\frac{9}{10} \times \frac{9}{10}$  |                     | ΙĀ    |               |
|          |   | ( or 0.81 )         | ĪĀ    |               |
| <u> </u> | $=\frac{81}{100}$   | (01 0.51)           |       |               |
|          |   |                     | (2)   |               |
| (c) Nu   | Imbers having exactly one zero digit s 101, 102,, 109, 110, 120,, 201, 202,, 209, 210, 220,, : : 901, 902,, 909, 910, 920,, | 190<br>290          |       |               |
|          |   | , 170               |       | 6             |
| Pro      | obability required = $\frac{9 \times 9 + 9 \times 9}{900}$  |                     | 14    | for numerator |
|          | = 9/50  | (or 0.18)           | 1A    |               |
| Pt       | robability required = $1 - \frac{1}{100} - \frac{81}{100}$  |                     | [M]   |               |
|          | = 9/50  | (or 0.18)           | ĨA.   |               |
| Pi       | robability required = $\frac{1}{10} \times \frac{9}{10} \times 2$   |                     | 1A    |               |
|          | $=\frac{9}{50}$   | (or 0.18)           | IA    |               |
| L        |   |                     | (2)   |               |
|          |   |                     |       |               |
|          |   |                     |       | 1             |

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|---------|---|--|----------------------|
|         | Solution  | Marks                                  | Remarks              |
| 13. (a) | Size of each interior angle of the pentagon = $\frac{(5-2)\times180^{\circ}}{5}$ = $\frac{108^{\circ}}{5}$              | IA                                     | <u></u>              |
|         | $\angle BCG = 108^{\circ} - 90^{\circ} = 18^{\circ}$  | 1A                                     | 6                    |
|         | $\angle CBG = \frac{180^{\circ} - 18^{\circ}}{2} = 81^{\circ}$  | IM.                                    | B F E                |
|         | $ \begin{array}{l} 2 \\ \angle ABP = 108^{\circ} - 81^{\circ} = 27^{\circ} \end{array} $                                | 1A                                     | $  \setminus   $     |
|         | $\angle APB = 180^{\circ} - 27^{\circ} - 108^{\circ} = 45^{\circ}$  | IA                                     | \                    |
|         |   | (5)                                    | \                    |
| (L)     | $\therefore \frac{AP}{\sin 27^{\circ}} = \frac{AB}{\sin 45^{\circ}}$  |  |                      |
| (0)     |   |  |                      |
|         | $\therefore AP = \frac{\sin 27^{\circ}}{\sin 45^{\circ}} AB$  |  |                      |
|         |   |  |                      |
|         | $= \frac{\sin 27^{\circ}}{\sin 45^{\circ}} AE \qquad (or \frac{AP}{\sin 27^{\circ}} = \frac{AE}{\sin 45^{\circ}} etc.)$ | IM                                     |                      |
|         | $\approx 0.642 AE$ (or $AE \approx 1.56 AP$ )   |  | l d.p. is sufficient |
|         | $\therefore$ AP is longer than PE.  | (3)                                    |                      |
|         |   | ()                                     | :                    |
|         |   | ' ــــــــــــــــــــــــــــــــــــ |                      |
|         |   |  |                      |
|         | 3rd row   | 13 22                                  | A10066               |
|         | 2nd re  |  | 19 42                |
|         |   | st row                                 | 20                   |
| 14 (4)  | Number of seats in the last row = $20 + 2(50 - 1)$  | 1A                                     |                      |
| 14. (2) | - 118   | _1A_                                   |                      |
|         |   | (2)                                    |                      |
|         | 7/3 20.2/ 19  | ,,                                     |                      |
| (b)     | <b>2</b> ·  | lA.                                    |                      |
|         | $= n^2 + 19n$   |  |                      |
|         | If $n^2 + 19n = 2000$ , then (or $n^2 + 19n \ge 2000$ )   | 1M                                     |                      |
|         | $n^{2} + 19n - 2000 = 0$ $n = \frac{-19 \pm \sqrt{19^{2} - 4(-2000)}}{2}$   |  |                      |
|         | $-19 \pm \sqrt{19^2 - 4(-2000)}$  |  |                      |
|         | $n = \frac{1}{2}$   | -                                      |                      |
|         | $n = 36.2 \text{ or } -55.2 \qquad (\text{or } n \approx 36.2 \text{ only})$  | 1A                                     | r.t. 36.2, -55.2     |
|         | The seat numbered 2000 can be found in the 37th row.  | 1A                                     |                      |
|         | Let $f(n) = n^2 + 19n$ .  |  |                      |
|         | ∴ f(36) = 1980  | } [M+[A                                |                      |
|         | f(37) = 2072<br>∴ The seat numbered 2000 can be found in the 37th row.  | I IA                                   |                      |
|         | The seat numbered 2000 can be found in the 37th tow.  |  |                      |
|         |   | (4)                                    |                      |
|         |   |  |                      |
|         |   |  |                      |
|         |   |  | i                    |

| Solution   | Marks          | Remarks                      |
|--|----------------|------------------------------|
| 15. (a) $x$ and $y$ satisfy the following conditions:<br>$1000(40x) + 800(30y) \le 2400000$ or $5x + 3y \le 300$<br>$1000(10x) + 800(25y) \le 1200000$ or $x + 2y \le 120$<br>$x + y \le 70$<br>$x + 3y \le 120$ | IA<br>1A<br>1A | Withhold I mark for any "<". |
| у <sub>ф</sub>   |                | ·<br>====                    |



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|-----|---|-----------------------|----------------------------------|--|--|--|
|     | Solution  | Marks                 | Remarks                          |  |  |  |
| (b) | In addition to the conditions in (a), $x$ , $y$ should also satisfy $y < x$ . The feasible solution becomes the shaded region.  | 1 <b>A</b>            | or drawing $y = x$ in the figure |  |  |  |
| (b) | In addition to the conditions in (a), $x$ , $y$ should also satisfy $y < x$ . The feasible solution becomes the shaded region.  By considering lines parallel to $4x + 5y = 0$ (or testing points). $P(x, y)$ attains its maximum at (36, 34).  The greatest profit is \$62800. | 1A<br>1A<br>1A<br>(3) | or drawing $y = x$ in the figure |  |  |  |
|     |   |                       |                                  |  |  |  |

| Refer to Figure 9A   |                        | 25.10   | / DIT (20)   | TON TEACH              | . ,   |   |
|--|------------------------|---|--|------------------------|-------|---|
| Figure 9A   Figure 9B   (tangent 1 radius)   (tangent properties)   (切線仕事で)   (切線仕事で)   (切線仕事で)   (切線仕事で)   (切線仕事で)   (世級代事で)   (世級代 |                        |   | Solution   |                        | Marks | Remarks                                 |
| Figure 9A  Figure 9B  Figure 9A  (L1) ∠OPC = 90°  (L2) ∠PCO = 180° - 90° - 30° = 60° (∠ sum of Δ)  (L3) ∠PQO = ½ ∠PCO = 30°  (L4) ∠OPC = 90°  (L5) ∠OPC = 90°  (L5) ∠OPC = 90°  (L5) ∠PCO = 180° - 90° - 30° = 60° (∠ sum of Δ)  (L5) ∠OPC = 90°  (L5) ∠OPC = 90°  (L5) ∠PCO = 180° - 90° - 30° = 60° (∠ sum of Δ)  (L6) ∠OPC = 90°  (L5) ∠PCO = 180° - 90° - 30° = 60° (∠ sum of Δ)  (L7) ∠ CPQ = ∠CQP = x (base ∠s of isos. Δ)  (L9) x = 30°  Refer to Figure 9B, and let ∠CQP = x (∠ in alt. segment)  (L1) ∠ TPQ = ∠CQP = x (∠ in semicircle)  (L1) ∠ TPQ = 90°  (L2) ∠ TPQ = √CQP = x (∠ in alt. segment)  (L1) ∠ TPQ = 90°  (L1) ∠ TPQ = 90°  (L1) ∠ TPQ = 90°  (L2) ∠ TPQ = √CQP = x (∠ in semicircle)  (L1) ∠ TPQ = 90°  (L1) ∠ TPQ = 90°  (L2) ∠ TPQ = √CQP = x (∠ in alt. segment)  (Δ) ∠ TPQ = √CQP = x (∠ in alt   | 5                      | \$\langle \langle \lang | 1) [   | \$ 5                   |       |   |
| (L1)   | 0 120                  | Figure 9/   | 0  | — Р                    |       |   |
| (L2)   | (a) Refer to E<br>(L1) | Figure 9A, $\angle OPC = 90^{\circ}$  |  | (tangent 1 radius)     |       | (tangent properties)<br>[切線1半徑]、[切線性質/定 |
| (L4) ∠OPC = 90° (tangent ⊥ radius) (tangent properties) (切線上年極」、「切線性質/理]  (L5) ∠PCO = 180° - 90° - 30° = 60° (∠ sum of △) (五内角和]  (L6) ∠CPQ = ∠CQP = x (base ∠s of isos. △) (李腰△底角]  (L8) 2x = ∠PCO = 60° (ext. ∠ of △) (上9) x = 30°  Refer to Figure 9B, and let ∠CQP = x (∠ in alt. segment) (上10) ∠TPO = ∠CQP = x (∠ in alt. segment) (上11) ∠TPQ = 90° (∠ in semicircle) (上12) ∴ 30° + 90° + 2x = 180° (∠ sum of △) (□A角和]  Marking Scheme:  Case 1 Any correct proof with correct reasons. 3  Case 2 Any correct proof without reasons. 1 At most 2 marks  |                        |   |  |                        |       |   |
| (L5)   | 1                      |   | let $\angle CQP = x$ .   | (tangent 1 radius)     |       | [切線工半徑]、[切線性質/定                         |
| (L7)   |                        | and the second s  | were the transport of the California's Colors and Citizen's  | ° (∠ sum of Δ)         | Angel | 1                                       |
| (L1)   | r                      |   | - March Color of the Color of t |                        | 37    | 「等腰∆底角!                                 |
| Refer to Figure 9B, and let ∠CQP = x. (L10) ∠TPO = ∠CQP = x (∠ in alt. segment)  (L11) ∠TPQ = 90° (∠ in semicircle) (L12) ∴ 30° + 90° + 2x = 180° (∠ sum of Δ)  (L13) x = 30°  Marking Scheme:  Case 1 Any correct proof with correct reasons.  In addition, any relevant correct argument with correct reason (at most 1 mark).  Case 3 Any relevant correct argument with correct reason.  1 At most 1 mark  At most 1 mark  | 1.                     |   |  | •                      |       | 1                                       |
| Refer to Figure 9B, and let ∠CQP = x.  (L10) ∠TPO = ∠CQP = x (∠ in alt. segment)  (L11) ∠TPQ = 90° (∠ in semicircle)  (L12) ∴ 30° + 90° + 2x = 180° (∠ sum of △)  (L13) x = 30°  Marking Scheme:  Case 1 Any correct proof with correct reasons.  In addition, any relevant correct argument with correct reason  (at most 1 mark).  Case 3 Any relevant correct argument with correct reason.  1 At most 1 mark   | 1' '                   |   |  | ·                      |       |   |
| (L10) ∠TPO = ∠CQP = x (∠ in alt. segment) [交鳍弓形的圓周角]、[纺灯定理]  (L11) ∠TPQ = 90° (∠ in semicircle) [华圓上的圓周角]  (L12) ∴ 30° + 90° + 2x = 180° (∠ sum of Δ) [△内角和]  (L13) x = 30°  Marking Scheme:  Case 1 Any correct proof with correct reasons. 3  Case 2 Any correct proof without reasons. 1  In addition, any relevant correct argument with correct reason (at most 1 mark). At most 2 marks  Case 3 Any relevant correct argument with correct reason. 1 At most 1 mark  |                        |   | let /COP = r   |                        |       |   |
| (L12) : 30° + 90° + 2x = 180° (∠ sum of △) [△内角和]  (L13) x = 30°  Marking Scheme:  Case 1 Any correct proof with correct reasons. 3  Case 2 Any correct proof without reasons. 1 In addition, any relevant correct argument with correct reason 1 At most 2 marks (at most 1 mark).  Case 3 Any relevant correct argument with correct reason. 1 At most 1 mark  |                        |   |  | (∠ in alt. segment)    |       | [交錯弓形的圓周角]、[弦切<br>定理]                   |
| (L12) : 30° + 90° + 2x = 180° (∠ sum of △) [△內角和]  (L13) x = 30°  Marking Scheme:  Case ! Any correct proof with correct reasons. 3  Case 2 Any correct proof without reasons. 1  In addition, any relevant correct argument with correct reason (at most 1 mark).  Case 3 Any relevant correct argument with correct reason. 1 At most 1 mark   | (L11)                  | $\angle TPQ = 90^{\circ}$   | •  | (∠ in semicircle)      |       | [半圓上的圓周角]                               |
| Marking Scheme:  Case 1 Any correct proof with correct reasons. 3  Case 2 Any correct proof without reasons. 1  In addition, any relevant correct argument with correct reason 1 At most 2 marks (at most 1 mark).  Case 3 Any relevant correct argument with correct reason. 1 At most 1 mark   | (L12)                  | ∴ 30° + 90  | $0^{\circ} + 2x = 180^{\circ}$   | (∠ sum of ∆)           |       | [△ <b>内角</b> 和]                         |
| Case 1 Any correct proof with correct reasons.  Case 2 Any correct proof without reasons.  In addition, any relevant correct argument with correct reason (at most 1 mark).  Case 3 Any relevant correct argument with correct reason.  1 At most 1 mark  At most 1 mark   | (L13)                  | x = 30°   | _,   |                        |       |   |
| Case 1 Any correct proof with correct reasons.  Case 2 Any correct proof without reasons.  In addition, any relevant correct argument with correct reason (at most 1 mark).  Case 3 Any relevant correct argument with correct reason.  1 At most 1 mark  At most 1 mark   | Marki                  | ng Scheme :   |  |                        |       |   |
| In addition, any relevant correct argument with correct reason 1 At most 2 marks (at most 1 mark).  Case 3 Any relevant correct argument with correct reason. 1 At most 1 mark   |                        |   | proof with correct   | reasons.               |       |   |
| Case 3 Any relevant correct argument with correct reason. 1 At most I mark   | Case 2                 | In addition,  | any relevant corre   |                        |       | At most 2 marks                         |
| Case 3 Any reterant correst against  | Core 3                 |   |  | t with correct reason. | 1     | At most I mark                          |
| (3)  | Case 3                 | Ally Icicvan  | ir correct at Battlett   |                        |       | -                                       |
|  |                        |   |  |                        | (3)   |   |

|   |            | Remarks                           |
|---|------------|-----------------------------------|
| (b) (i)   |            |                                   |
| (L14) $\angle ROQ = \angle QOP = 30^{\circ}$ (tangents from ext. pt.)                           |            | (tangent properties)<br>[切線性質/定理] |
| (L15) ∠PQO = 30° (proved)   | ı          |                                   |
| (L16) : $\angle RQP + \angle POR = 180^{\circ}$ (opp. $\angle s$ of cyclic quad.)               |            | [圓內接四邊形的對角]                       |
| (L17) $\angle CQR = 180^{\circ} - 3 \times 30^{\circ} = 90^{\circ}$                             |            |                                   |
| (L18) Hence RQ is tangent to circle (conv. of tangent 1 radius).  PQS at Q.                     |            | [切錄上字徑的逆定理]                       |
| Marking Scheme :  | 1.4.4      | -                                 |
| Case I Any correct proof with correct reasons.  | 3          |                                   |
| Case 2 Any correct proof without reasons.   | 1          |                                   |
| In addition, any relevant correct argument with correct reason (at most 1 mark).                | 1          | At most 2 marks                   |
| Case 3 Any relevant correct argument with correct reason.                                       | 1          | At most 1 mark                    |
|   | (3)        |                                   |
| (b) (ii) $\therefore$ Slope of $OC = \frac{4}{3}$   |            |                                   |
| 3   | ŧΜ         |                                   |
| $\therefore  \text{Slope of } QR = -\frac{3}{4}$  | ( IVI      |                                   |
| $OC = \sqrt{6^2 + 8^2} = 10$  | 1 <b>A</b> |                                   |
| $\overrightarrow{CQ} \stackrel{\triangle}{=} CP = OC \sin 30^{\circ} \stackrel{\triangle}{=} 5$ | IM         |                                   |
| Let the coordinates of $Q$ be $(x, y)$ .  |            |                                   |
| OC: CQ = 10:5 = 2:1   |            |                                   |
| $\therefore \frac{2x+1(0)}{3}=6 \text{ and } \frac{2y+1(0)}{3}=8$                               | 1M         |                                   |
| Equation of circle: $(x-6)^2 + (y-8)^2 = 25$  |            |                                   |
| $x^2 + y^2 - 12x - 16y + 75 = 0$ (1)  |            |                                   |
| Equation of <i>OC</i> : $y = \frac{4}{3}x$ (2)  |            |                                   |
| Solving (1) and (2), $x^2 - 12x + 27 = 0$ (or $y^2 - 16y + 48 = 0$ )                            |            |                                   |
| x = 3 (rej.) or 9 (or $y = 4$ (rej.) or 12)<br>x = 9 and $y = 12$                               | 1M         | must reject the smaller root      |
| x = y and $y = 12$  |            |                                   |
| Hence the equation of $QR$ is   |            |                                   |
| $\frac{y-12}{y-9} = -\frac{3}{4}$   |            |                                   |
| 2 2 1   |            |                                   |
| $3x+4y-75=0$ (or $y=-\frac{3}{4}x+\frac{75}{4}$ )   | _IA_       |                                   |
| ,   | (5)        |                                   |
| 1   |            |                                   |
| •   |            |                                   |
| ļ   |            |                                   |
|   |            |                                   |
|   |            |                                   |
|   |            |                                   |

| Solution   | Marks                   | Remarks   |
|--|-------------------------|---|
| (a) (i) $AD = \frac{h}{\sin 30^{\circ}} \text{ m} = 2h \text{ m}$  | 1A                      | u−1 for missing unit                                      |
| $BD = \frac{h+10}{\sin 60^{\circ}} \text{ m} \neq \frac{2}{\sqrt{3}} (h+10) ; \text{m} = \frac{2\sqrt{3}}{3} (h+10) \text{ m}$   | 1 <b>A</b>              |   |
| (ii) $AB^2 = 10^2 + 10^2 \text{ (m}^2\text{)}$   | 1A                      | or $AB = \sqrt{200}$ , $\frac{10}{\sin 45^{\circ}}$ m etc |
| By cosine law,<br>$AB^2 = AD^2 + DB^2 - 2(AD)(DB) \cos \angle ADB$   |                         | •   |
| $200 = \left(\frac{h}{\sin 30^{\circ}}\right)^{2} + \left(\frac{h+10}{\sin 60^{\circ}}\right)^{2} - 2\left(\frac{h}{\sin 30^{\circ}}\right)\left(\frac{h+10}{\sin 60^{\circ}}\right)\cos 30^{\circ}$ | 1M+IA                   | Do not accept setting $AD = BE$                           |
| $200 = 4h^2 + \frac{4}{3}(h+10)^2 - 4h(h+10)$  |                         |   |
| $h^2 - 10h - 50 = 0$   | 1A                      | or multiples  |
| h = 13.660 or $-3.660$   |                         | or 5±5√3  |
| h ≈ 13.7 or -3.66 (rejected)   | 1A                      | or h≈ 13.7 only   |
| $5+5\sqrt{3}$ or $5-5\sqrt{3}$ (rejected)  |                         |   |
| Vertical 30° 60° D   | (7)                     |   |
| (b) $AC = 2(10 \sin 10^\circ)$ (m) $\sqrt{10^2 + 10^2 - 2(10)(10)\cos 20^\circ}$ (m) $\approx 3.47296$ (m) $AE = \frac{h}{\sin 25^\circ}$ (m) $\approx 32.3$ (m)                                     | 1A                      |   |
| By sine law, $\sin \angle ACE = \frac{AE \sin 5^{\circ}}{AC}$  |                         |   |
| AC hsin 5°   |                         |   |
| ≈ <del>738115</del><br>20 sin 10° sin 25°  | 1 <b>M</b>              |   |
| $\therefore \angle ACE = 54.2^{\circ} \text{ or } 126^{\circ} \frac{54^{\circ}13' \text{ or } 126^{\circ}}{54^{\circ}13' \text{ or } 126^{\circ}}$   | . <b>iA+</b> 1A.<br>(4) | r.t. <b>54.2</b> , 126                                    |
|  |                         |   |
|  |                         | i   |

|       |  |            | S   | olution                                  | ·  | Marks    | Remarks  |
|-------|--|------------|---|--|--|----------|--|
| 18. ( | (a) Let $V = ah^2 + bh^3$ where $a$ , $b$ are non-zero constants. Then $\begin{cases} \frac{29}{3}\pi = a + b & \begin{cases} a + b = \frac{29}{3}\pi \end{cases} & \dots & (1) \\ 81\pi = 9a + 27b & \begin{cases} a + b = \frac{29}{3}\pi \end{cases} & \dots & (2) \end{cases}$ |            |   |  | And the second s | IA<br>IM |  |
|       |  |            | (2) – (1) gives $2b = -$  | $\frac{2}{3}\pi$                         |  |          |  |
|       |  |            | Hence $b = -\frac{\pi}{3}$ and  | a = 10π                                  |  | 1A       |  |
|       |  | <i>:</i> . | $V = 10\pi h^2 - \frac{\pi}{3}h^3$  |  | P. h cm  | <b> </b> |  |
|       |  |            | 3   |  |  | (3)      |  |
|       |  |            |   |  | 0  | :        |  |
| (     | (b)  | (i)        | Surface area = $2x \times 10^3$<br>$\approx 628 \text{ cm}^3$                     |  | :m² )  | 1A       | r.t. 628   |
|       |  | 6i)        | ∵ Volume of hemisp  | where $=\frac{2}{\pi} \times 10^3$ (c    | :m³)   | 1A       |  |
|       |  | 12         | $\therefore \frac{2}{3}\pi \times 10^3 - 2V =$                                    | -  |  |          |  |
|       |  |            |   | $\frac{\pi}{3} h^3 = \frac{1400}{3} \pi$ |  | · IM     |  |
|       |  |            | $\frac{2}{3}\pi(1000-30h^2)$  | $+h^3-700)=0$                            |  |          |  |
|       |  |            | $3 - 30h^2 + 300 =$   |  |  | 1        |  |
|       |  |            | From the graph in   | Figure 11.3,                             | (4 Setos)  | ĬМ       | or claiming to draw $y = -300$ , writing $h \approx 3.35$ , $h \approx 3.4$ etc. |
|       |  |            | Let $f(h) = h^3 - 30h^2 +$  | 300 , then f(3.3) >                      | 0 and f(3.4) < 0.  |          |  |
|       |  |            | Using the method of bit   |  |  | 1        |  |
|       |  |            | Interval  | "mid-value"                              | f(h)   |          | use interval ⊆ [0, 5] containing the root as the starting interval               |
|       |  |            | 3.3 < h < 3.4   | 3.35                                     | +ve (0.9204)   | IM       | testing sign of "mid-value" or<br>any intermediate value                         |
|       |  |            | 3.35 < h < 3.4  | 3.375                                    | -ve (-3.2754)  | 1M       | choosing the correct interval  |
|       |  |            | 3.35 < h < 3.375  | 3.363                                    | -ve (-1.2583)  | 1        |  |
|       |  |            | 3.35 < h < 3.363  | 3.357<br>3.354                           | -ve (-0.2519)<br>+ve (0.2507)  |          |  |
|       |  |            | 3.35 < h < 3.357<br>3.354 < h < 3.357   | 3.356                                    | -ve (-0.0843)  |          |  |
|       |  |            | 3.354 < h < 3.356   | 3,355                                    | +ve (0.0832)   |          |  |
|       |  |            | . 3,355 < h < 3.356   |  | \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \  | 1        |  |
|       |  |            | h≈3.36 (correc  | t to 2 decimal places                    | 5)   | 1A       | f.t.   |
|       |  |            | Let $f(h) = h^3 - 30h^2 + \frac{1}{2}$  | -300 .                                   |  |          |  |
|       |  |            | $f(3,34) \approx 2.5917$<br>$f(3,35) \approx 0.9203$<br>$f(3,36) \approx -0.7549$ | f(3.355) ≈                               | 0.0832   | IM+IM    |  |
|       |  |            | f(3,37) =-2,4342  |  | •)   | [A       | £t.  |
|       |  |            | ∴ n ≈ 3.30 (correc  | t to 2 decimal place                     | »į   | U.Ci     |  |
|       |  |            |   |  |  | (8)      |  |
|       |  |            |   |  |  |          | I  |