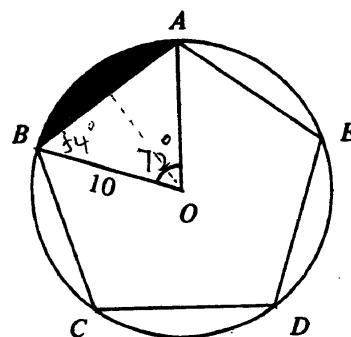


Solutions	Marks	Remarks
1. (a) $\frac{\pi}{6}$ (radian) (≈ 0.5236) (b) $x = 150^\circ (\frac{5\pi}{6}, 2.62)$ (c) $\cos A$	1A 1A 1A	
	<u>3</u>	
2. (a) $p + q$ (b) -2 (c) $\sqrt{3} - \sqrt{2} (1.732 - 1.414)$	1A 1A 1A	
	<u>3</u>	
3. (a) $y \geq \frac{1}{2}$ $2x - y \geq 2$ $3x + 5y \leq 30$ (b) 16	1A 1A 1A 1A	Withhold 1 mk if '=' omitted 16 is correct
	<u>4</u>	
4. (a) (i) $x^2 - 2x = x(x - 2)$ (ii) $x^2 - 6x + 8 = (x - 2)(x - 4)$ (b) $\frac{1}{x^2 - 2x} + \frac{1}{x^2 - 6x + 8} = \frac{1}{x(x - 2)} + \frac{1}{(x - 2)(x - 4)}$ $= \frac{(x - 4) + x}{x(x - 2)(x - 4)}$ $= \frac{2x - 4}{x(x - 2)(x - 4)}$ $= \frac{2}{x(x - 4)} \quad \left(= \frac{2}{x^2 - 4x} \right)$	1A 1A 1M 1A 1A 1A 1A	$x^2 - 2x \geq 0$ $\sqrt{x-2} \geq 0$ $x > 2$
	<u>5</u>	
5. (a) Slope of $L_2 = \frac{1}{2}$ Slope of $L_1 = -2$ Equation of $L_1 : y - 5 = -2(x - 10)$ i.e. $2x + y - 25 = 0$ (or $y = -2x + 25$) (b) Solving $\begin{cases} x - 2y + 5 = 0 \\ 4x + 2y - 50 = 0 \end{cases}$ $5x - 45 = 0$ $x = 9$ (or $y = 7$) $\therefore L_1$ and L_2 meet at (9, 7)	1A 1A 1M 1A 1M 1A 1A 1A 1A 1A 1A 1A	Pt-slope form Eliminating 1 unknown Accept $x = 9$, $y = 7$

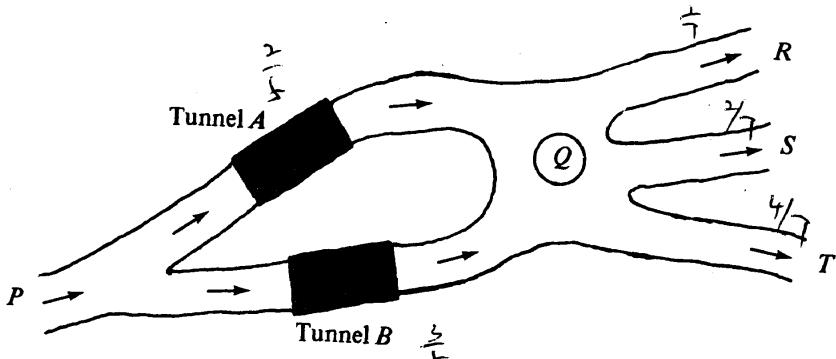
RESTRICTED PAPER

Solutions	Marks	Remarks
<p>6. For distinct real roots $\Delta = (2k)^2 - 4(k+6) > 0$ $4k^2 - 4k - 24 > 0$ $(k+2)(k-3) > 0$ $\therefore k < -2 \text{ or } k > 3$</p>	2M+1A 1A 2A <hr/> 6	1A for $(2k)^2 - 4(k+6)$ 2M for $\Delta > 0$ $(\Delta \geq 0, 1M \text{ only})$ For $(k+2)(k-3)$ For '., , '=' withhold 1 mk each $k < -2 \text{ and } k > 3$
<p>7. (a) $\angle AOB = \frac{360^\circ}{5} = 72^\circ \left(= \frac{2\pi}{5} \approx 1.26 \text{ radians} \right)$ Area of $\triangle OAB = \frac{1}{2}(10)(10)\sin 72^\circ$ $= 47.6$ (47.5528)</p>	1A 1M <hr/> 1A	Any figure roundable to 47.6
<p>(b) Area of sector $OAB = \frac{1}{5} \cdot \pi 10^2$ $= 20\pi$ (62.83) Area of shaded part = $20\pi - 47.55$ $= 15.3$ (15.2790)</p>	1A 1M <hr/> 1A <hr/> 6	Accept 15.2 ~ 15.3
<p>8. (a) Total score of the team = $70(m+n)$ (b) Total score is also equal to $75m + 62n$. $75m + 62n = 70(m+n)$ $5m = 8n$ $m : n = 8 : 5 \left(= \frac{8}{5} \right)$ (c) The number of men = $39 \times \frac{8}{8+5}$ $= 24$</p>	1A 1A 1M 1A 1M <hr/> 1A <hr/> 6	



Solutions	Marks	Remarks																								
9. (a) (i) Area of $OAPB = a \times b$ $= a(2a^2 - 4a + 3)$ $= 2a^3 - 4a^2 + 3a$	1A 1A																									
(ii) For $OAPB$ to be a square, $a = b$ or $a^2 = b$	1M	Equating adjacent sides																								
$a = 2a^2 - 4a + 3$ $2a^2 - 5a + 3 = 0$ $(2a - 3)(a - 1) = 0$ $\therefore a = \frac{3}{2}$ or 1	1A 1A+1A 6																									
(b) (i) If the area of $OAPB = \frac{3}{2}$, $2a^3 - 4a^2 + 3a = \frac{3}{2}$ $\therefore 4a^3 - 8a^2 + 6a - 3 = 0 \dots \dots \dots (*)$	1A																									
(ii) Let $f(a) = 4a^3 - 8a^2 + 6a - 3$ $f(1.2) < 0 (= -0.408)$ and $f(1.3) > 0 (= 0.068)$ $\therefore (*)$ has a root lying between 1.2 and 1.3	1A 1A 1A	$f(1.2) \cdot f(1.3) < 0$ Correct signs only																								
<table border="1"> <thead> <tr> <th>Interval</th> <th>Mid-value a_i</th> <th>$f(a_i)$</th> </tr> </thead> <tbody> <tr> <td>$1.2 < a < 1.3$</td> <td>1.25</td> <td>- (-0.1875)</td> </tr> <tr> <td>$1.25 < a < 1.3$</td> <td>1.275</td> <td>- (-0.0643)</td> </tr> <tr> <td>$1.275 < a < 1.3$</td> <td>1.2875 (etc)</td> <td>+ (+0.0007)</td> </tr> <tr> <td>$1.275 < a < 1.2875$</td> <td>1.28125</td> <td>- (-0.0321)</td> </tr> <tr> <td>$1.28125 < a < 1.2875$</td> <td>1.284375</td> <td>- (-0.01578)</td> </tr> <tr> <td>$1.284375 < a < 1.2875$</td> <td>1.2859375</td> <td>- (-0.00757)</td> </tr> <tr> <td>$1.2859375 < a < 1.2875$</td> <td></td> <td></td> </tr> </tbody> </table>	Interval	Mid-value a_i	$f(a_i)$	$1.2 < a < 1.3$	1.25	- (-0.1875)	$1.25 < a < 1.3$	1.275	- (-0.0643)	$1.275 < a < 1.3$	1.2875 (etc)	+ (+0.0007)	$1.275 < a < 1.2875$	1.28125	- (-0.0321)	$1.28125 < a < 1.2875$	1.284375	- (-0.01578)	$1.284375 < a < 1.2875$	1.2859375	- (-0.00757)	$1.2859375 < a < 1.2875$			1M+1A 1M 1M	1M for testing sign at mid-value Choosing correct interval
Interval	Mid-value a_i	$f(a_i)$																								
$1.2 < a < 1.3$	1.25	- (-0.1875)																								
$1.25 < a < 1.3$	1.275	- (-0.0643)																								
$1.275 < a < 1.3$	1.2875 (etc)	+ (+0.0007)																								
$1.275 < a < 1.2875$	1.28125	- (-0.0321)																								
$1.28125 < a < 1.2875$	1.284375	- (-0.01578)																								
$1.284375 < a < 1.2875$	1.2859375	- (-0.00757)																								
$1.2859375 < a < 1.2875$																										
$\therefore a = 1.29$ (corr. to 2 d.p.)	1A 6	Check last interval, $a = 1.2874$																								

RESTRICTED 内部文件

Solutions	Marks	Remarks
10. (a) The probabilities that a car leaving P will		
(i) pass through B = $1 - \frac{2}{5} = \frac{3}{5}$ (= 0.6) (P_1)	1A	
(ii) not arrive at T = $1 - \frac{4}{7} = \frac{3}{7}$ (= 0.429)	1A	$\frac{1}{7} + \frac{2}{7}$
(iii) arrive at R through Tunnel B = $\frac{3}{5} \times \frac{1}{7}$ = $\frac{3}{35}$ (= 0.0857)	1M 1A	$P_1 \times \frac{1}{7}$ \uparrow $\circ < \text{題意} < 1$
(iv) pass through Tunnel A but not arrive at R = $\frac{2}{5} \times (1 - \frac{1}{7})$ = $\frac{12}{35}$ (= 0.343)	1A 1A 6	$\frac{2}{5} \times \frac{2}{7} + \frac{2}{5} \times \frac{4}{7}$
(b) (i) The probability that the first one will arrive at R and the second one at S		
$S = \frac{1}{7} \times \frac{2}{7} = \frac{2}{49}$ (= 0.0408) (P_2)	1A	Award 1A if $\frac{2}{49}$ given as answer
The probability that one of them will arrive at R and the other one at S		
$s = 2 \times \frac{1}{7} \times \frac{2}{7}$ = $\frac{4}{49}$ (= 0.0816)	1M 1A	$P_2 \times 2$ \uparrow $\circ < \text{題意} < 1$
(ii) The probability that both cars will arrive at S with the first one through Tunnel A and the second one through Tunnel B		
= $\frac{2}{5} \times \frac{2}{7} \times \frac{3}{5} \times \frac{2}{7} = \frac{24}{1225}$ (0.0196) (P_3)	1A	Award 1A if $\frac{24}{1225}$ given as answer
The required probability = $2 \times \frac{24}{1225}$ = $\frac{48}{1225}$ (0.0392)	1M 1A 6	$P_3 \times 2$ \uparrow $\circ < \text{題意} < 1$
		

RESTRICTED 内部文件

Solutions	Marks	Remarks
11. (a) Proof :		
$\angle f_1 = \boxed{\angle a_1}$ ($\angle D A Y$, etc.) (Corr. $\angle s$, $AD // FE$.)	1A	Accept a_1 , etc.
But $\boxed{\angle a_1} = \boxed{\angle e_3}$ (Ext. \angle , cyclic quad.)	1A	1A
$\therefore \angle f_1 = \angle e_3$		
$\therefore EY = \boxed{F Y}$ (Sides opp. equal $\angle s$)	1A	
i.e. $\triangle EFY$ is isosceles		
	3	
(b) Proof :		
$\widehat{BCD} = \widehat{AFE}$ (Given)		
$\therefore \angle a_2 = \boxed{\angle d}$ (Equal arcs subtend equal $\angle s$ at circumference)	1A	
$\therefore BA // DE$ (Alt. $\angle s$ equal)	1	
(c) Proof :		
$\angle a_1 = \boxed{\angle f_1}$ (Corr $\angle s$, $AD // FE$)	1A	
But $\boxed{\angle f_1} = \angle b$ (Ext. \angle , cyclic quad.)	1A	
and $\angle b = \angle e_1$ (Alt. $\angle s$, $BA // DE$)		
$\therefore \angle a_1 = \boxed{\angle e_1}$	1A	
$\therefore A, X, E, Y$ are concyclic.		
	3	
(d) Solution :		
$\angle f_1 = 47^\circ$	1A	Note that $a_1 = a_2 = b = d = f_1 = e_1 = e_3$
$\angle y = 86^\circ$	1M+1A	$y = 180^\circ - f_1 - e_3$
$\angle x = 94^\circ$	1M+1A	or $y = 180^\circ - x$
		$x = 180^\circ - y$
		or $x = b + a_2$
		or $x = e_1 + d$
	5	
		缺第 1 頁

92-CE-Maths. I

P. 6

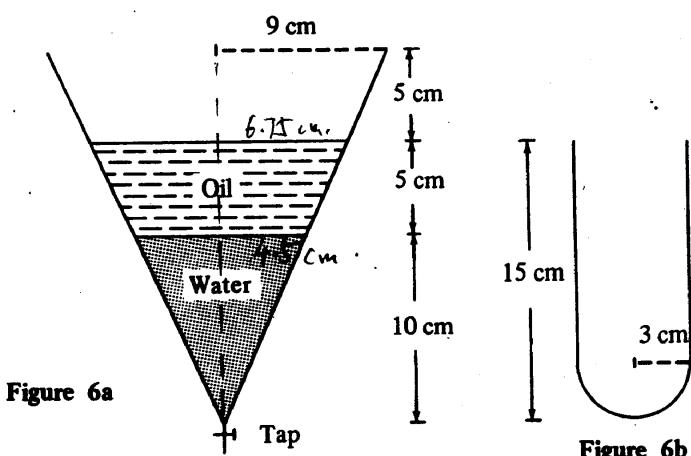
GA 29

RESTRICTED 内部文書

Provided by dse.life

RESTRICTED 内部文件

Solutions	Marks	Remarks
12. (a) (i) Capacity of funnel = $\frac{1}{3}\pi(9)^2 \times 20$ = $540\pi \text{ cm}^3$	1A 1A	
(ii) Vol. of water : total vol. of oil and water : cap of funnel = $10^3 : 15^3 : 20^3$ = $2^3 : 3^3 : 4^3 (= 8:27:64)$ \therefore vol. of water : vol. of oil : capacity of funnel = $8:19:64$	1A+1A 1A 1A	1A for 10:15:20 $\checkmark 10^3 : 15^3 : 20^3$ $\checkmark 8:19:64$
(b) Let the depth of water be h cm. Capacity of bottom part = $\frac{2}{3}\pi \cdot 3^3$ = $18\pi \text{ (cm}^3)$	1A	
$67.5\pi \times \frac{8}{64} = \pi \times 3^2(h - 3) + 18\pi$ \therefore depth = $8\frac{1}{2} \text{ cm}$	1M 1A 3	Equating vol. of water in two forms
(c) Vol. of water : vol. of oil = 8:19 \therefore depth of water : depth of oil = $2 : \sqrt[3]{19}$ \therefore depth of oil = $10 \times \frac{\sqrt[3]{19}}{2} = 5\sqrt[3]{19} \text{ cm (13.3 cm)}$	2M 1A 3	



RESTRICTED 内部文件

	Solutions	Marks	Remarks
12.	<p><u>Alternatively:</u></p> <p>(a) (ii) Vol. of water = $\frac{1}{3}\pi \left(\frac{9}{20}\right)^2 \times 10 = 67.5\pi \text{ (cm}^3)$</p> <p>Vol. of water + oil = $\frac{1}{3}\pi \left(\frac{9}{20}\right)^2 \times 15 = 227.8125\pi \text{ (cm}^3)$</p> <p>$\therefore$ vol. of water : vol. of oil : cap. of funnel $= 67.5\pi : 227.8125\pi : 540\pi$ $= 8 : 27 : 64$</p> <p>Vol. of water : vol. of oil : cap. of funnel $= 8 : 19 : 64$</p> <p>(c) Let the depth of the oil be h cm, the radius of the oil surface be r cm.</p> <p>Then $\frac{r}{h} = \frac{9}{20}$</p> <p>Volume of oil remaining = $\frac{1}{3}\pi r^2 h$ $= \frac{1}{3}\pi \left(\frac{9h}{20}\right)^2 h \text{ (cm}^3)$</p> <p>But volume of oil = $540\pi \times \frac{19}{64} \text{ (cm}^3)$</p> <p>$540\pi \times \frac{19}{64} = \frac{1}{3}\pi \left(\frac{9h}{20}\right)^2 h$</p> <p>$\frac{135 \times 19}{16} = \frac{27}{400} h^3$</p> <p>Depth = $5 \times \sqrt[3]{19} \text{ cm } (13.34 \text{ cm})$</p>	1A 1A 1A 1A	1565 Sub r

$$\frac{540\pi \left(\frac{19}{64}\right)}{640\pi} = \left(\frac{h}{20}\right)^3$$

$$135\pi : 16 = 540\pi : 640\pi$$

RESTRICTED 内部文件

Solutions	Marks	Remarks
13. (a) $C = (9, 7)$ (or $x = 9, y = 7$)	1A	8.7 (part)
Radius = $\sqrt{9^2 + 7^2 - 105} = 5$	1A 2	
(b) Putting $y = mx$,	1A	
$x^2 + (mx)^2 - 18x - 14(mx) + 105 = 0$	1A	
$(1 + m^2)x^2 - (18 + 14m)x + 105 = 0$	1A	
As x_1, x_2 are the roots, $x_1 x_2 = \frac{105}{1 + m^2}$	1A 2	Only awarded if above correct As x_1, x_2 are the roots.
(c) $OA = \sqrt{x_1^2 + y_1^2}$	1A	{ optional }.
$= \sqrt{x_1^2 + (mx_1)^2}$	1A	
$(= (\sqrt{1 + m^2}) x_1)$	2 + 1	
$OB = \sqrt{x_2^2 + y_2^2} = \sqrt{x_2^2 + (mx_2)^2} (= (\sqrt{1 + m^2}) x_2)$	1A	
$\therefore OA \times OB = (1 + m^2) x_1 x_2$	1A	
$= 105$	1A 4	
(d) Let M = mid-point of AB . If $CM = 3$,	1M	(已知兩點，但因學生誤寫)
$AM = \sqrt{5^2 - 3^2} (= 4)$	1A	由圖知
$\therefore AB = 2 \times 4 = 8$	1A	由圖知
Let $OA = x$, then	1M	OR
$x(x + 8) = 105$	1M	
$x^2 + 8x - 105 = 0$		
$(x - 7)(x + 15) = 0$		
$\therefore x = 7$ (as $x \neq -15$)	1A 4	$\therefore OA = OM - AM$ $= 11 - 4 = 7$ 1A

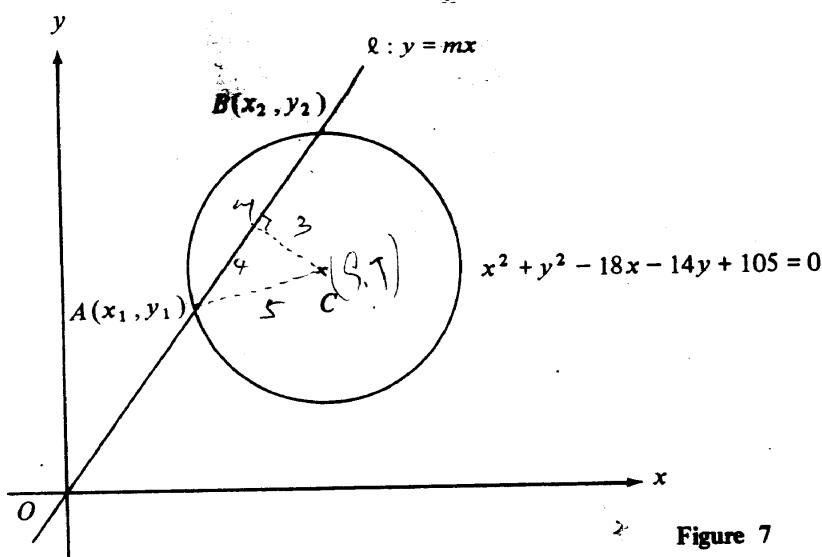
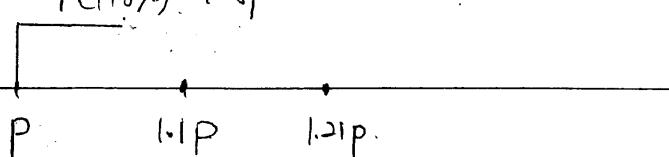


Figure 7

RESTRICTED 内部文件

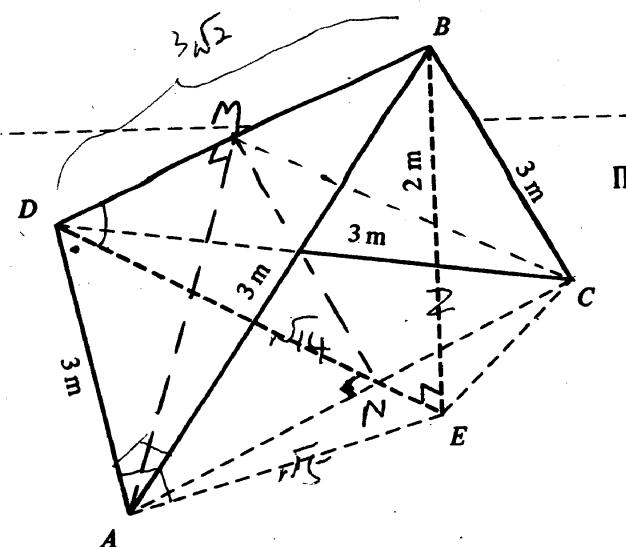
Solutions	Marks	Remarks
14. (a) The common ratio = $\frac{b}{a}$	1A	
The sum to n terms = $\frac{a^n \left[1 - (\frac{b}{a})^n \right]}{1 - \frac{b}{a}}$ $= \frac{a(a^n - b^n)}{a - b} \quad (= \frac{a^{n+1} - ab^n}{a - b})$	1M 1A 3	or $a^n - \frac{b}{a}(ab^{n-1})$ $1 - \frac{b}{a}$
(b) (i) The balance at the end of (1) the 1st year = \$1.08P (2) the 2nd year = \$(1.08^2 P + 1.1 \times 1.08P) (3) the 3rd year = \$(1.08^3 P + 1.1 \times 1.08^2 P + 1.1^2 \times 1.08P)	1A 1A+1A 1A	= (1 + 8%)P = 1.1664P + 1.188P = 2.3544P = 3.849552P
(ii) At the end of the n th year, the balance $= \$P[1.08^n + 1.08^{n-1} \times 1.1 + 1.08^{n-2} \times 1.1^2 + \dots + 1.08^2 \times 1.1^{n-2} + 1.08 \times 1.1^{n-1}]$ $= \$P \frac{1.08(1.08^n - 1.1^n)}{1.08 - 1.1}$ $= \$54P(1.1^n - 1.08^n)$	2A 1 7	
(c) In n years' time, the flat is worth \$1080000 $\times 1.15^n$ Put $P = 20000$, the amount in the man's account $= \$1080000(1.1^n - 1.08^n)$ $< \$1080000 \times 1.15^n$ $P(1+8\%) = 1.08P$ 	1A 1A 1A 2	

(-, 13.

$$\begin{aligned}
 & (1.08P + 1.1P) \times (1+8\%) \\
 & = (1.08P + 1.1P) \times 1.08 \\
 & = 1.08^2 P + 1.1 \times 1.08 \times P
 \end{aligned}$$

RESTRICTED 内部文件

Solutions	Marks	Remarks
15. (a) $BD = \sqrt{3^2 + 3^2} = 3\sqrt{2} \text{ m } (\sqrt{18} \text{ m})$	1A	4.24, withhold 1 mk if answers not in surd form
$ED = \sqrt{BD^2 - BE^2}$ = $\sqrt{18 - 4}$ = $\sqrt{14} \text{ m}$	1A	3.74
$AE = \sqrt{BA^2 - BE^2}$ = $\sqrt{9 - 4}$ = $\sqrt{5} \text{ m}$	<u>1A</u> <u>3</u>	2.24
(b)		
$\cos \angle ADE = \frac{3^2 + (\sqrt{14})^2 - (\sqrt{5})^2}{2 \times 3 \times \sqrt{14}} (= 0.8018)$	1M+1A	
$\therefore \angle ADE = 36.7^\circ$	1A	36.5°~36.8°
<u>Alternatively :</u> As $\angle DAE = 90^\circ$ $\tan \angle ADE = \frac{AE}{AD} = \frac{\sqrt{5}}{3}$ $\therefore \angle ADE = 36.7^\circ$	1A 1M <u>1A</u> <u>3</u>	Follow through if omitted 36.5°~36.8°
(c) $\sin \angle BDE = \frac{2}{\sqrt{18}} (= 0.4714)$ $\therefore \angle BDE = 28.1^\circ$ (28.1255)	1M <u>1A</u> <u>2</u>	or $\tan \angle BDE = \frac{2}{\sqrt{14}}$ or $\cos \angle BDE = \frac{\sqrt{14}}{\sqrt{18}}$



RESTRICTED 内部文件

Solutions	Marks	Remarks
<p>(d) Let M be a point on BD such that (or mid-pt of BD, etc.) 1M $AM \perp BD$. We have $DM = MB$ as $AB = AD$.</p> <p>Let N be the mid-point of AC.</p> <p>Then $MN \perp AC$ as $AM = MC$.</p> <p>Similarly $DN \perp AC$.</p> <p>Now $\sin \angle ADE = \frac{AN}{AD}$</p> <p>$\therefore AN = 3 \sin 36.7^\circ \text{ m } (= 1.7928)$</p> <p>$AM = \frac{1}{2} BD = \frac{3}{2} \sqrt{2} \text{ m}$</p> <p>$\sin \angle AMN = \frac{AN}{AM} = \frac{3 \sin 36.7^\circ}{\frac{3}{2} \sqrt{2}} (= 0.84515)$</p> <p>$\therefore \angle AMN = 57.69 \text{ (57.6885)}$</p> <p>$\therefore \angle AMC = 2 \times 57.69 = 115^\circ (-116^\circ)$</p>	1A	Considering AM See also alt. solution $3 \sin 36.5^\circ -$ $3 \sin 36.8^\circ$
	1M	Attempt to find $\angle AMN$ or $\angle AMC$
	<u>1A</u> <u>4</u>	

Alternatively:

$$\text{Now } \sin \angle ADE = \frac{AN}{AD}$$

$$\therefore AC = 2AN = 2 \times 3 \sin 36.7^\circ \text{ m } (= 3.5858)$$

$$AM = \frac{1}{2} BD = \frac{3}{2} \sqrt{2} \text{ m}$$

By the cosine formula,

$$\cos \angle AMC = \frac{\left(\frac{3}{2} \sqrt{2}\right)^2 + \left(\frac{3}{2} \sqrt{2}\right)^2 - (2 \times 3 \sin 36.7^\circ)^2}{2 \left(\frac{3}{2} \sqrt{2}\right) \left(\frac{3}{2} \sqrt{2}\right)}$$

$$= -0.4286$$

$$\therefore \angle AMC = 115^\circ (-116^\circ)$$

1A

1M

Attempt to
find $\angle AMC$

1A

--	--	--

1992

1. (a)
- $\frac{\pi}{6}$
- (radian)

C E
 (b) $x = 150^\circ (\frac{5\pi}{6}, 2.62)$

Math. (c) $\cos A$

2. (a)
- $p + q$
-
- (b) -2
-
- (c)
- $\sqrt{3} - \sqrt{2}$

3. (a)
- $y \geq \frac{1}{2}$

$2x - y \geq 2$

$3x + 5y \leq 30$

(b) 16

4. (a) (i)
- $x^2 - 2x = x(x - 2)$

(ii) $x^2 - 6x + 8 = (x - 2)(x - 4)$

$$\begin{aligned}
 \text{(b)} \quad & \frac{1}{x^2 - 2x} + \frac{1}{x^2 - 6x + 8} = \frac{1}{x(x - 2)} + \frac{1}{(x - 2)(x - 4)} \\
 & = \frac{(x - 4) + x}{x(x - 2)(x - 4)} \\
 & = \frac{2x - 4}{x(x - 2)(x - 4)} \\
 & = \frac{2}{x(x - 4)} \quad \left(= \frac{2}{x^2 - 4x} \right)
 \end{aligned}$$

5. (a) Slope of
- $L_2 = \frac{1}{2}$

Slope of $L_1 = -2$ Equation of $L_1 : y - 5 = -2(x - 10)$

i.e. $2x + y - 25 = 0$

- (b) Solving
- $\begin{cases} x - 2y + 5 = 0 \\ 4x + 2y - 50 = 0 \end{cases}$

$5x - 45 = 0$

$x = 9$ (or $y = 7$)

 $\therefore L_1$ and L_2 meet at (9, 7)

6. For distinct real roots

$a = (2k)^2 - 4(k + 6) > 0$

$4k^2 - 4k - 24 > 0$

$(k + 2)(k - 3) > 0$

$k < -2$ or $k > 3$

7. (a)
- $\angle AOB = \frac{360^\circ}{5} = 72^\circ \left(= \frac{2\pi}{5} = 1.26 \text{ radians} \right)$

$$\begin{aligned}
 \text{Area of } \triangle OAB &= \frac{1}{2}(10)(10)\sin 72^\circ \\
 &\approx 47.6 \quad (47.5528)
 \end{aligned}$$

$$\begin{aligned}
 \text{(b) Area of sector } OAB &= \frac{1}{5} \cdot \pi 10^2 \\
 &\approx 20\pi \quad (62.83) \\
 \text{Area of shaded part} &= 20\pi - 47.55 \\
 &\approx 15.3 \quad (15.2790)
 \end{aligned}$$

8. (a) Total score of the team
- $= 70(m + n)$

$$\begin{aligned}
 \text{(b) Total score is also equal to } 75m + 62n. \\
 75m + 62n = 70(m + n) \\
 5m = 8n
 \end{aligned}$$

$m : n = 8 : 5$

$$\begin{aligned}
 \text{(c) The number of men} &= 39 \times \frac{8}{8+5} \\
 &\approx 24
 \end{aligned}$$

9. (a) (i) Area of
- $OAPB = a \times b$

$= a(2a^2 - 4a + 3)$

$= 2a^3 - 4a^2 + 3a$

- (ii) For
- $OAPB$
- to be a square,
- $a = b$

$a = 2a^2 - 4a + 3$

$2a^2 - 5a + 3 = 0$

$(2a - 3)(a - 1) = 0$

$\therefore a = \frac{3}{2}$ or 1

- (b) (i) If the area of
- $OAPB = \frac{3}{2}$
- ,

$2a^3 - 4a^2 + 3a = \frac{3}{2}$

$$\begin{aligned}
 \therefore 4a^3 - 8a^2 + 6a - 3 &= 0 \dots \dots \dots \dots \dots \dots \quad (*)
 \end{aligned}$$

(iii) Let $f(a) = 4a^3 - 8a^2 + 6a - 3$

$f(1.2) < 0$ (≈ -0.408) and $f(1.3) > 0$ ($= 0.068$)

(*) has a root lying between 1.2 and 1.3

92 - 1